

Logik für Informatiker Logic for computer scientists

Strategies in Fitch

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WiSe 2011/12

Conjunction Elimination (\wedge Elim)

$$\triangleright \left| \begin{array}{l} P_1 \wedge \dots \wedge P_i \wedge \dots \wedge P_n \\ \vdots \\ P_i \end{array} \right.$$

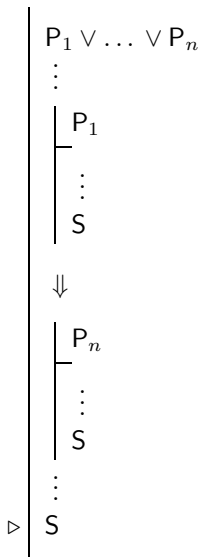
Conjunction Introduction (\wedge Intro)

$$\begin{array}{l} | \\ | \\ P_1 \\ | \\ \Downarrow \\ | \\ P_n \\ | \\ \vdots \\ | \\ \triangleright P_1 \wedge \dots \wedge P_n \end{array}$$

Disjunction Introduction (\vee Intro)

$$\triangleright \left| \begin{array}{l} P_i \\ \vdots \\ P_1 \vee \dots \vee P_i \vee \dots \vee P_n \end{array} \right.$$

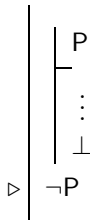
Disjunction Elimination (\vee Elim)



\perp Introduction (\perp Intro)

	P
	⋮
	$\neg P$
	⋮
\triangleright	\perp

Negation Introduction (\neg Intro)



Negation Elimination (\neg Elim)

$$\begin{array}{l|l} & \neg\neg P \\ & \vdots \\ \triangleright & P \end{array}$$

\perp Elimination

(\perp Elim)

$$\begin{array}{c|c} & \perp \\ & \vdots \\ \triangleright & P \end{array}$$

Strategies and tactics in Fitch

- 1 *Understand* what the sentences are saying.
- 2 *Decide* whether you think the conclusion follows from the premises.
- 3 If you think it does not follow, or are not sure, try to find a *counterexample*.
- 4 If you think it does follow, try to give an *informal proof*.
- 5 If a *formal proof* is called for, use the *informal proof to guide* you in finding one.
- 6 In giving consequence proofs, both formal and informal, don't forget the tactic of *working backwards*.
- 7 In working backwards, though, always check that your *intermediate goals are consequences* of the available information.

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Strategies in Fitch, cont'd

- Always try to *match* the situation in your proof with the *rules* in the book (see book appendix for a complete list)
- Look at the *main connective* in a *premise*, apply the corresponding *elimination rule* (forwards)
- Or: look at the *main connective* in the *conclusion*, apply the corresponding *introduction rule* (backwards)