

Software specification in CASL - Datatypes

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October 2006

Free datatypes: Natural numbers

spec NAT =

free type $Nat ::= 0 \mid suc(Nat)$

preds $---<=---, --->=--- : Nat \times Nat$

ops $---+--- : Nat \times Nat \rightarrow Nat;$

$\forall m, n, r, s, t: Nat$

%% axioms concerning predicates

- $0 <= n$ %(leq_def1_Nat)%
- $\neg suc(n) <= 0$ %(leq_def2_Nat)%
- $suc(m) <= suc(n) \Leftrightarrow m <= n$ %(leq_def3_Nat)%
- $m >= n \Leftrightarrow n <= m$ %(geq_def_Nat)%

%% axioms concerning operations

- $0 + m = m$

%(add_0_Nat)%

- $suc(n) + m = suc(n + m)$

%(add_suc_Nat)%

end

Lists

```

spec LIST [sort Elem] = %mono
  free type List[Elem] ::= [] | ___::__(Elem; List[Elem])
  op    ___++___ : List[Elem] × List[Elem] → List[Elem]
  ∀ x: Elem; L, K: List[Elem]
  %% axioms concerning operations
  • [] ++ K = K                                %(concat_nil_List)%
  • (x :: L) ++ K = x :: (L ++ K)          %(concat_NeList_List)%
end

```

Mutually Recursive Datatypes

```
spec UNBOUNDEDBRANCHINGTREE[sort Elem] =  
free types  
Tree ::= Leaf(Elem) | Branch(Forest);  
Forest ::= Nil | Cons(Tree; Forest)  
end
```