

HYBRIS – Efficient Analysis of Hybrid Systems

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Outline

1. HybridUML – Specification Formalism for Hybrid Systems
2. Automated Model-Based Code Generation – The Hybrid Low-Level Framework HL^3 as Compilation Target for Real-Time Specification Formalisms
3. Automated Testing against (Hybrid) Real-Time Specifications – Timed CSP, HybridCSP, HybridUML
4. Domain-Specific Descriptions for Railway Control Systems

HybridUML – Specification Formalism for Hybrid Systems

- Formal Semantics

- UML

HybridUML – Specification Formalism for Hybrid Systems

- Formal Semantics

- + Hybrid automata (Henzinger)
- + Hierarchic Modelling
- + Semantics by Transformation $\Rightarrow HL^3$
- + Semantically well-defined
- + Executable in Hard Real-Time

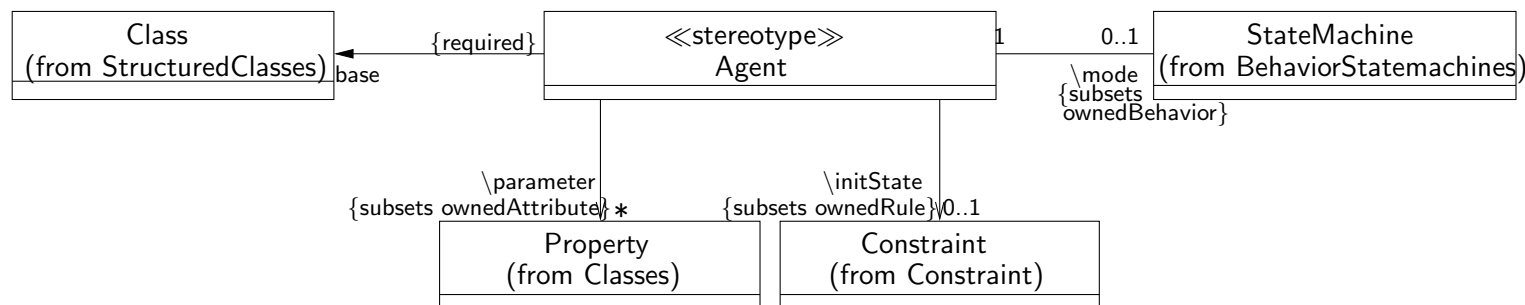
- UML

HybridUML – Specification Formalism for Hybrid Systems

- Formal Semantics

- UML

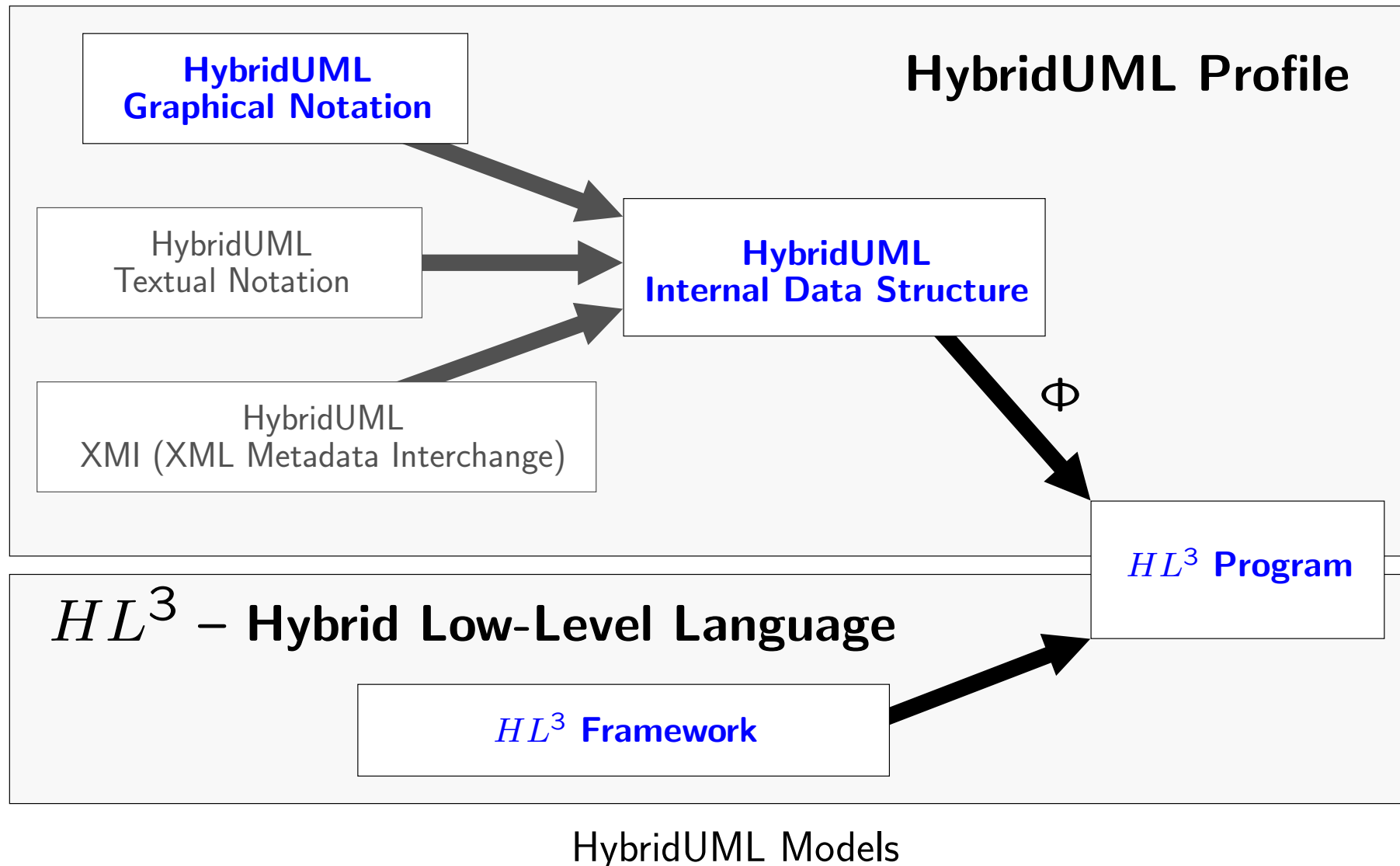
+ Customisation of UML 2.0 – HybridUML Profile:



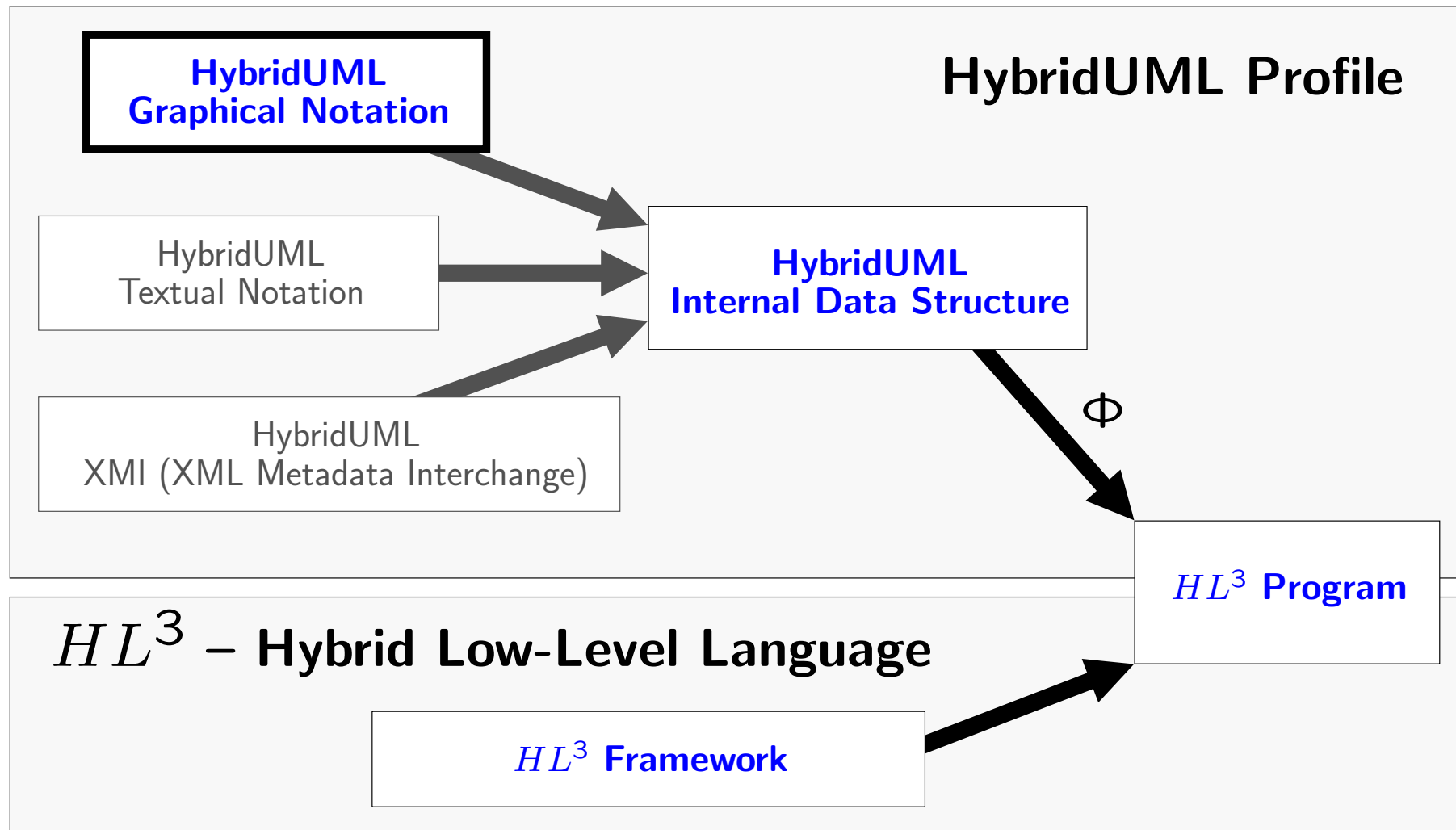
Additional constraints, i.e. `self.mode->forAll(oclIsTypeOf (Mode))`

+ Enhanced by (time-continuous) Flow Constraints and Invariants

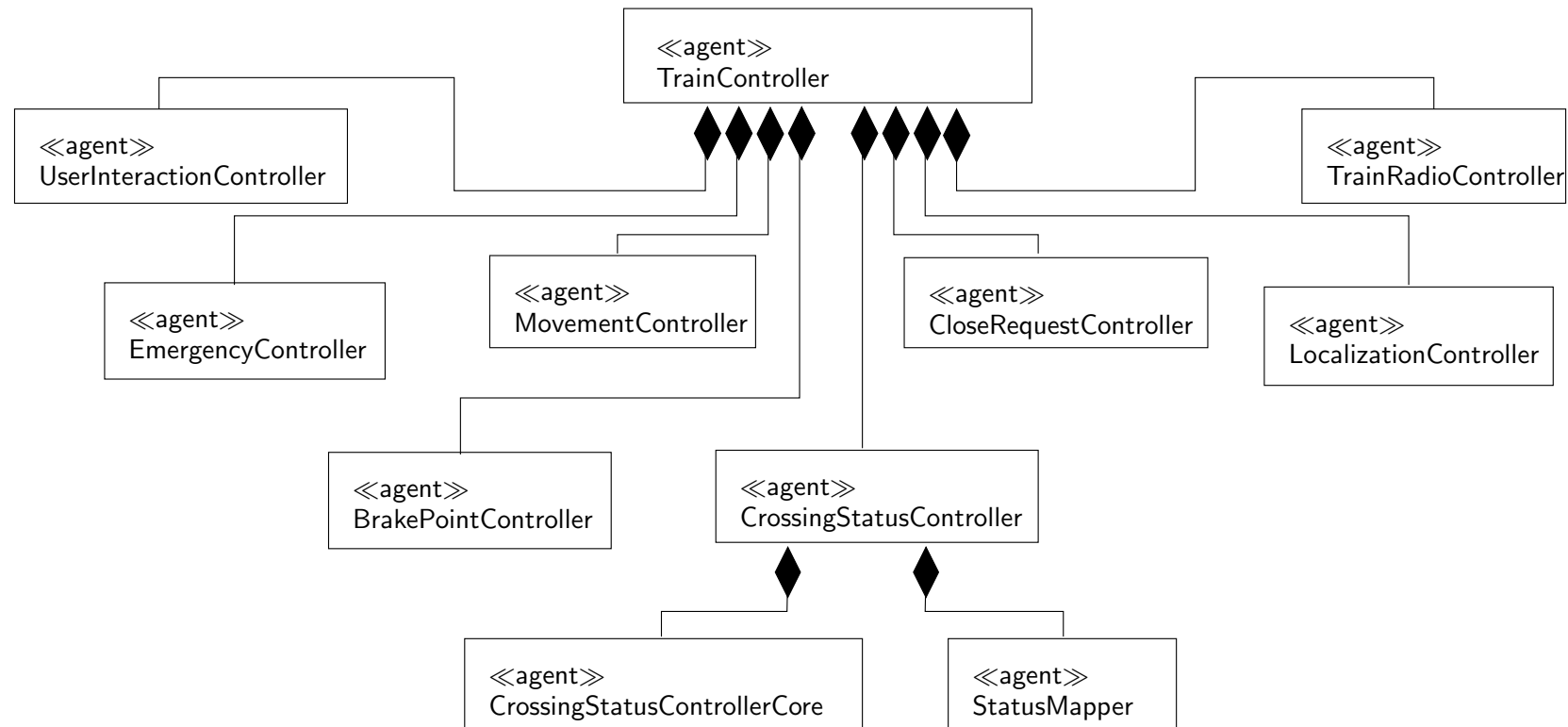
HybridUML – Specification Formalism for Hybrid Systems



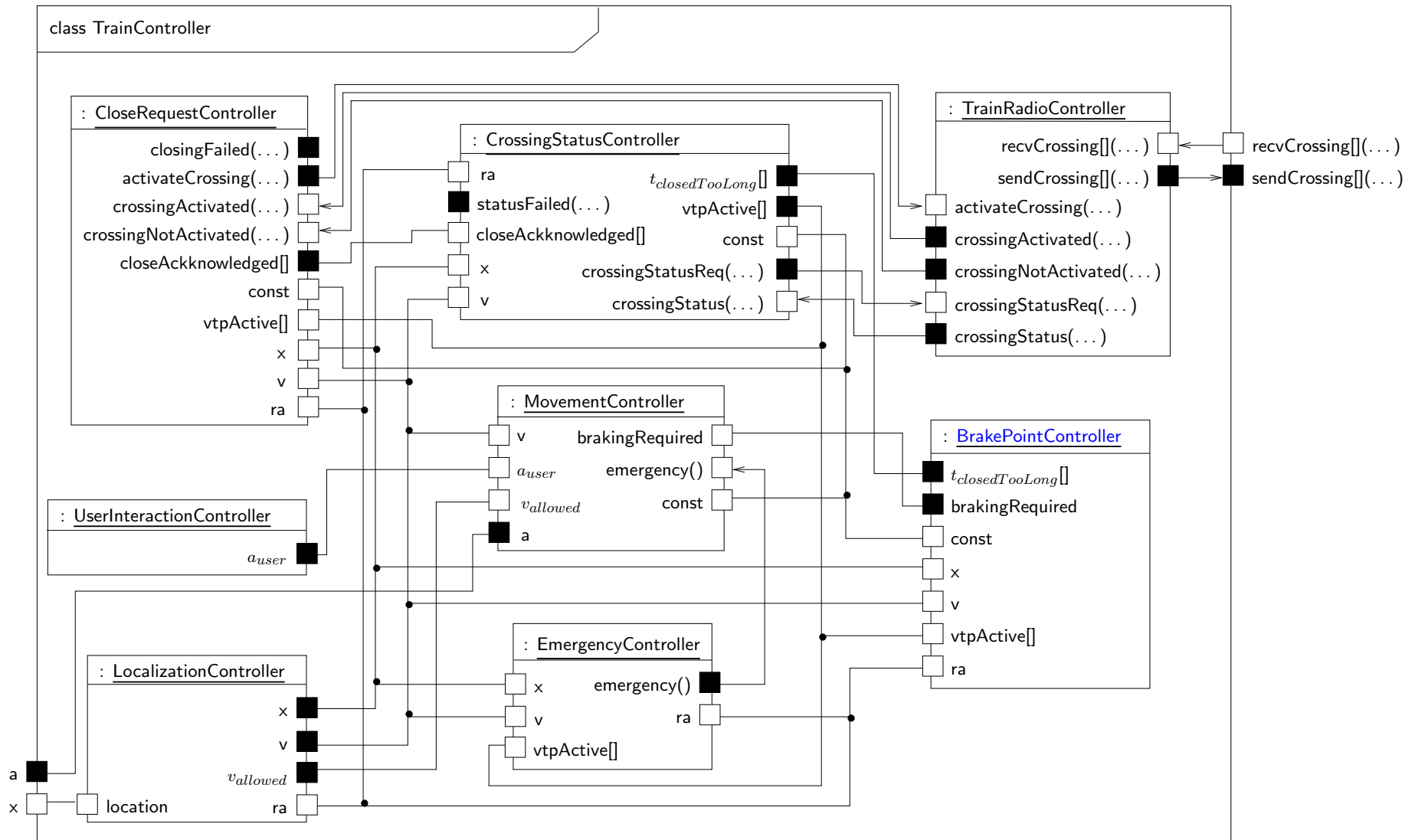
HybridUML Graphical Notation



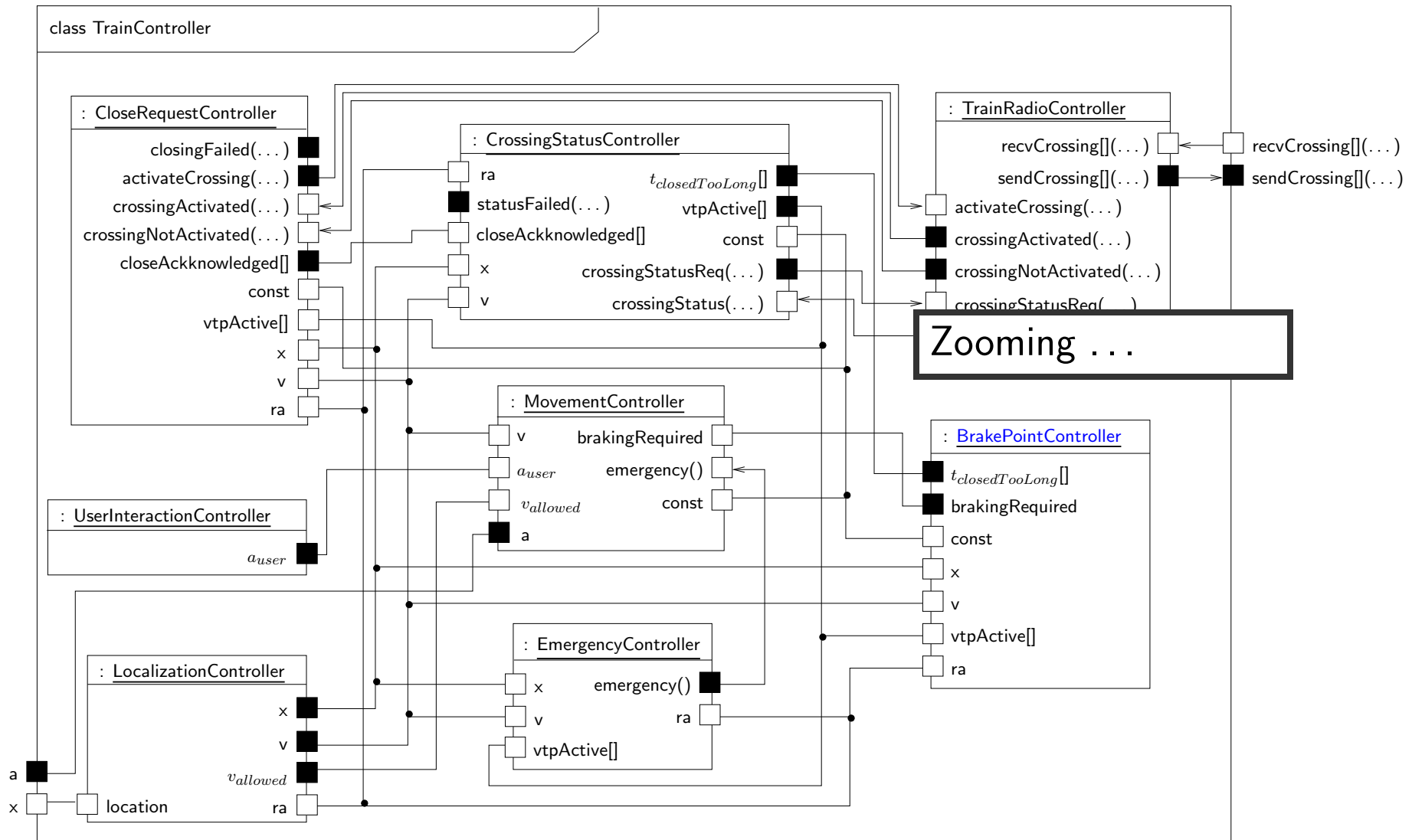
HybridUML Models – Graphical Notation



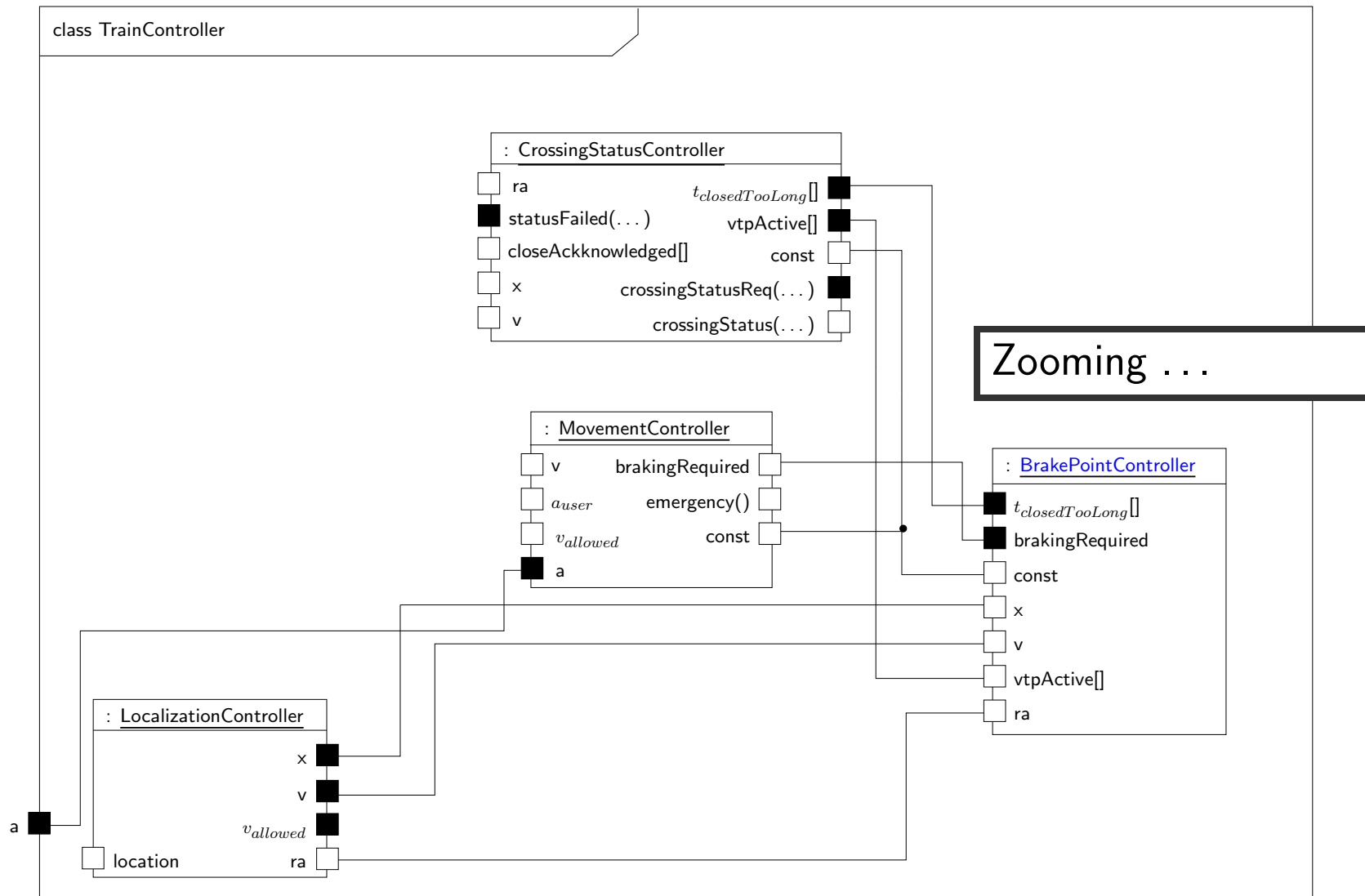
Class diagram of TrainController



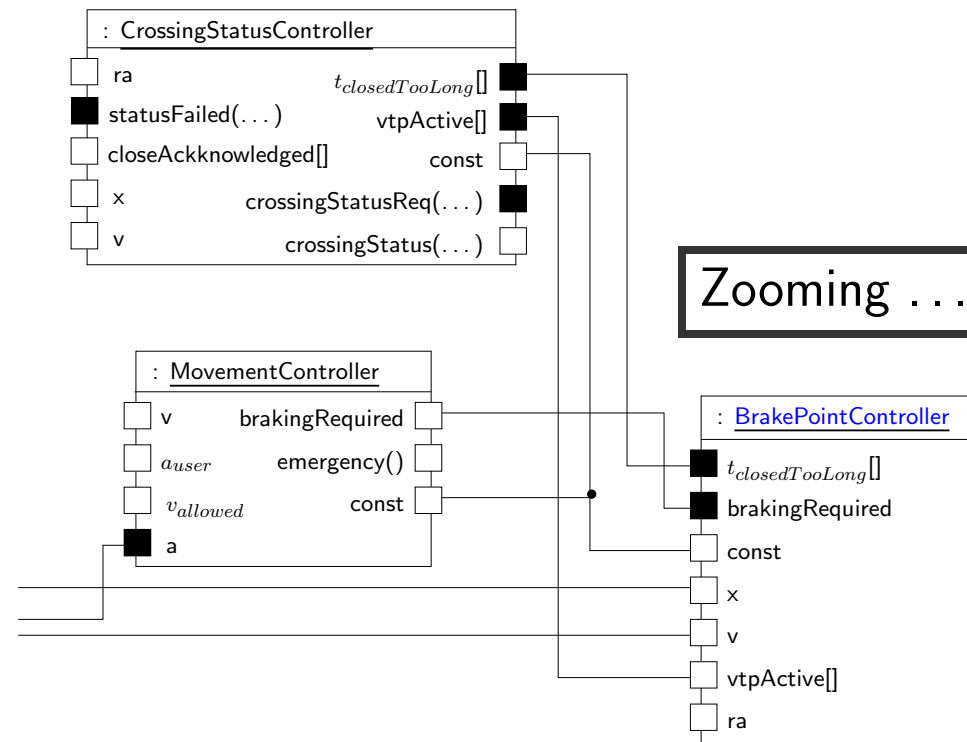
Structure diagram of TrainController



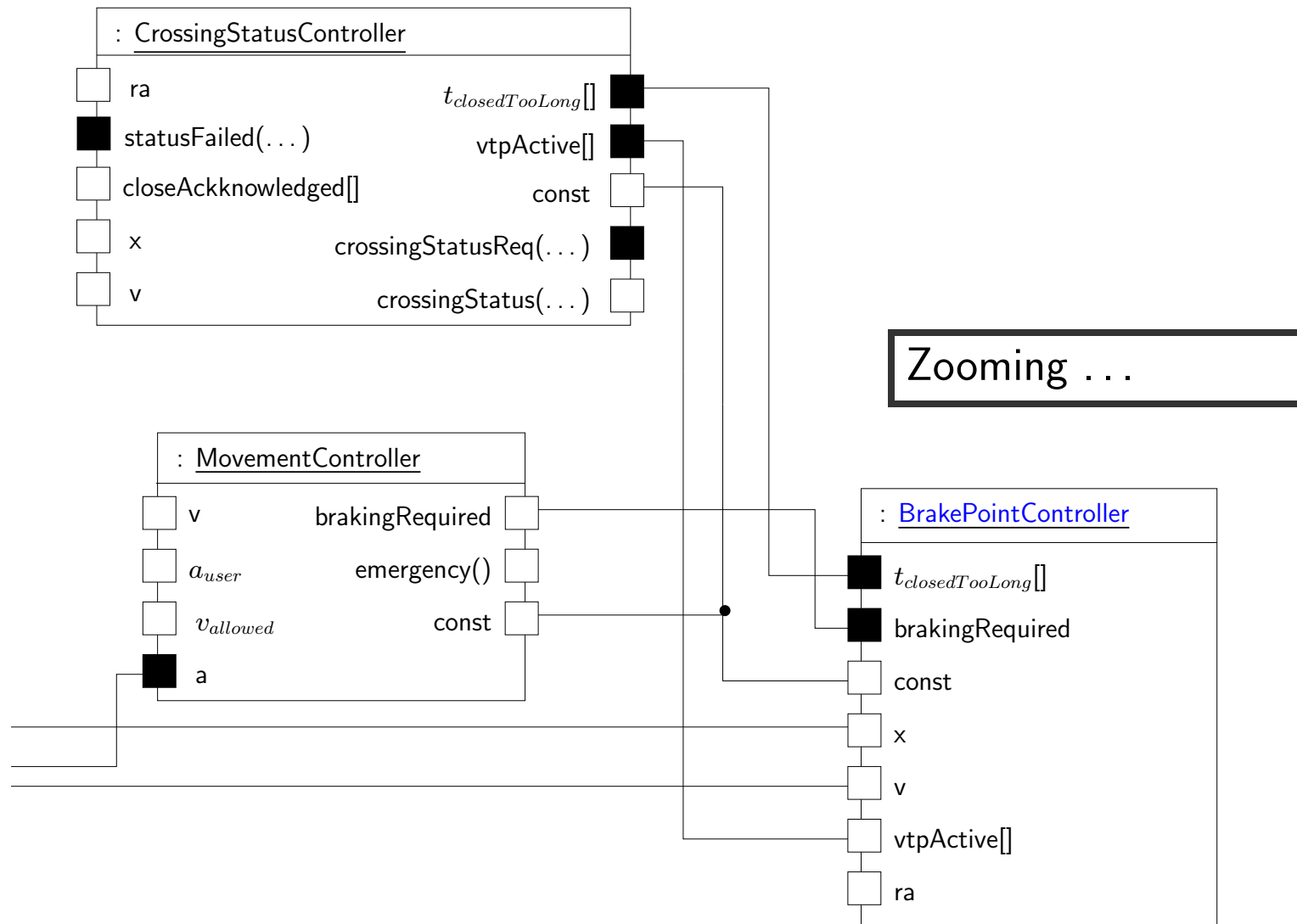
Structure diagram of TrainController



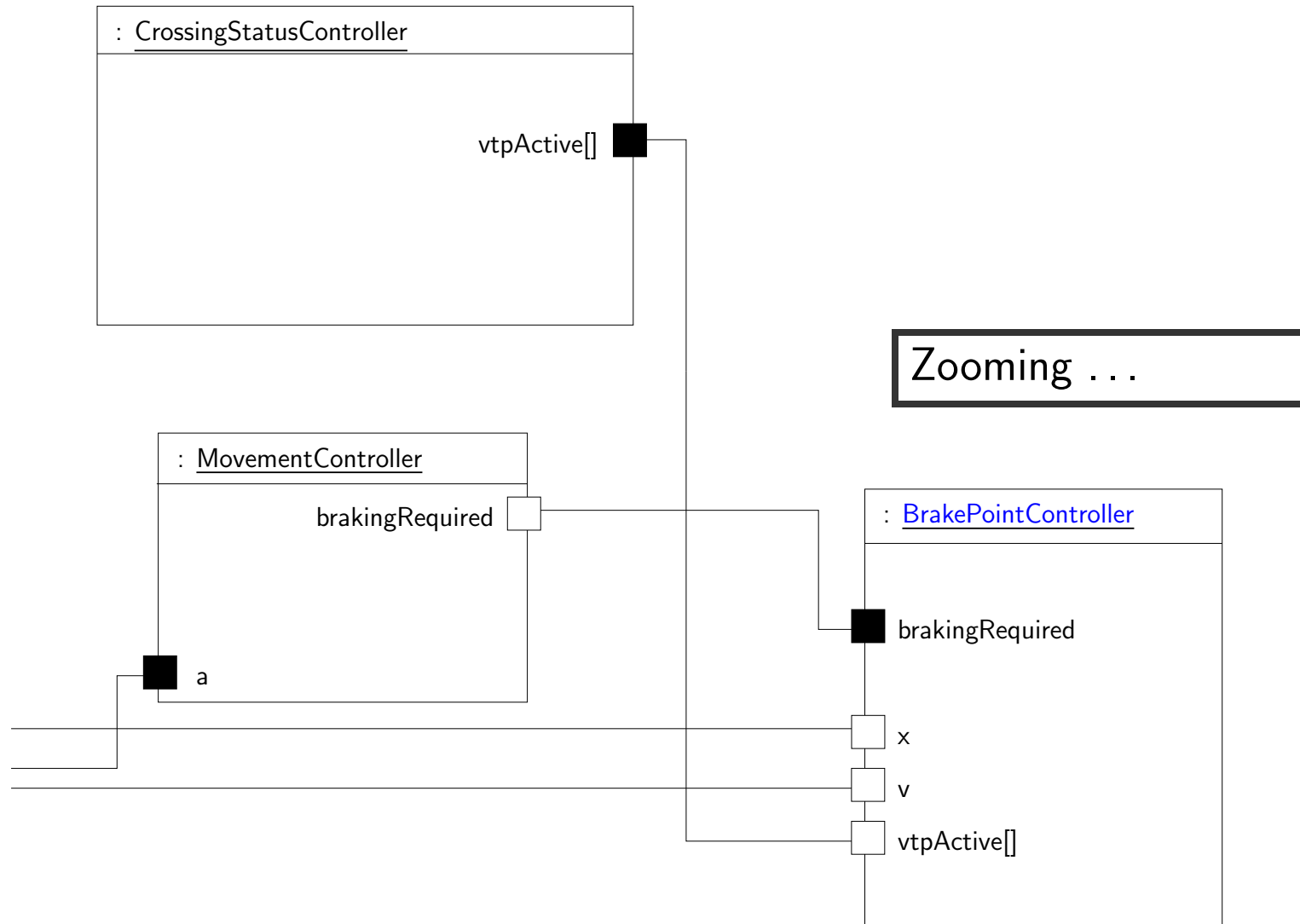
Focus on BrakePointController



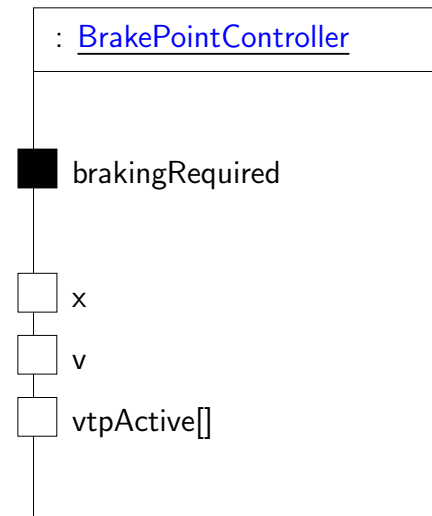
Focus on BrakePointController



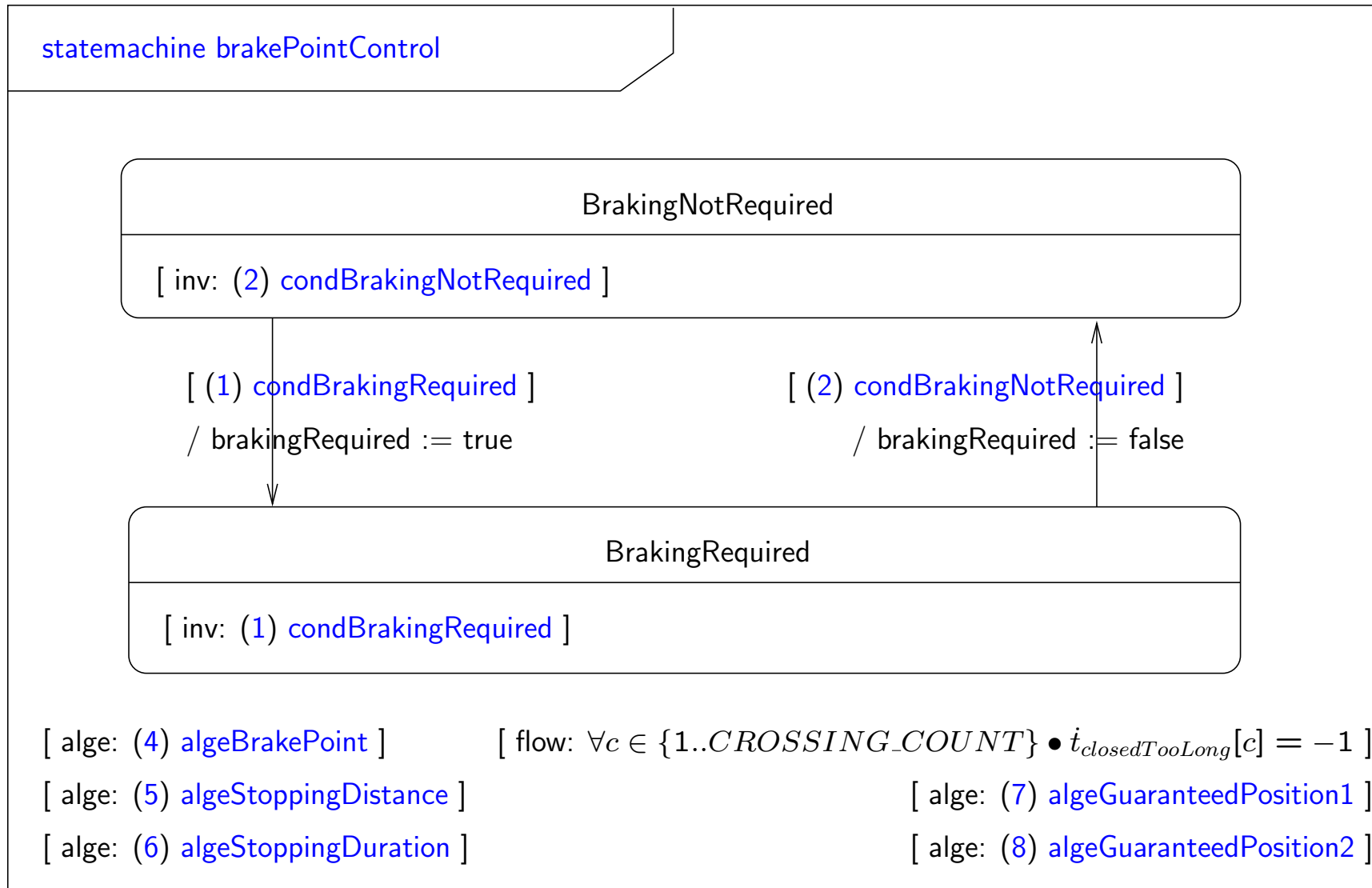
Focus on BrakePointController



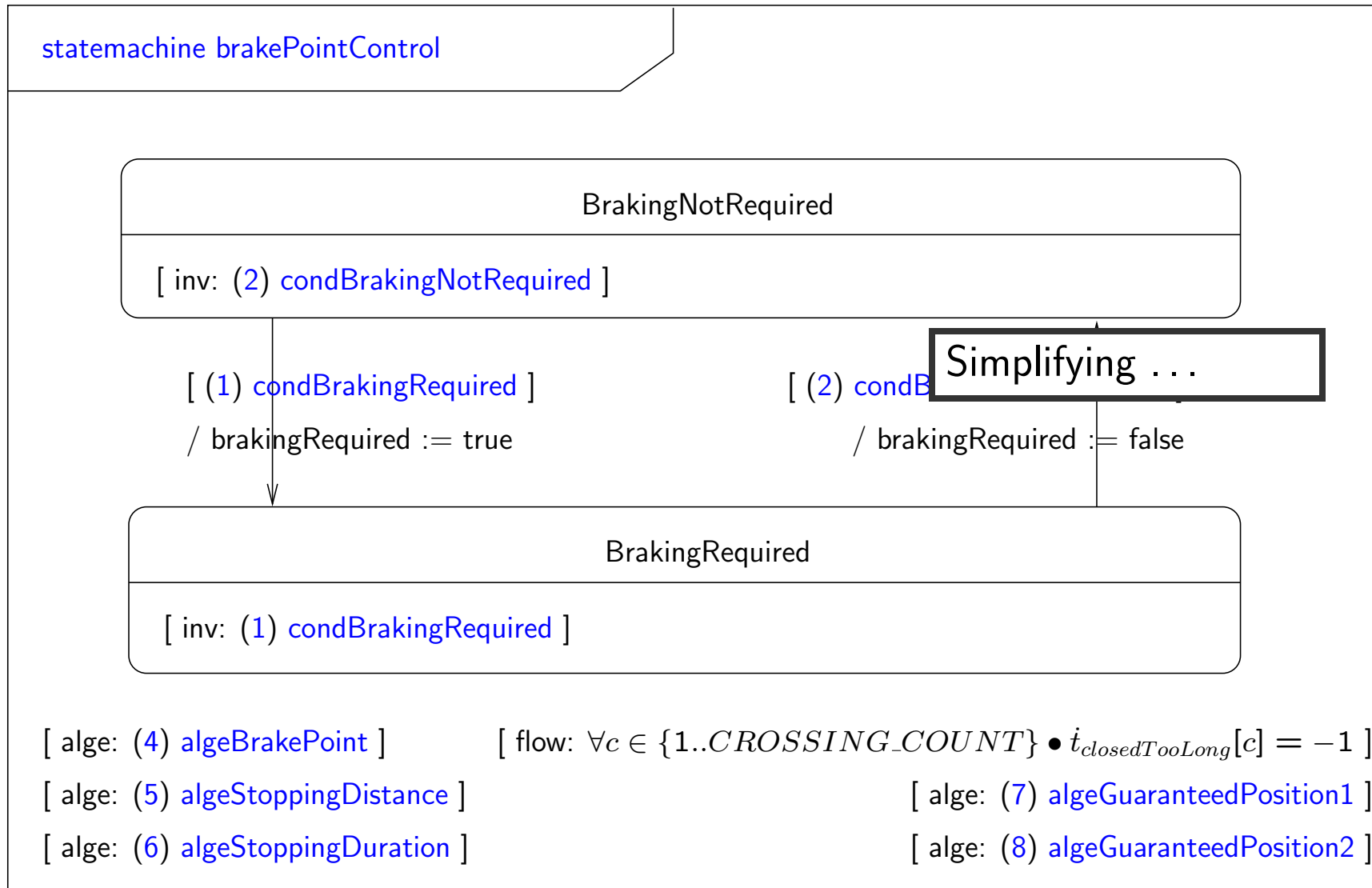
Focus on BrakePointController



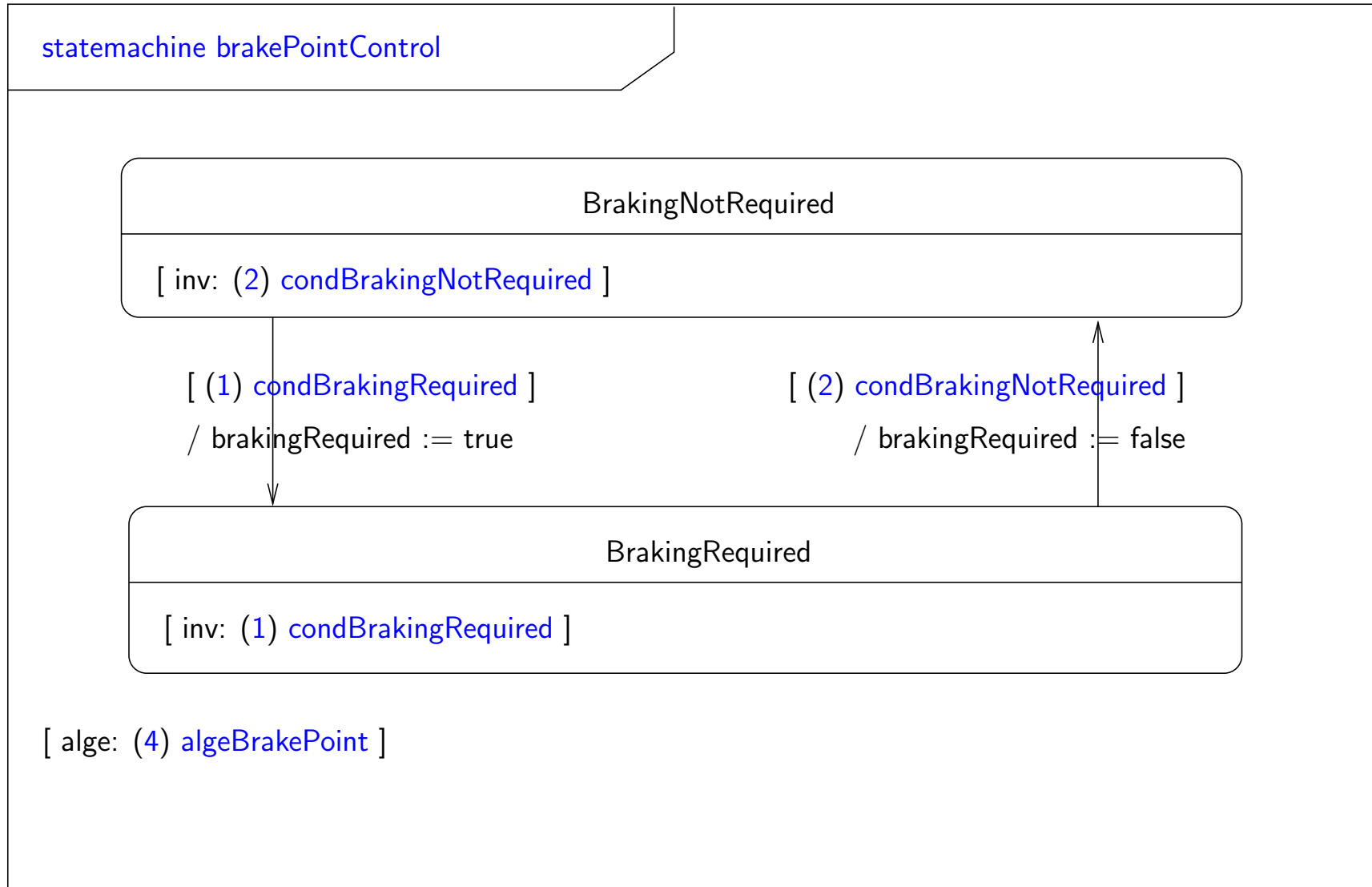
Focus on BrakePointController



Behaviour of BrakePointController

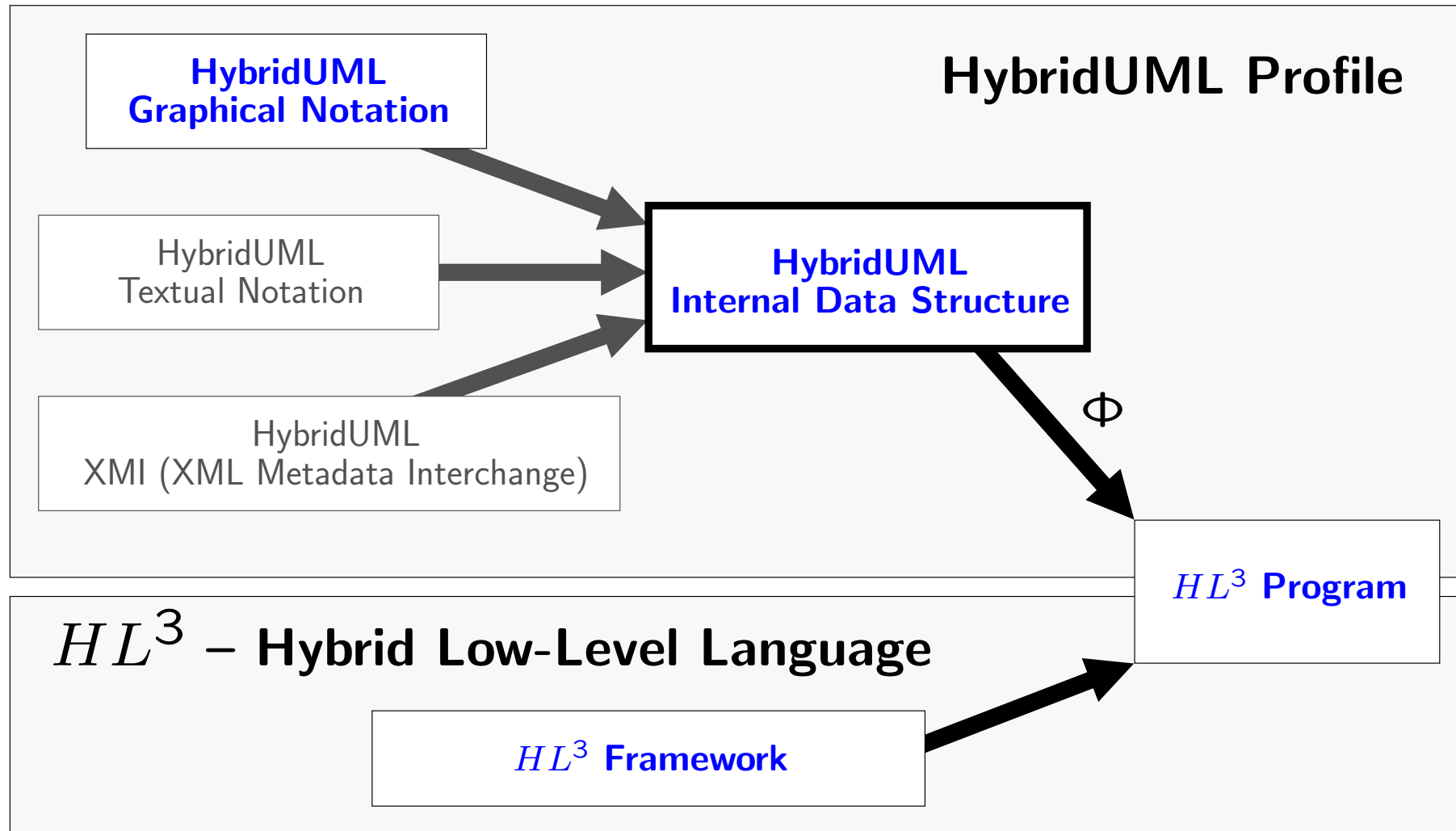


Behaviour of BrakePointController

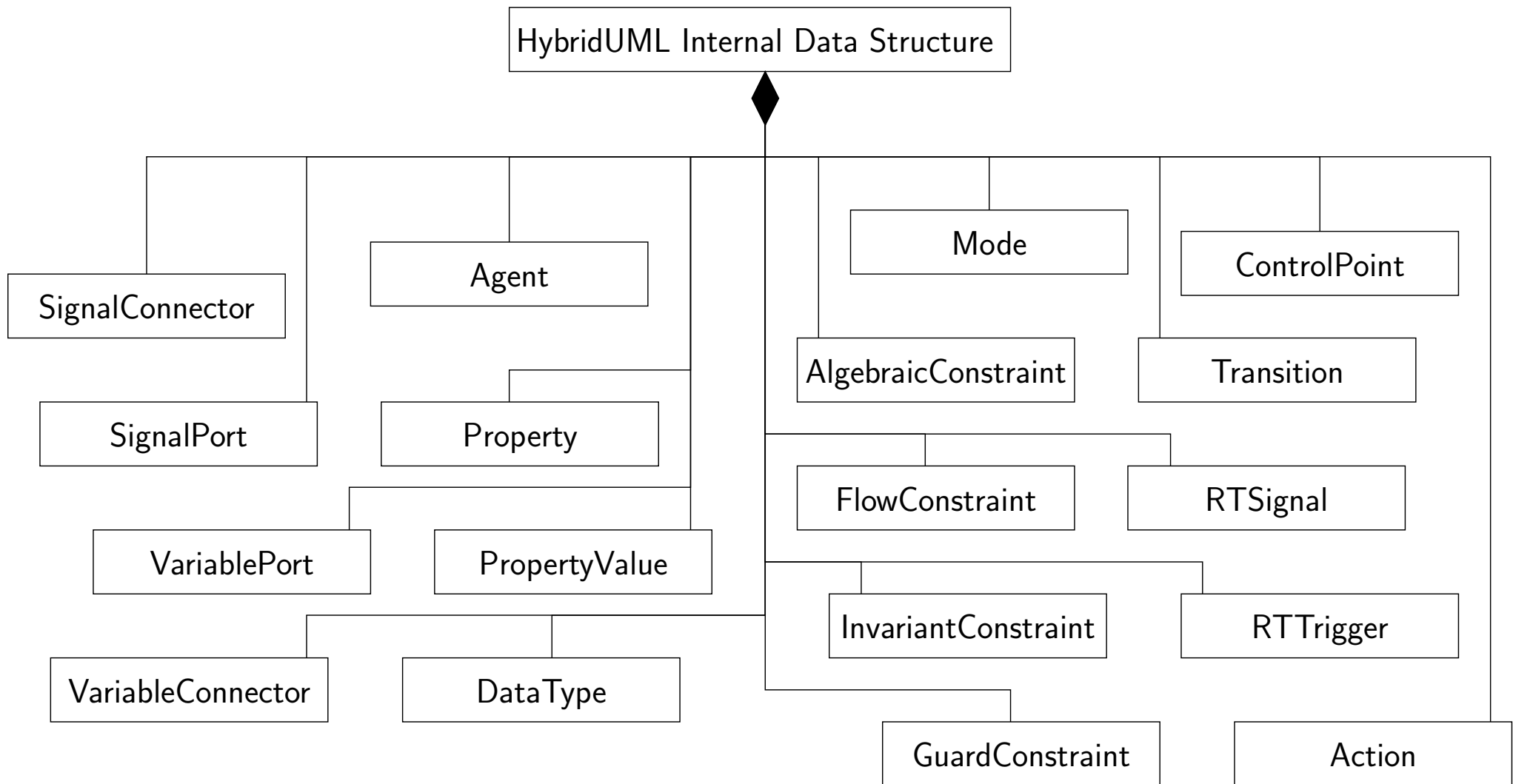


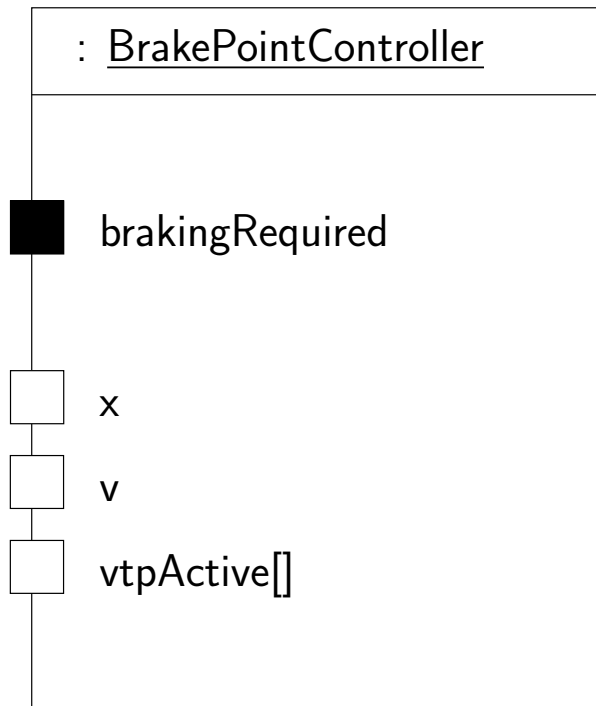
Simplified behaviour of BrakePointController

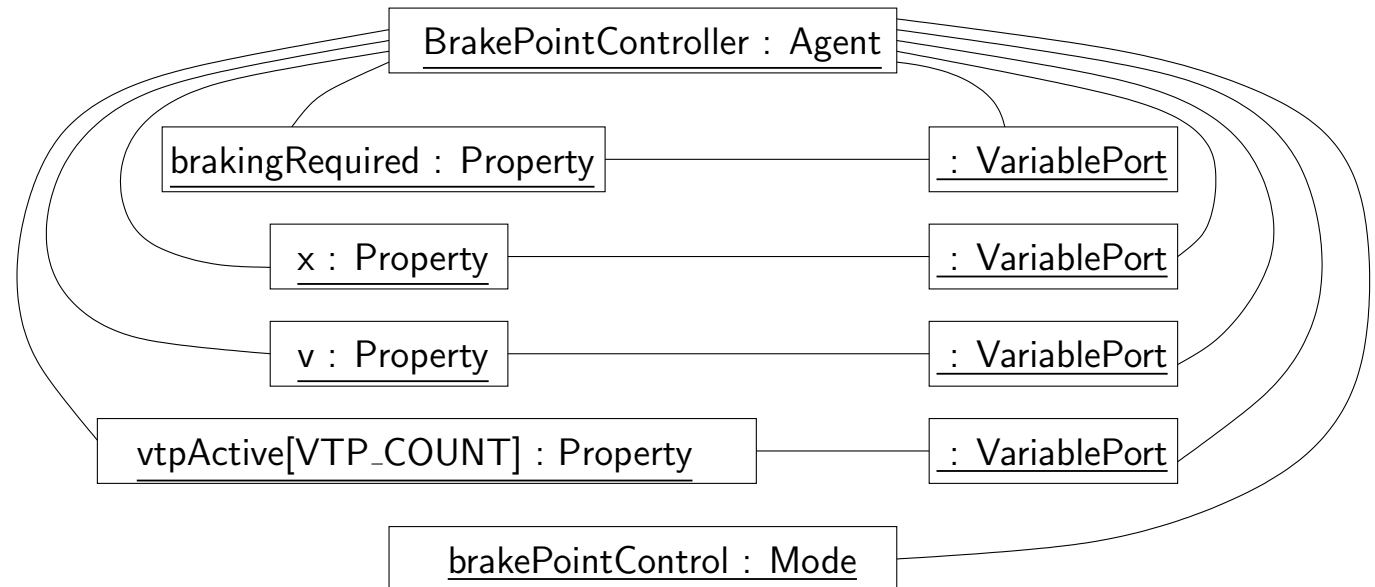
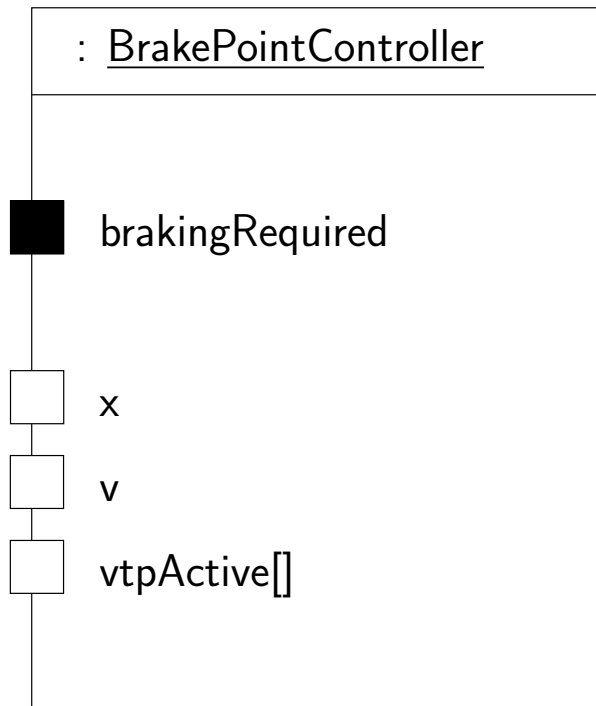
HybridUML Internal Data Structure



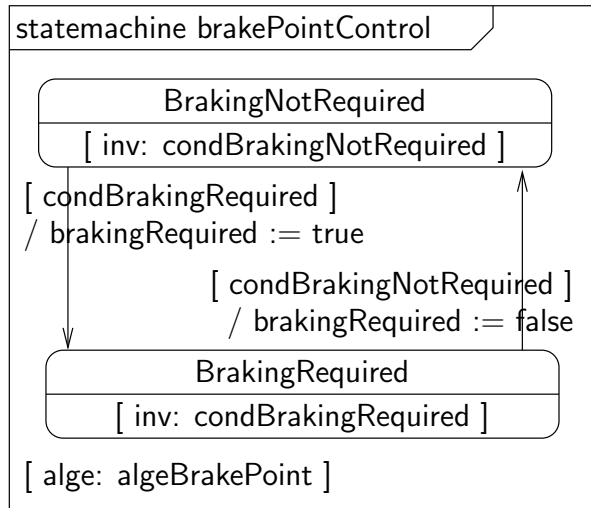
HybridUML Models – Internal Data Structure

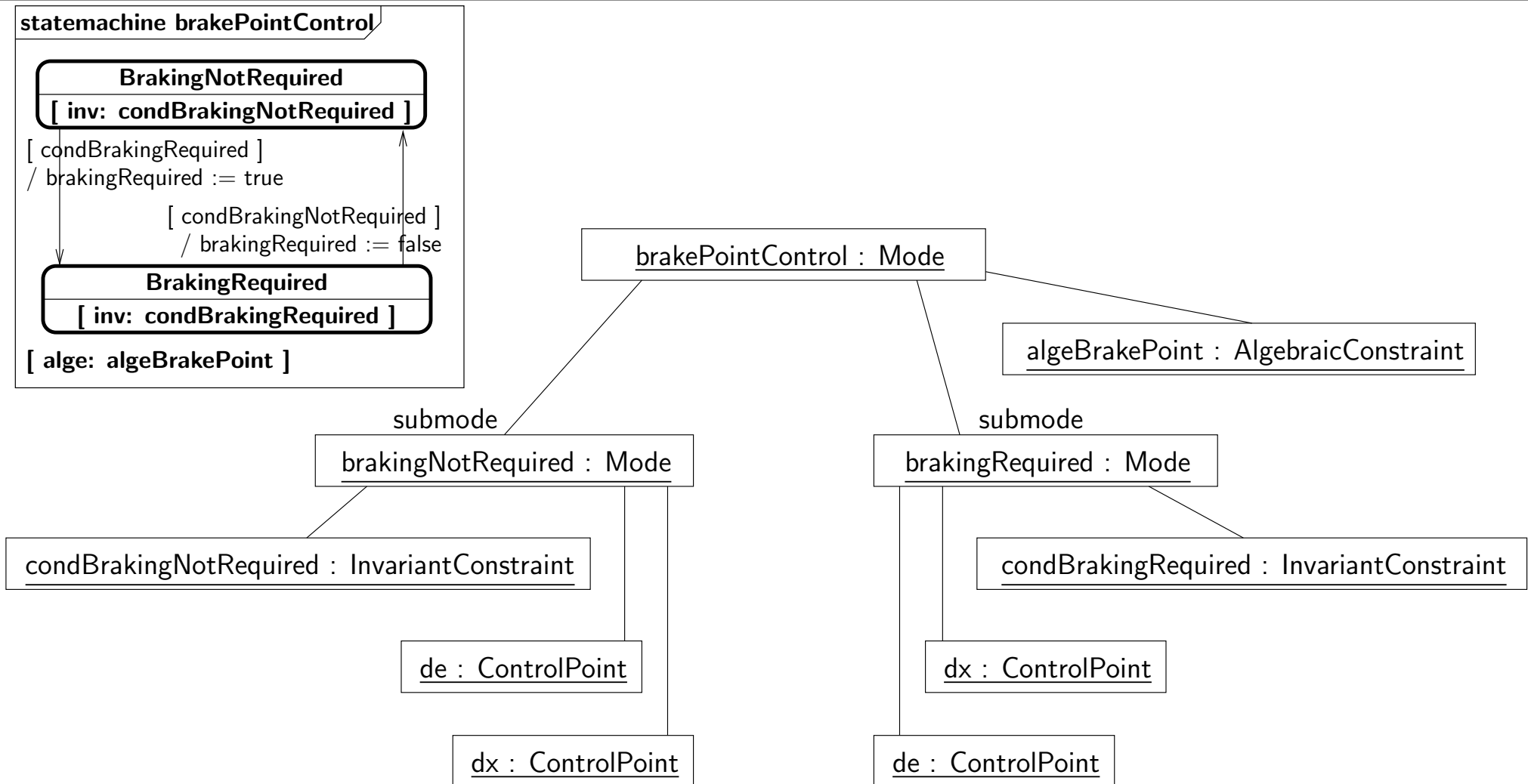






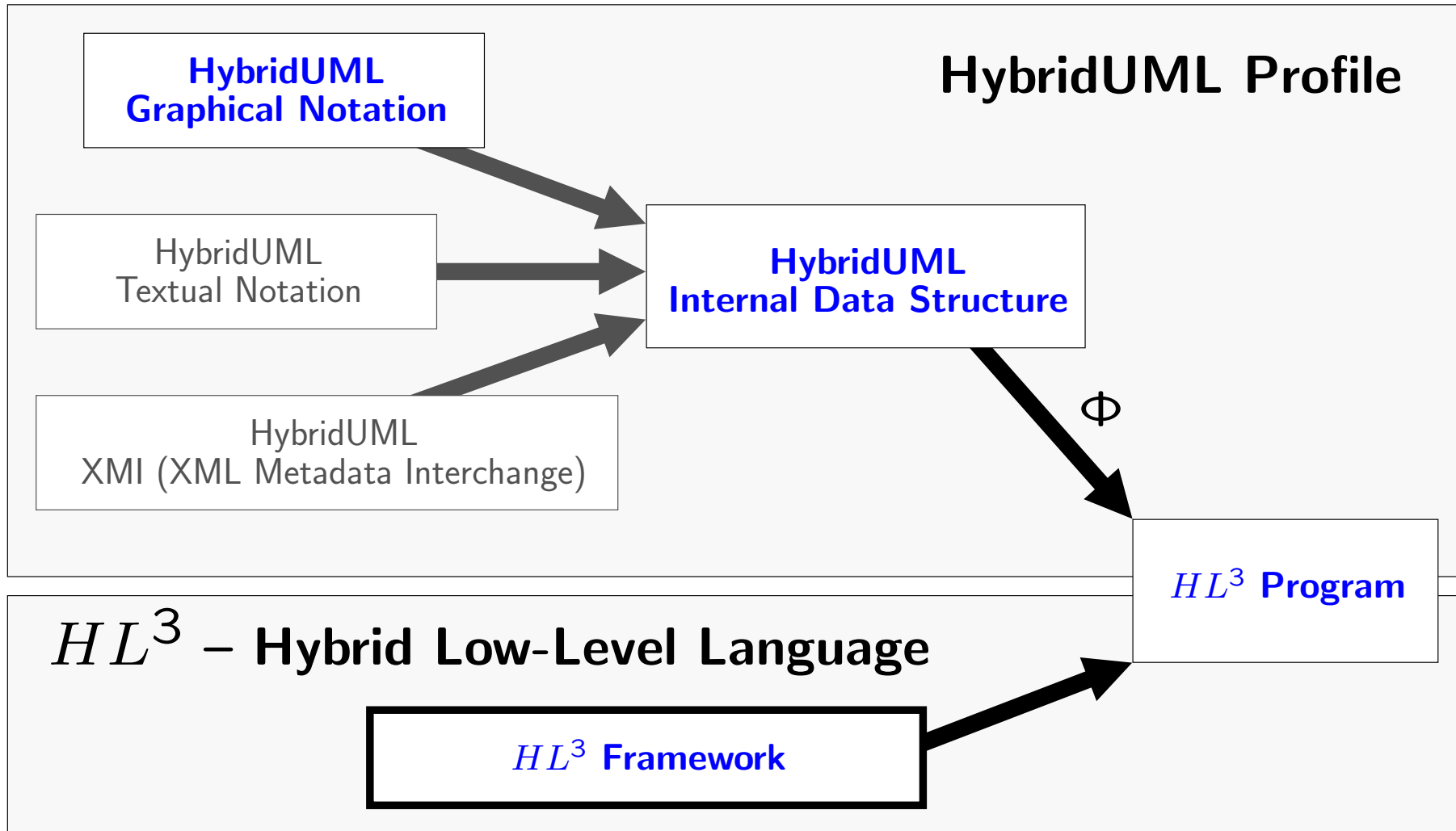
Internal Data Structure Representation of BrakePointController





Internal Data Structure Representation of BrakePointController

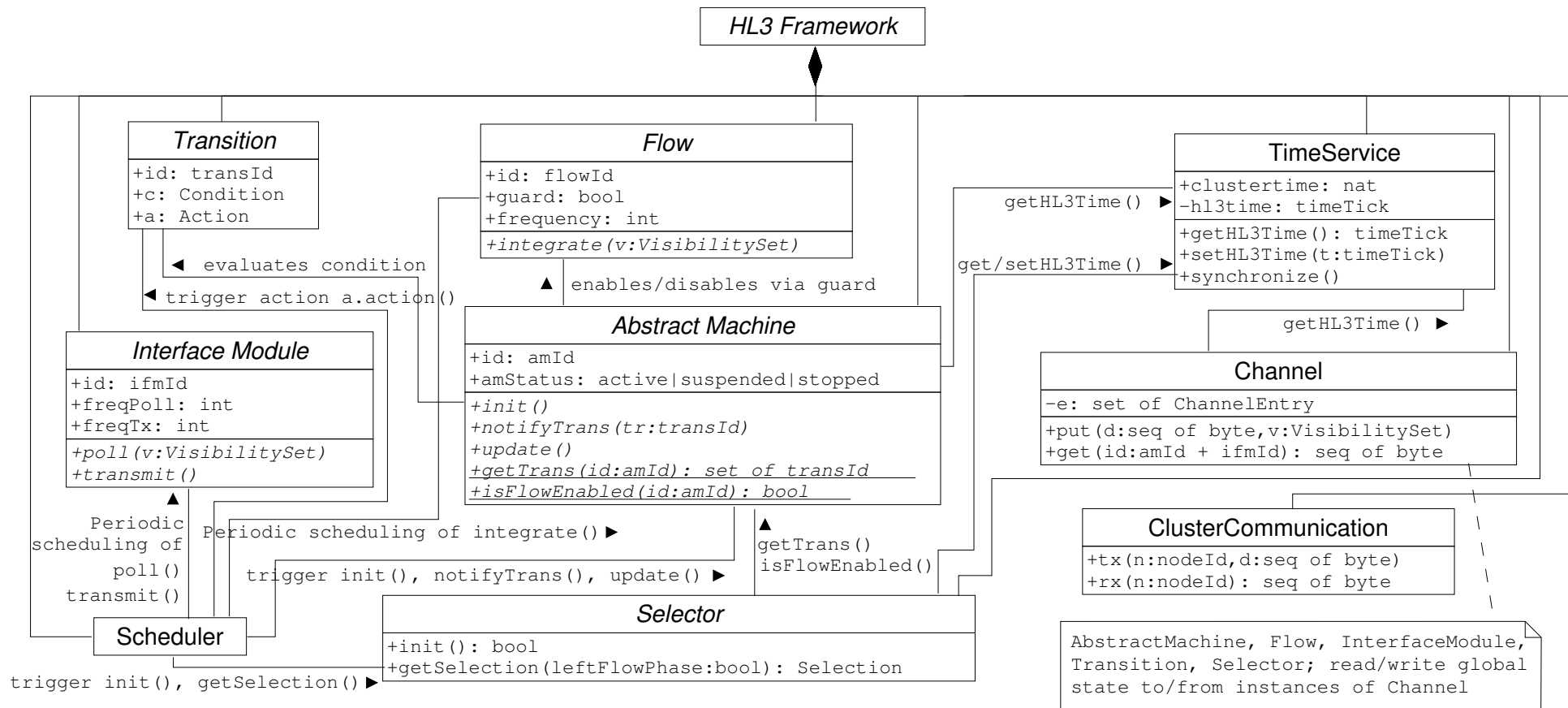
HL³ Framework



HybridUML Models – HL³ Framework

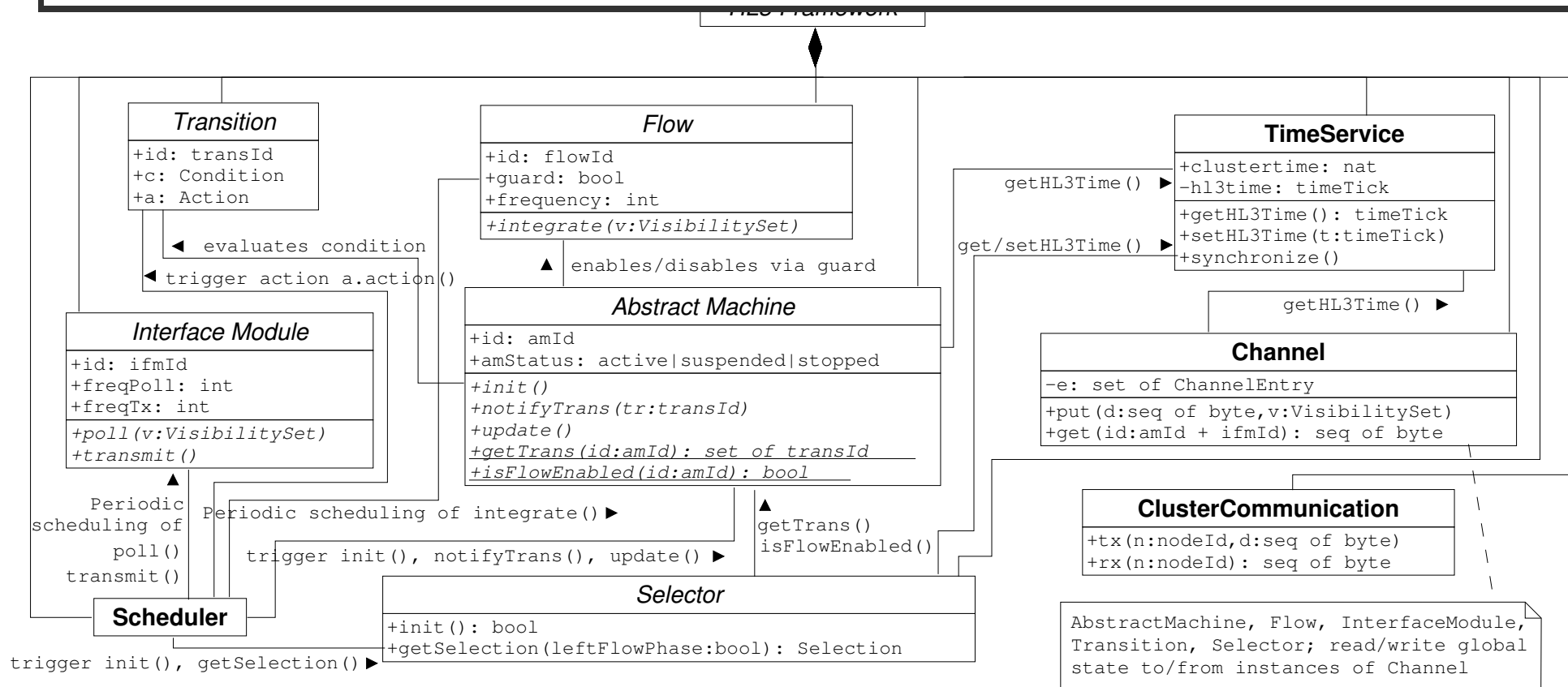
HL³ Framework

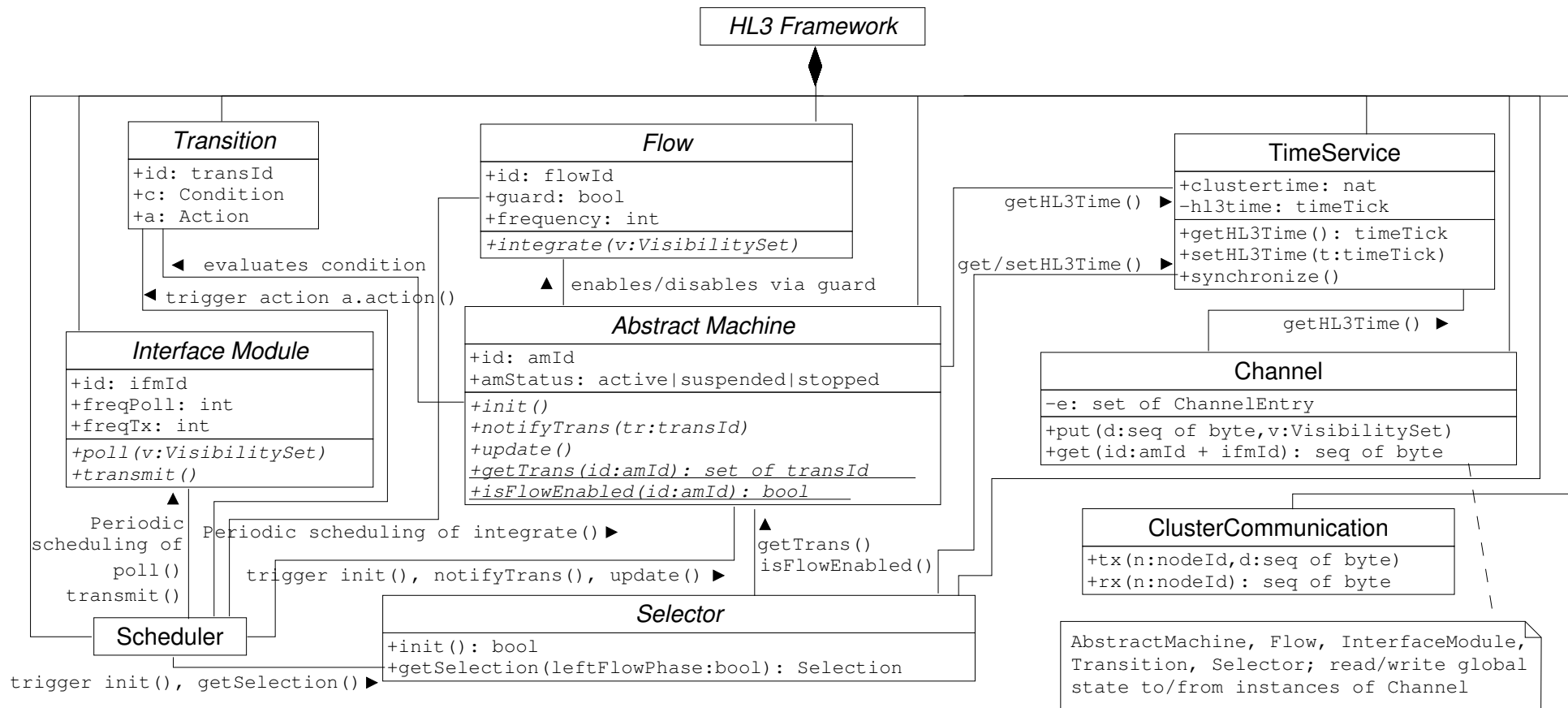
- Generic compilation target for hybrid high-level formalisms
- Development and test of embedded applications
- Transformation of high-level models (e.g. HybridUML specifications)
→ executable code
- Executable code defines formal semantics, based on:
 - Runtime environment
 - Design pattern



Runtime Environment

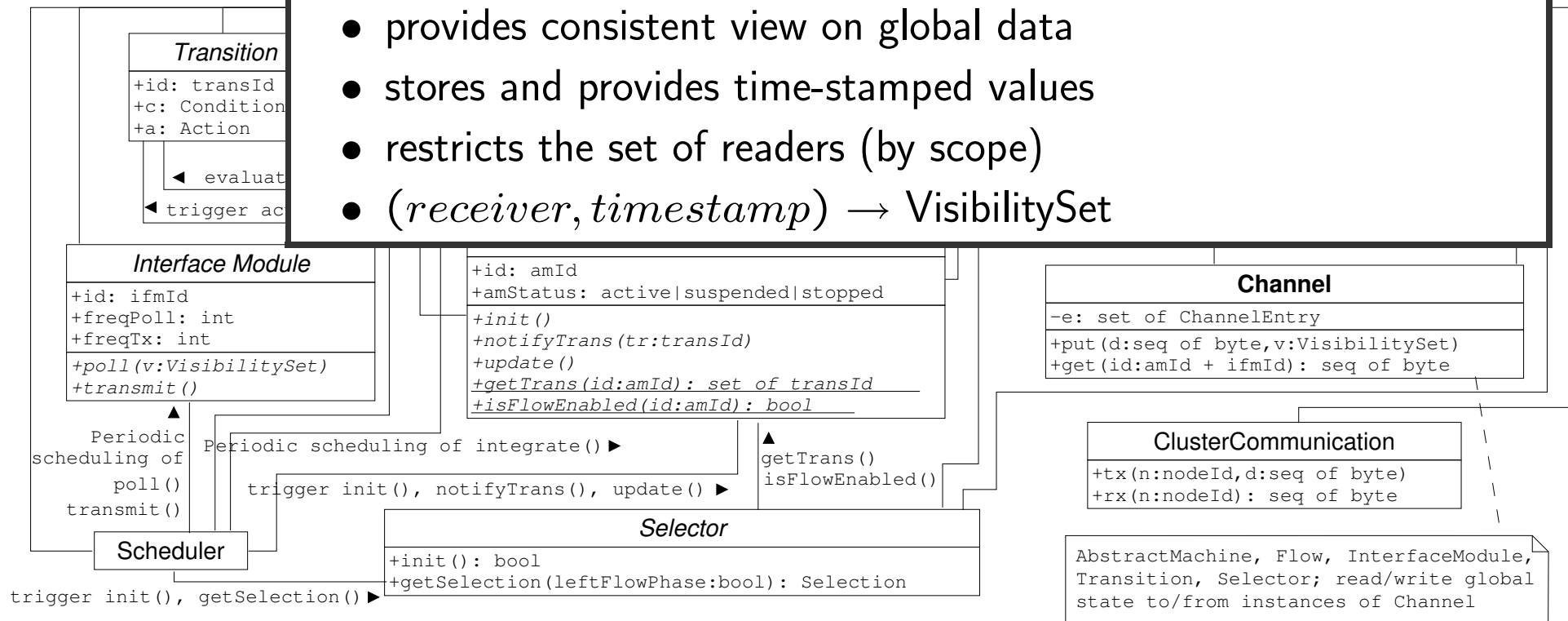
Provides low level constructs to be used by *HL³* programs: (1) Channel (2) Cluster-Communication (3) TimeService (4) Scheduler

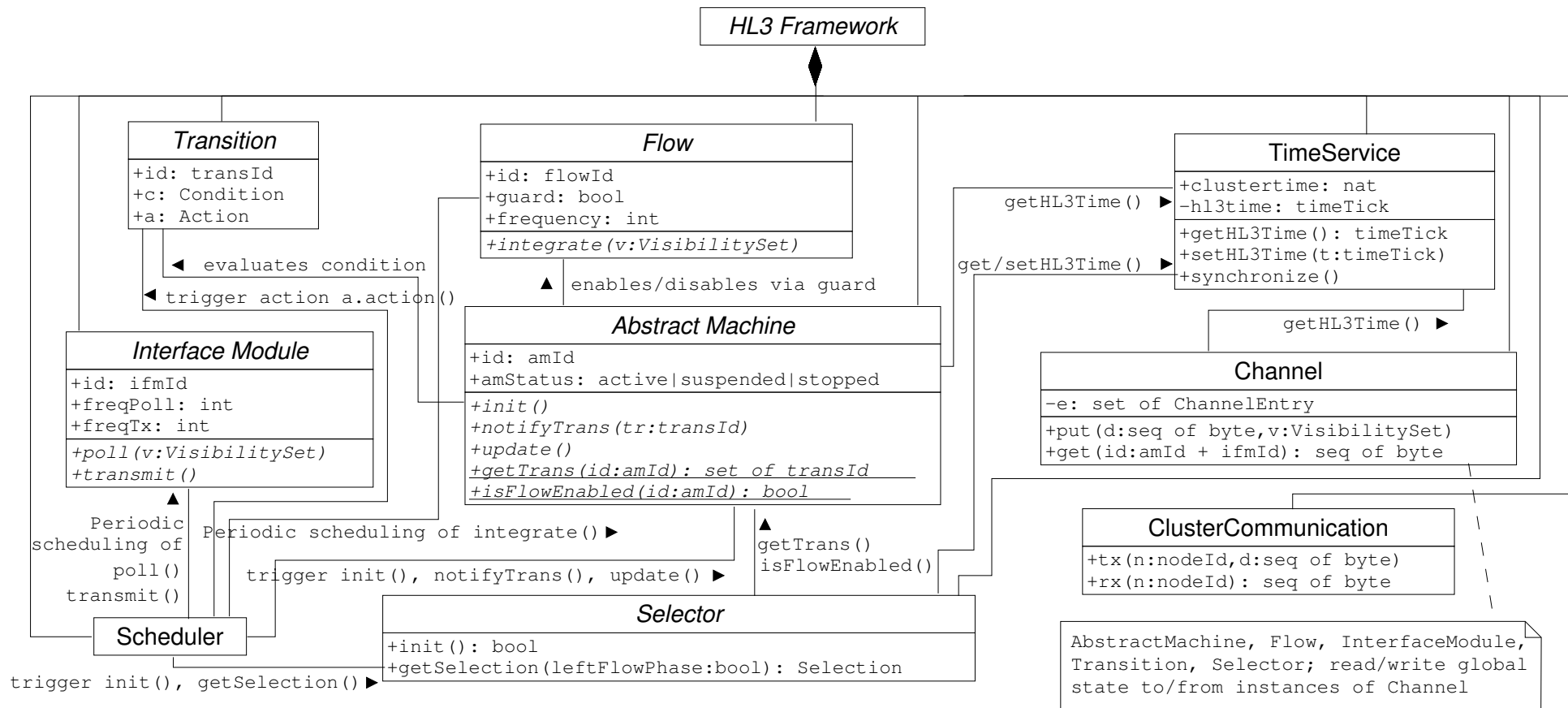


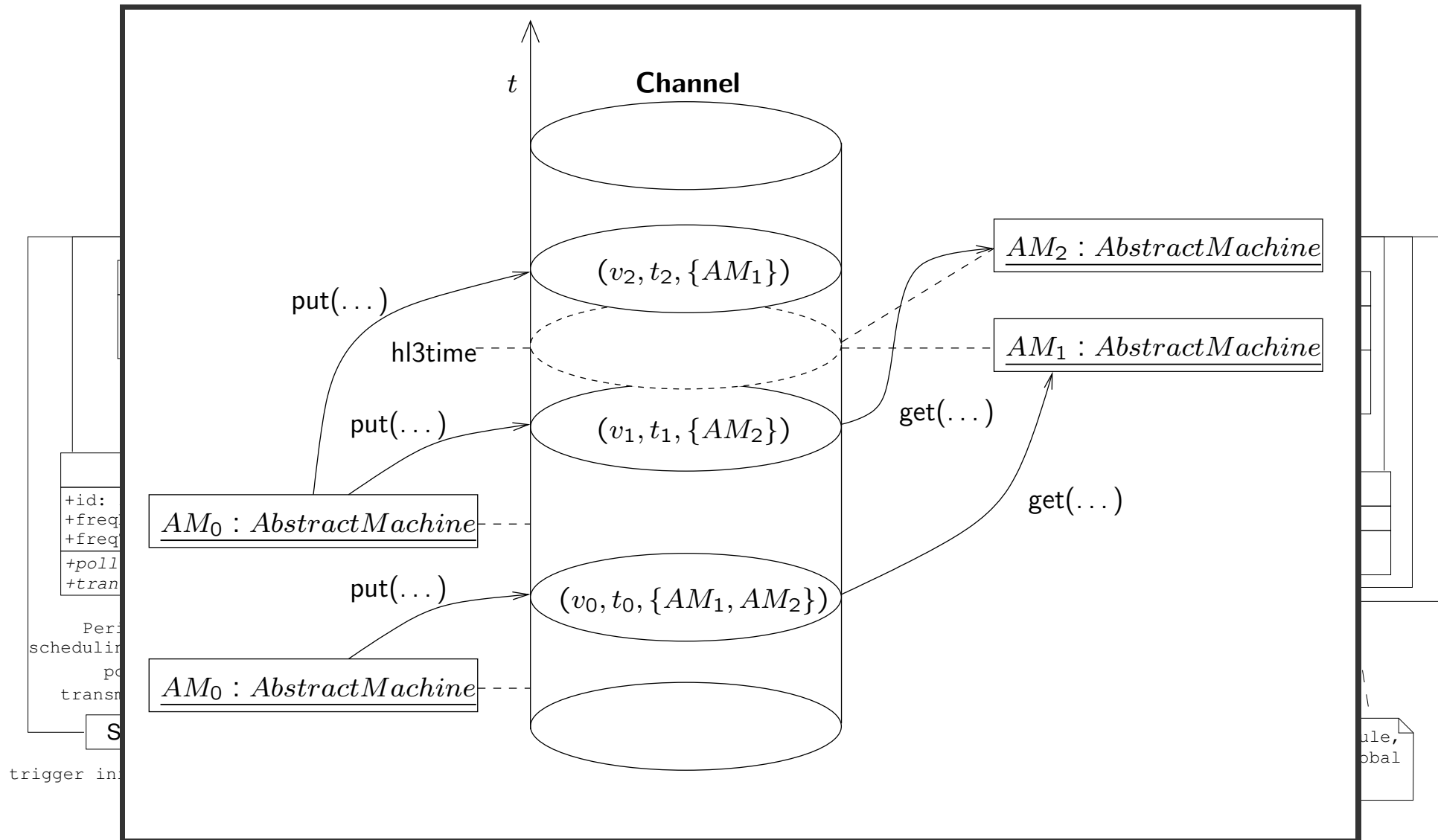


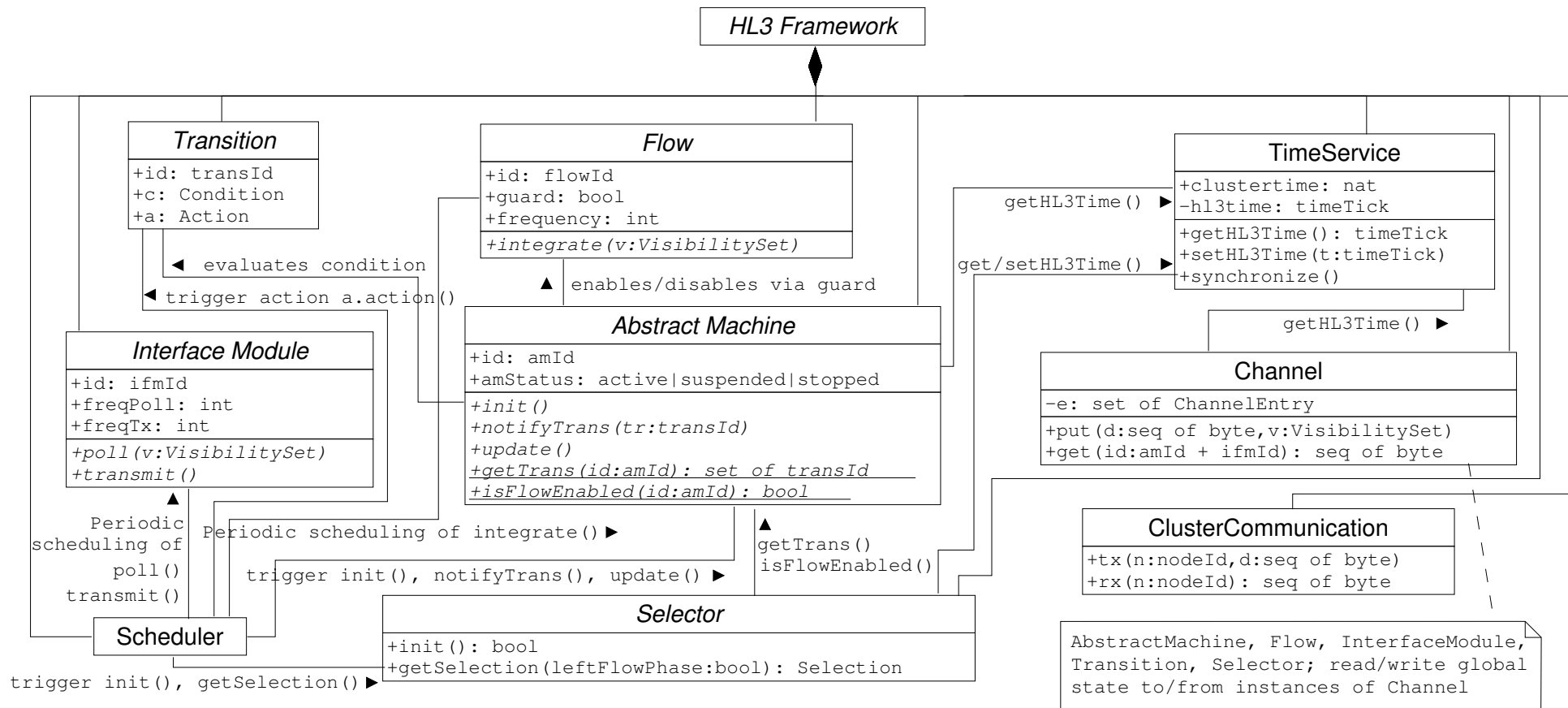
Channel:

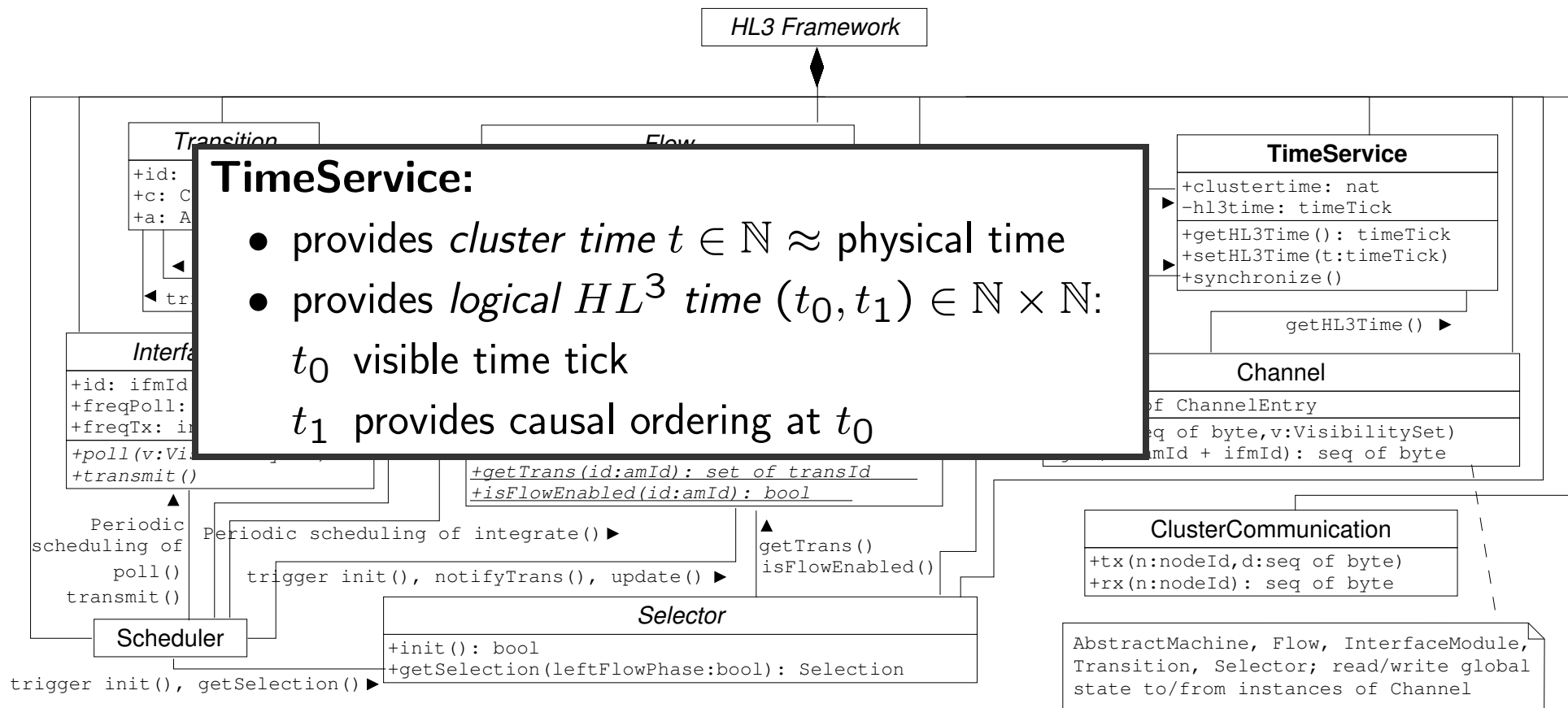
- represents a global variable or signal (of the high-level model)
- provides consistent view on global data
- stores and provides time-stamped values
- restricts the set of readers (by scope)
- $(receiver, timestamp) \rightarrow VisibilitySet$

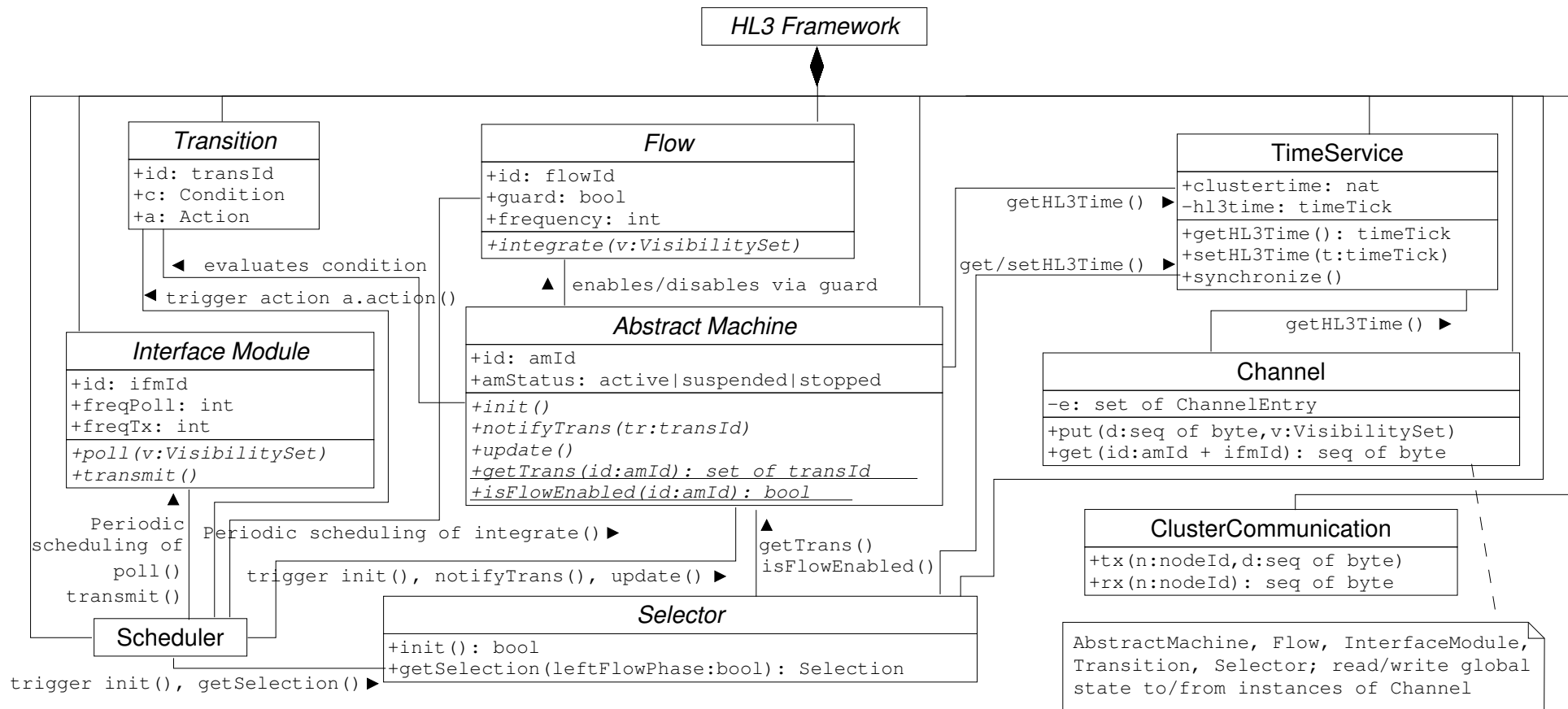


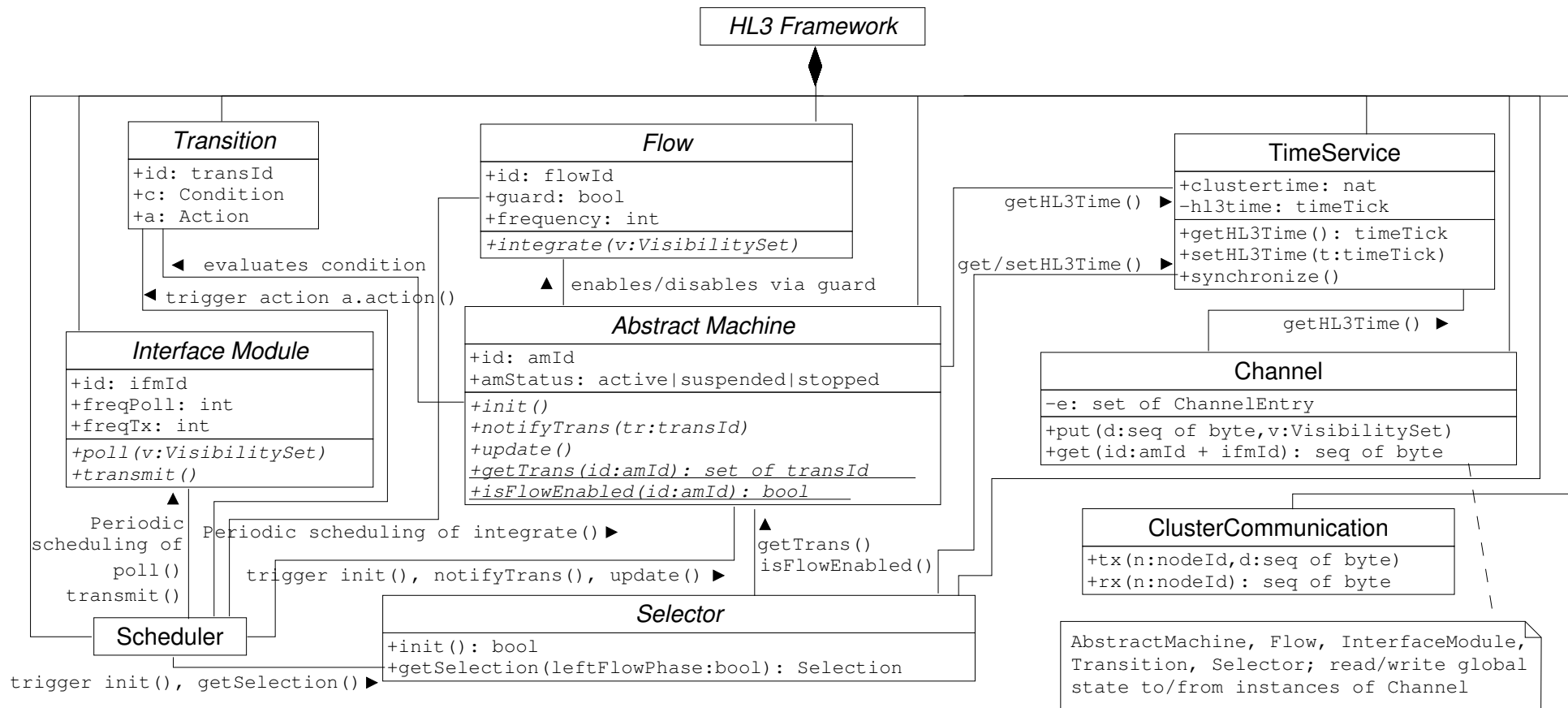






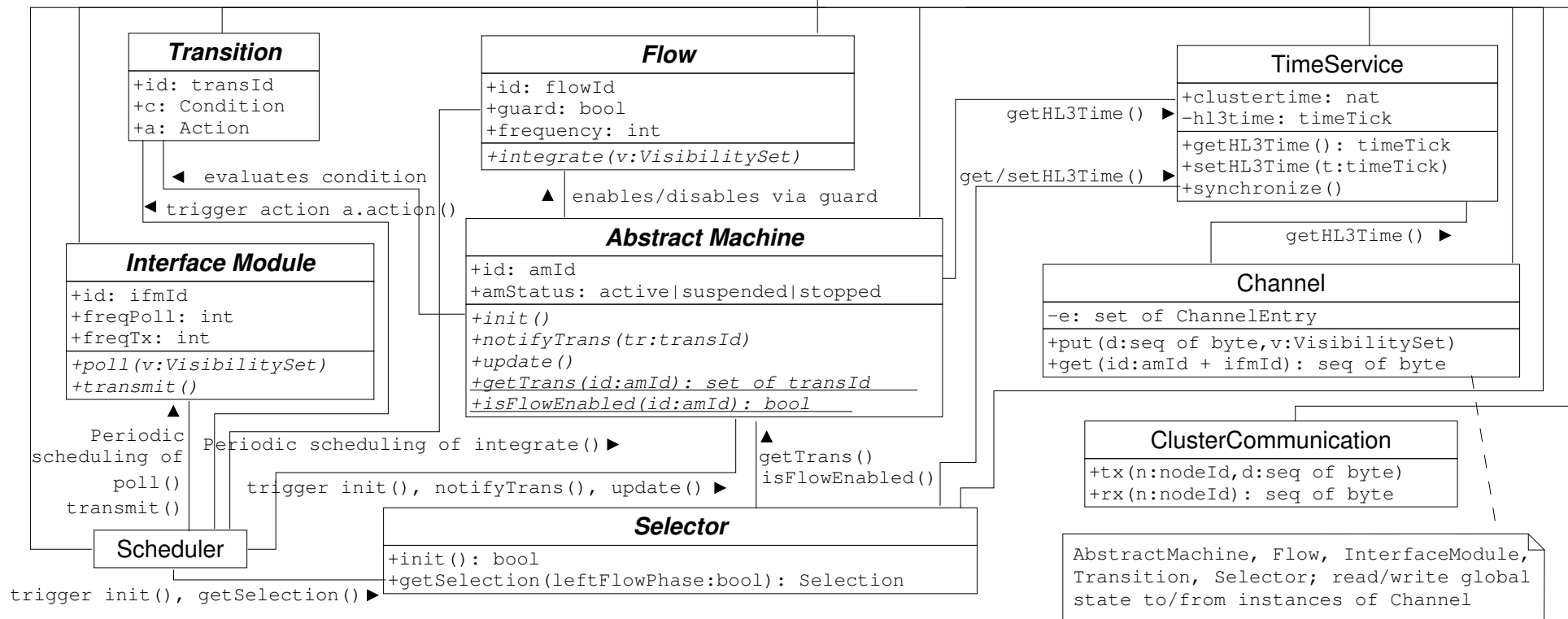


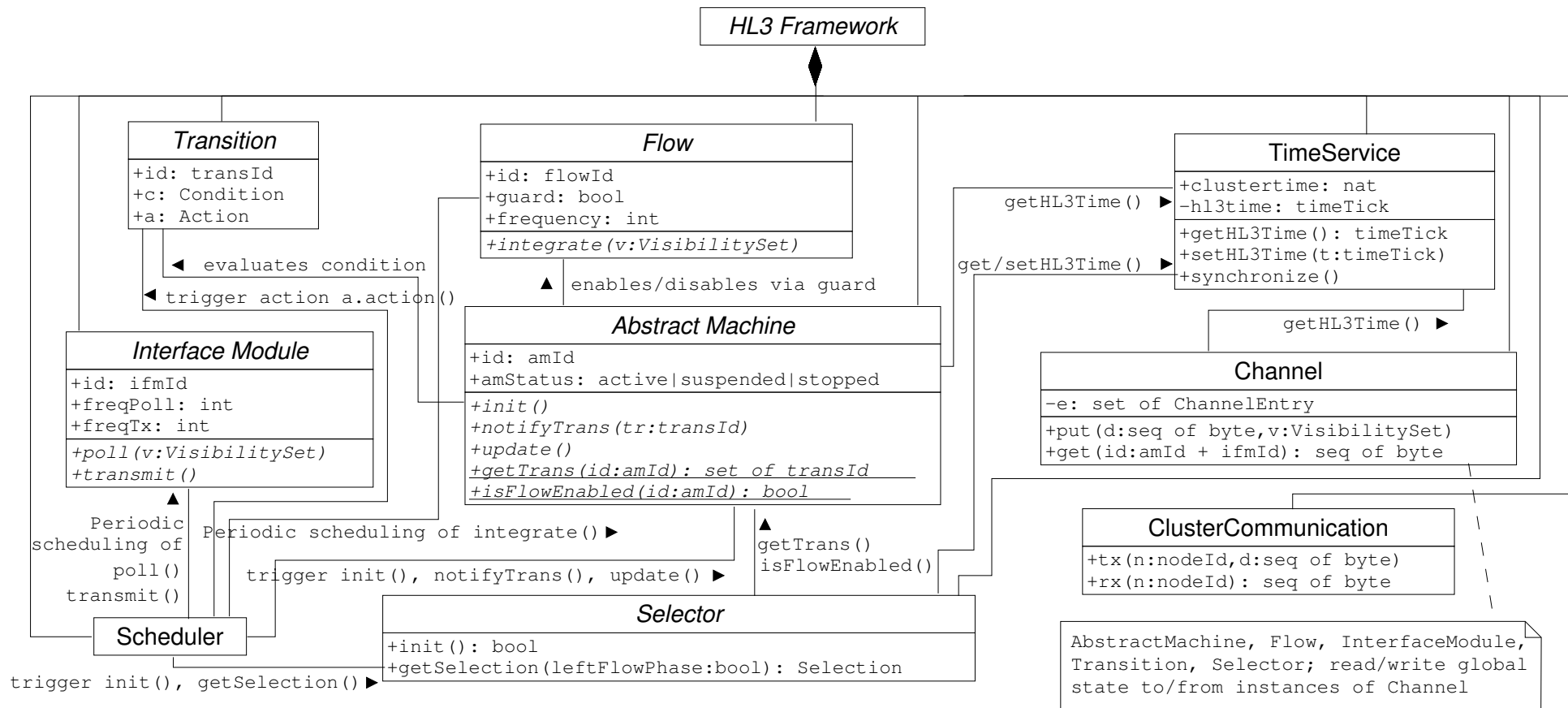




Design Pattern Proposes how to decompose (models of) a high-level formalism:

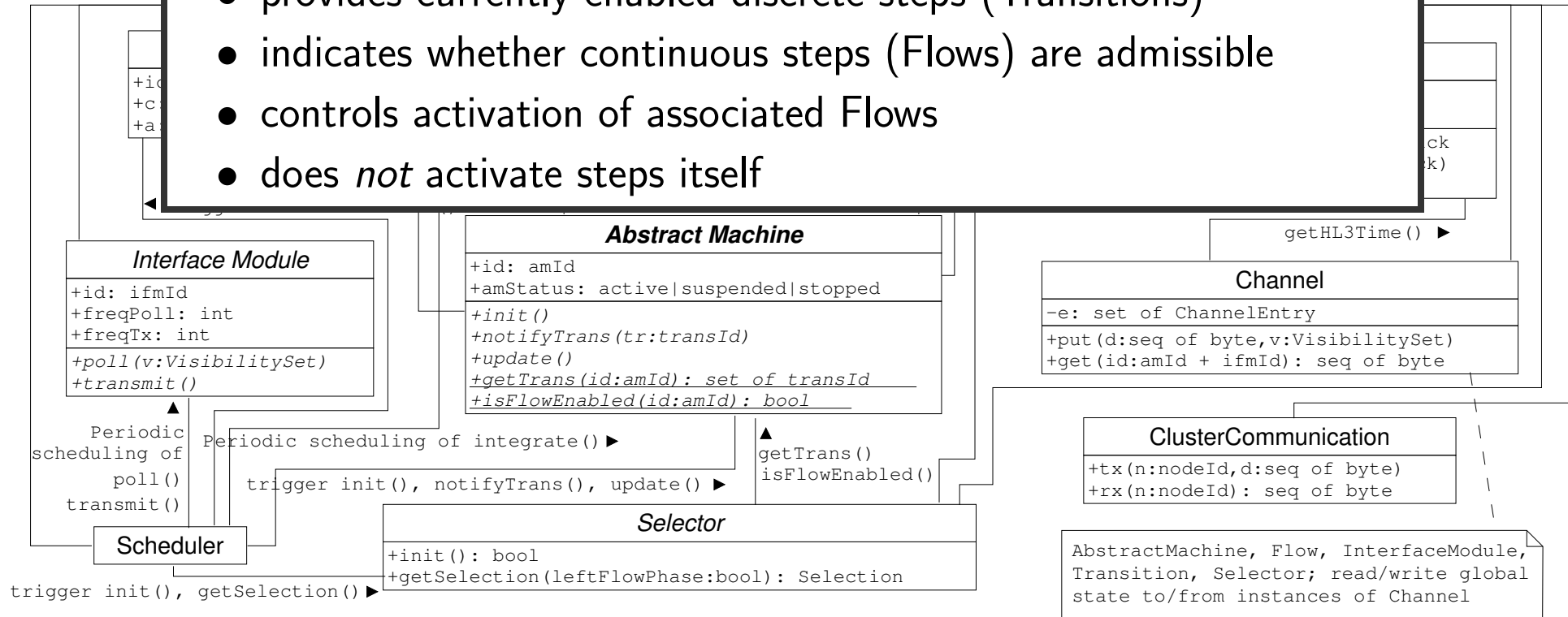
- (1) AbstractMachine
- (2) Transition
- (3) Flow
- (4) InterfaceModule (per high-level formalism + per model)
- (5) Selector (per high-level formalism)

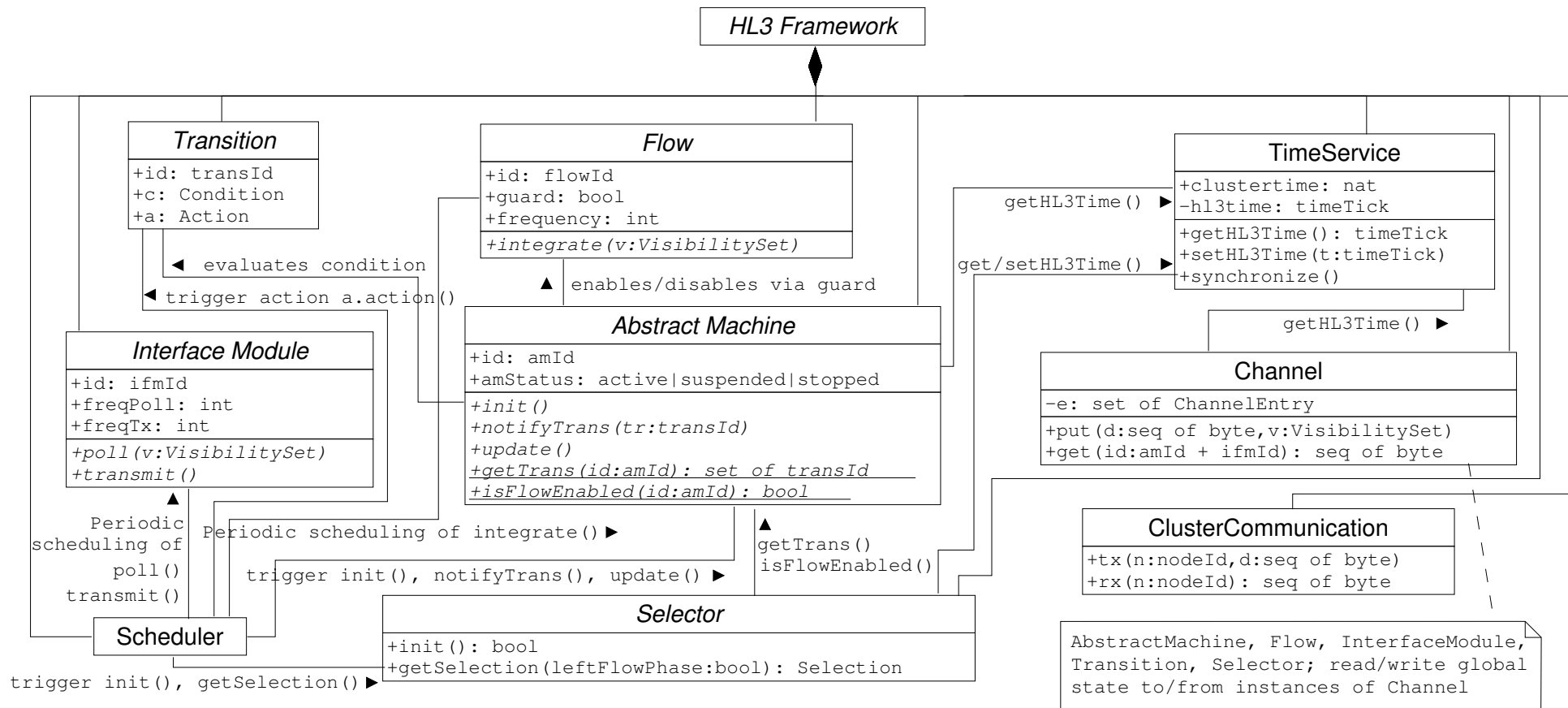




AbstractMachine:

- represents local behaviour of sequential components
- encapsulates local control structure
- provides currently enabled discrete steps (Transitions)
- indicates whether continuous steps (Flows) are admissible
- controls activation of associated Flows
- does *not* activate steps itself

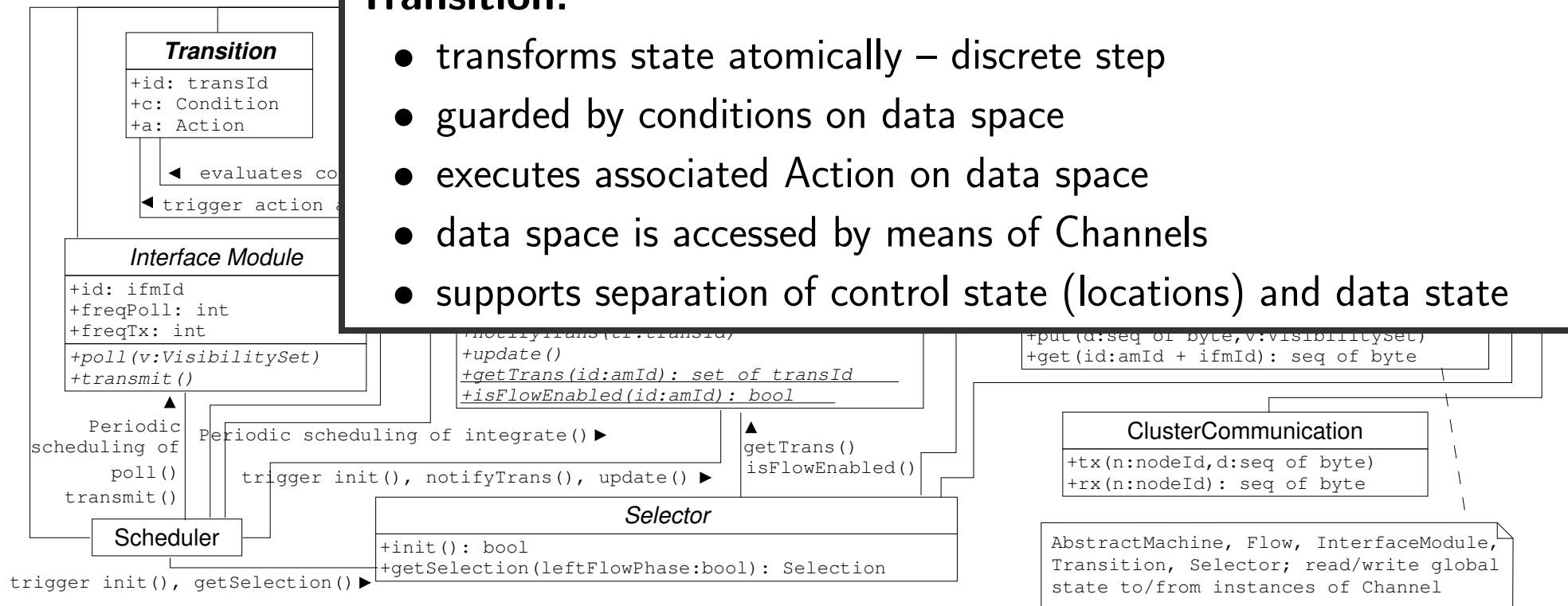


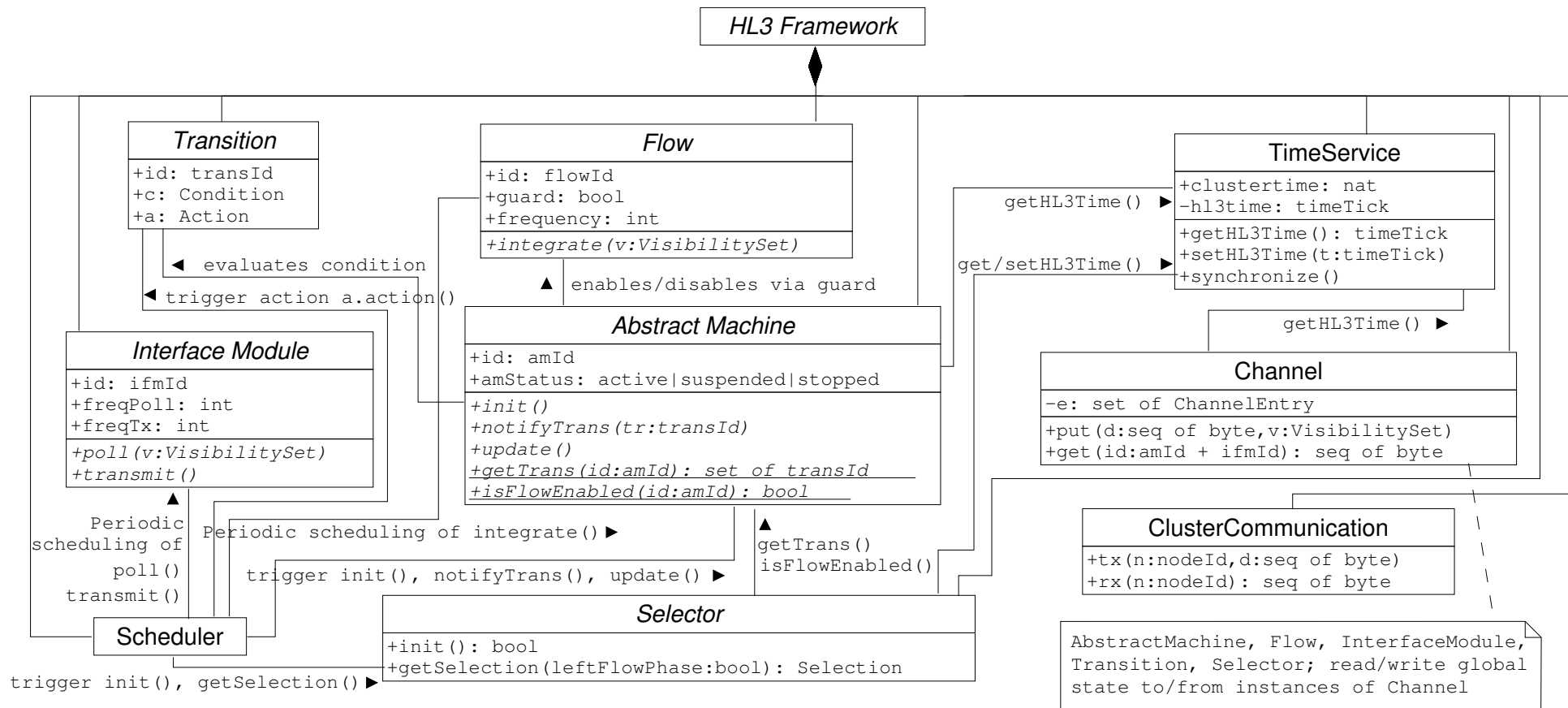


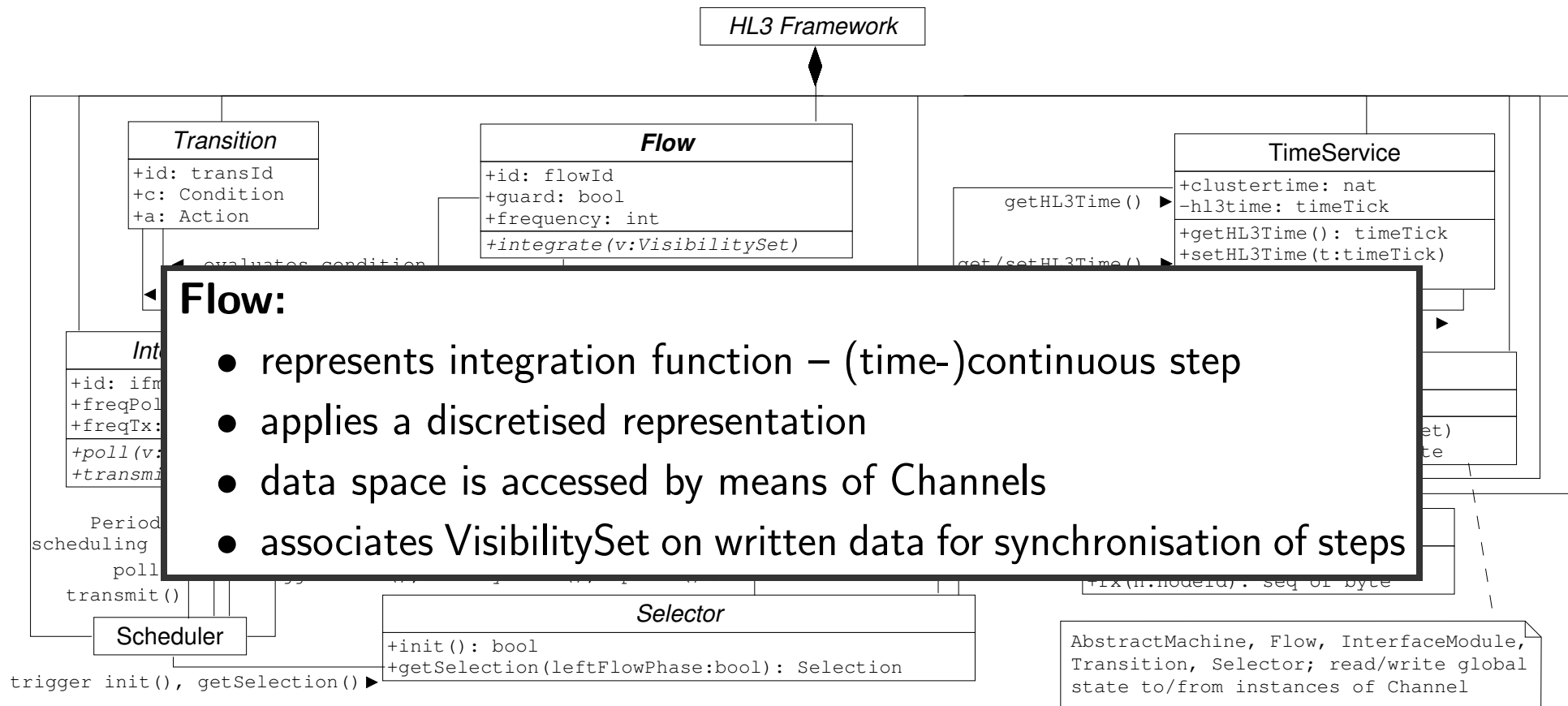
HL3 Framework

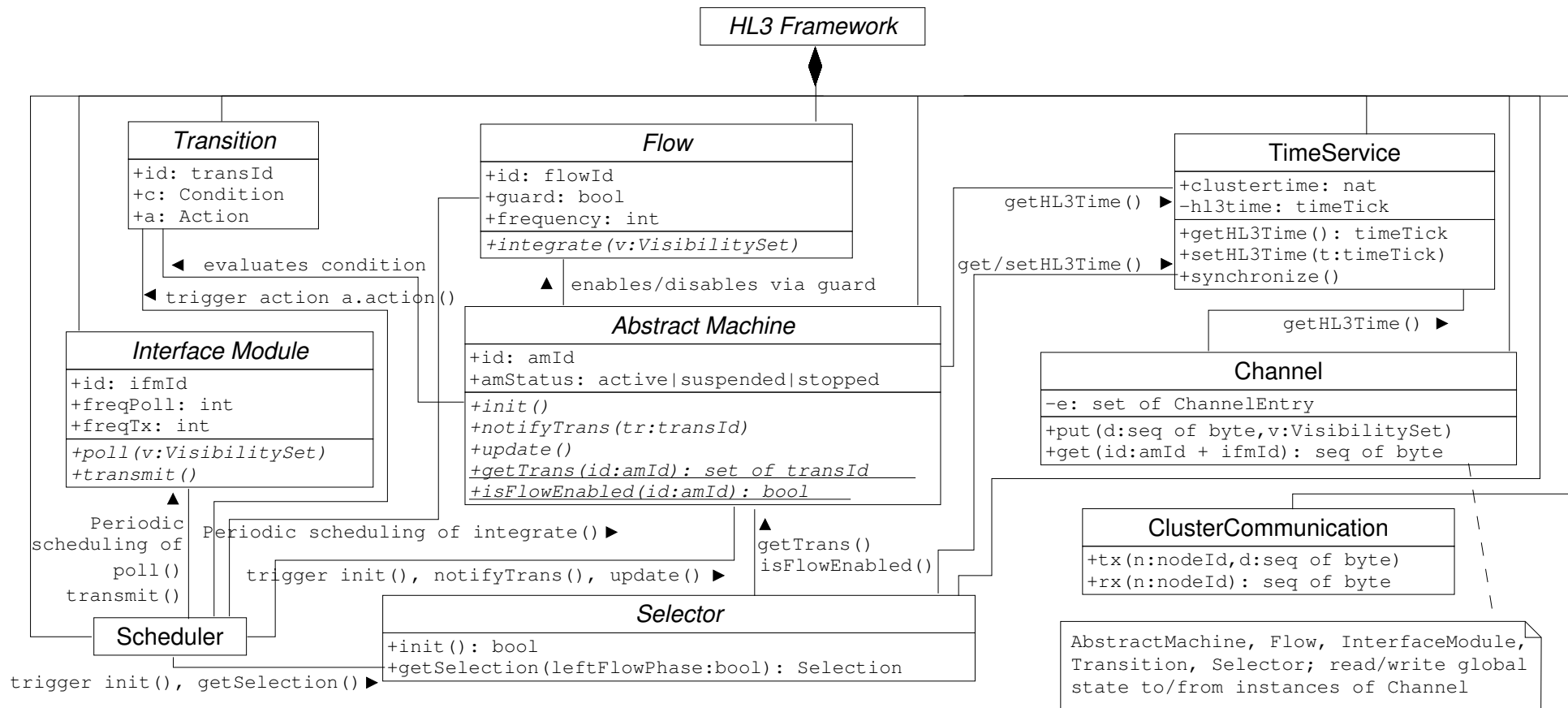
Transition:

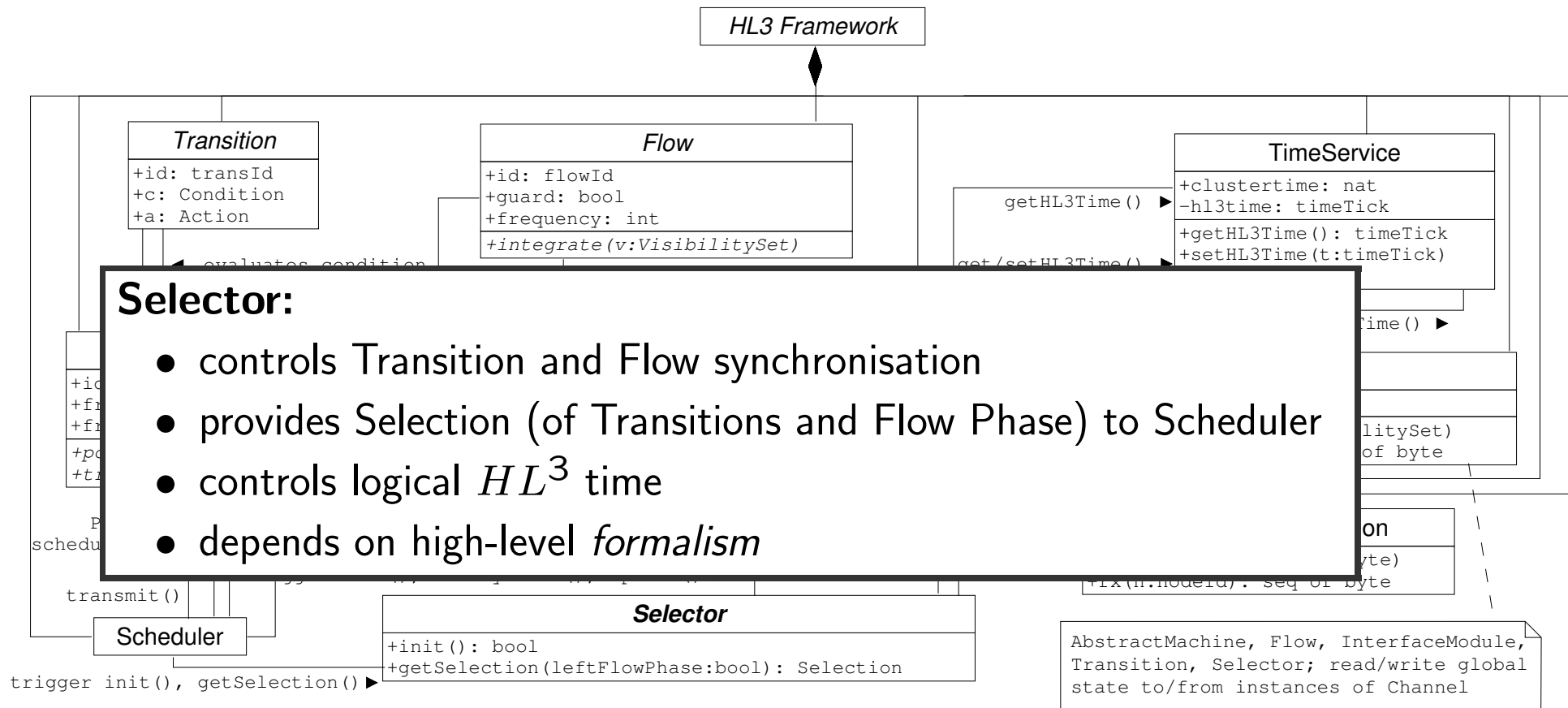
- transforms state atomically – discrete step
- guarded by conditions on data space
- executes associated Action on data space
- data space is accessed by means of Channels
- supports separation of control state (locations) and data state



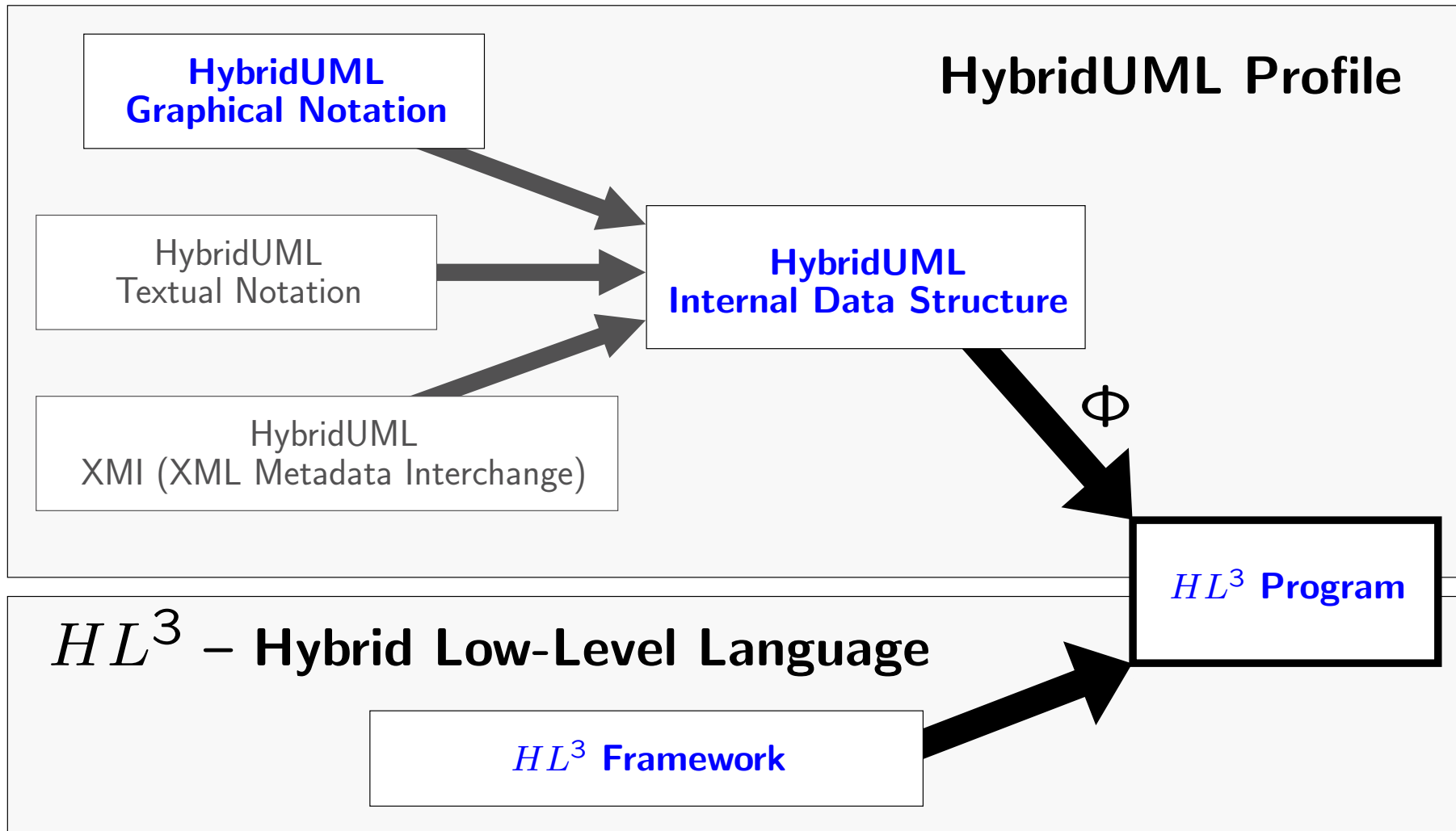








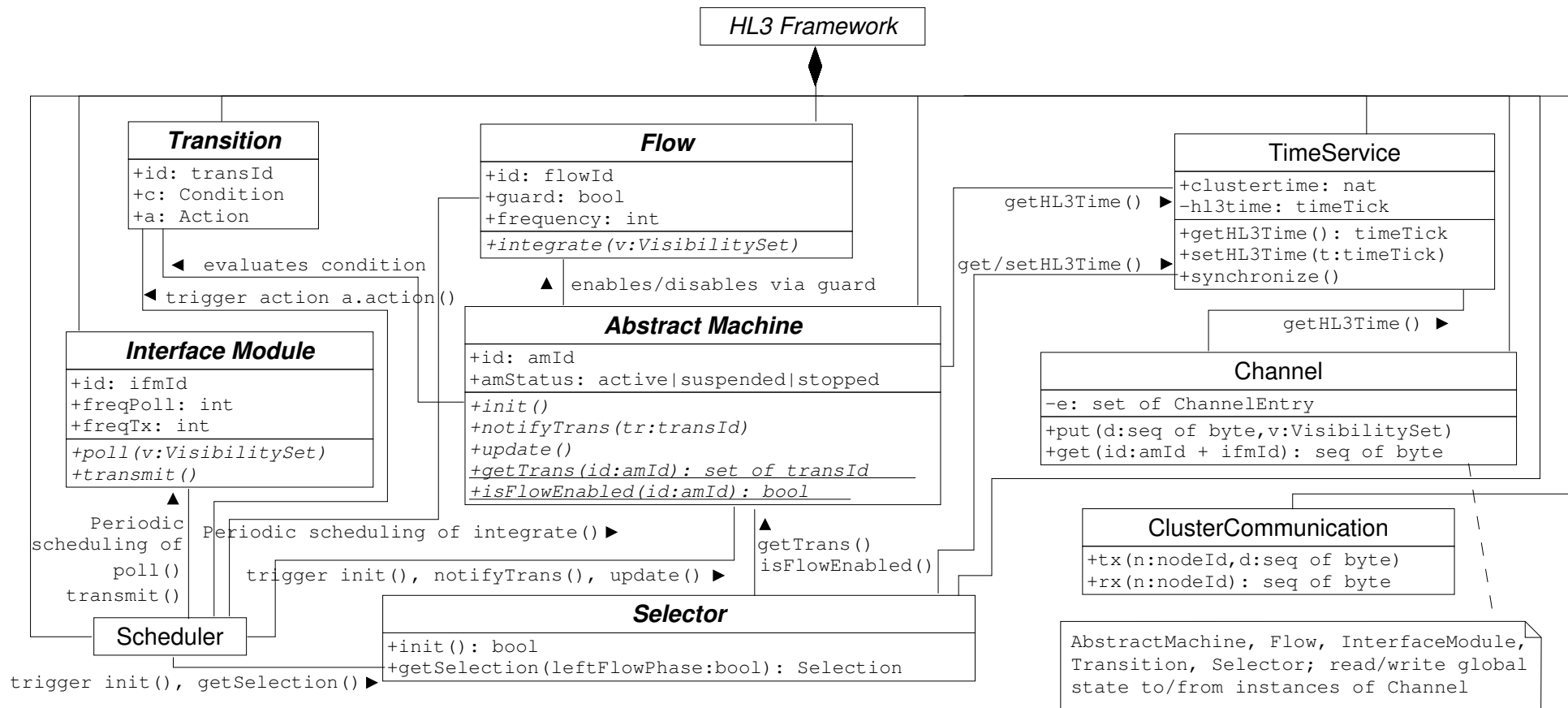
$\Phi \rightarrow HL^3$ Program



HybridUML Models – HL^3 Program

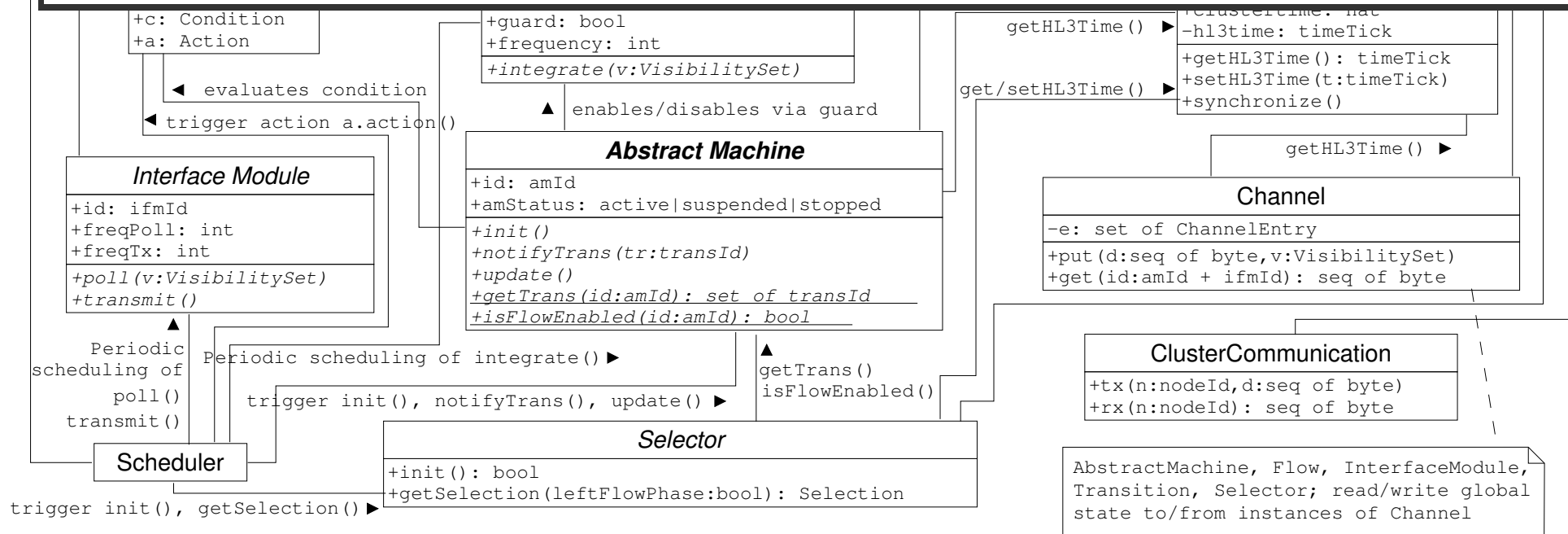
Φ

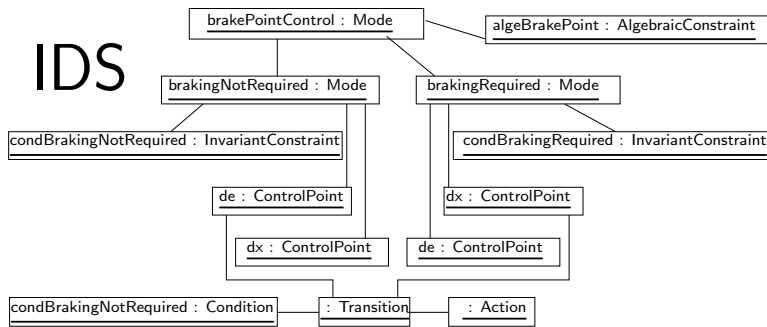
Transforming Internal Data Structure into a HL^3 program by applying the HL^3 Design Pattern.



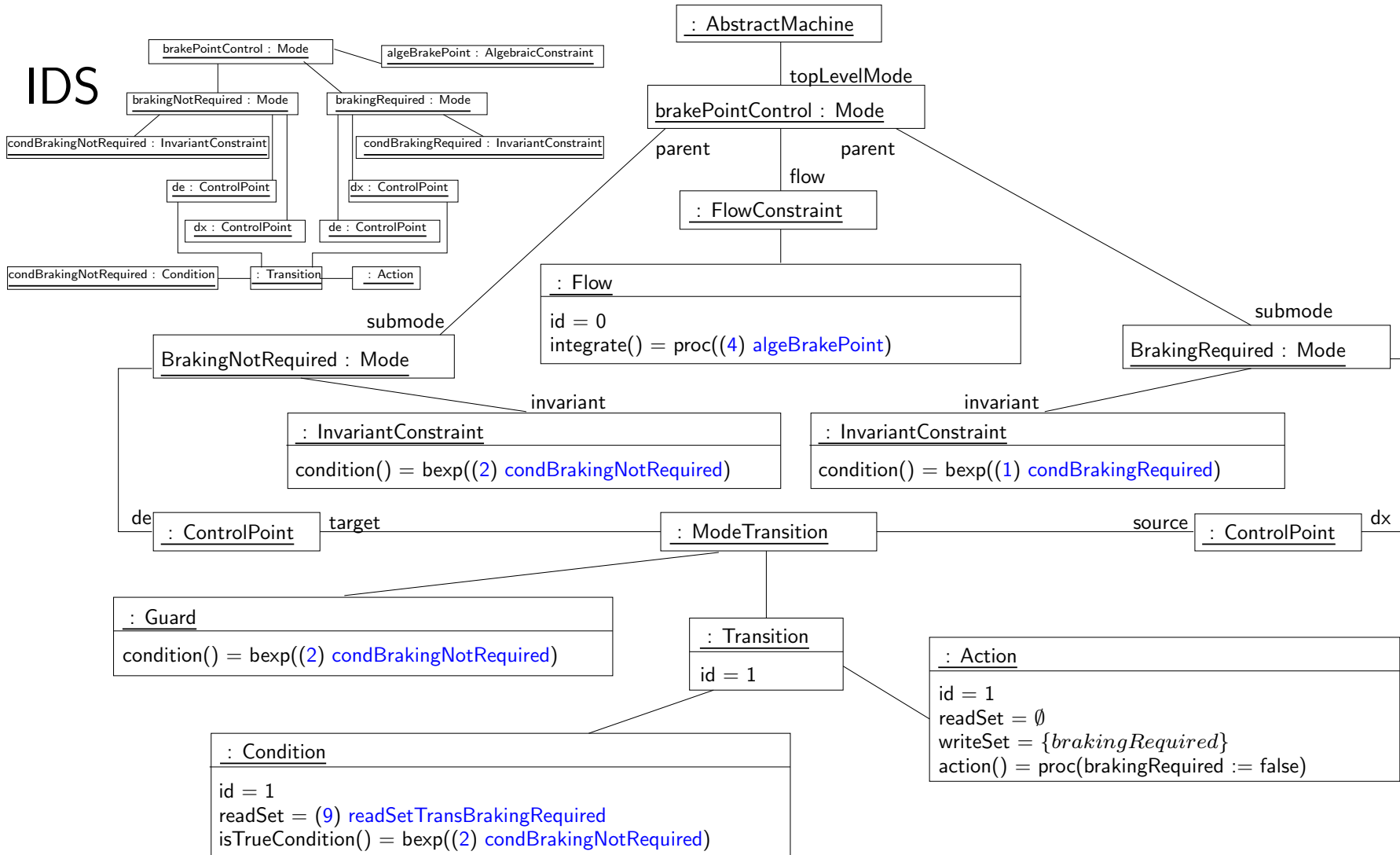
Step 1 – Generate $HL^3::AbstractMachine$

- AbstractMachine class: once
- notifyTrans(...), update(...),: once
- data structure for HybridUML Modes' local control structure: once
- ⇒ AbstractMachine instances for HybridUML basic agents: for each HybridUML model

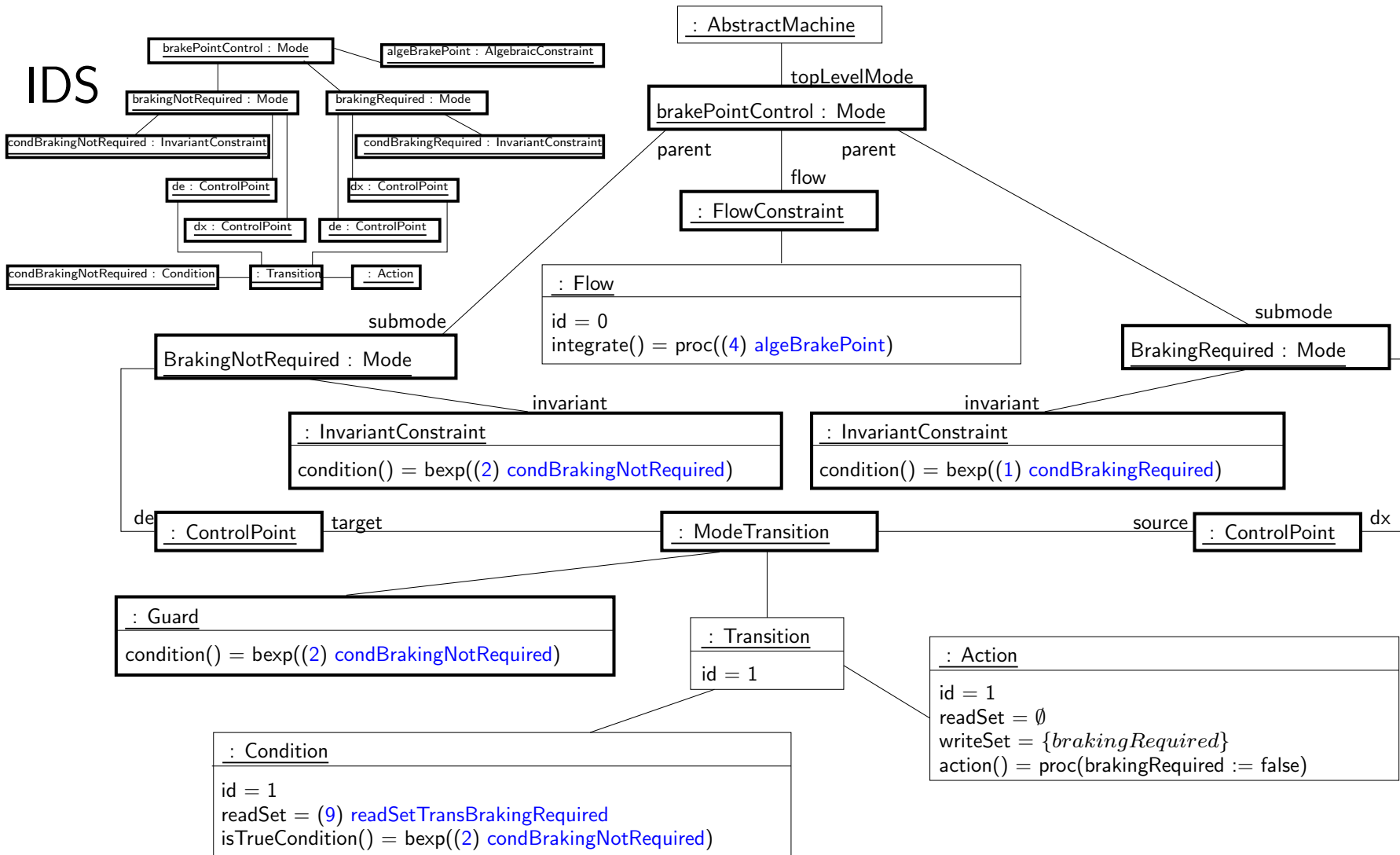




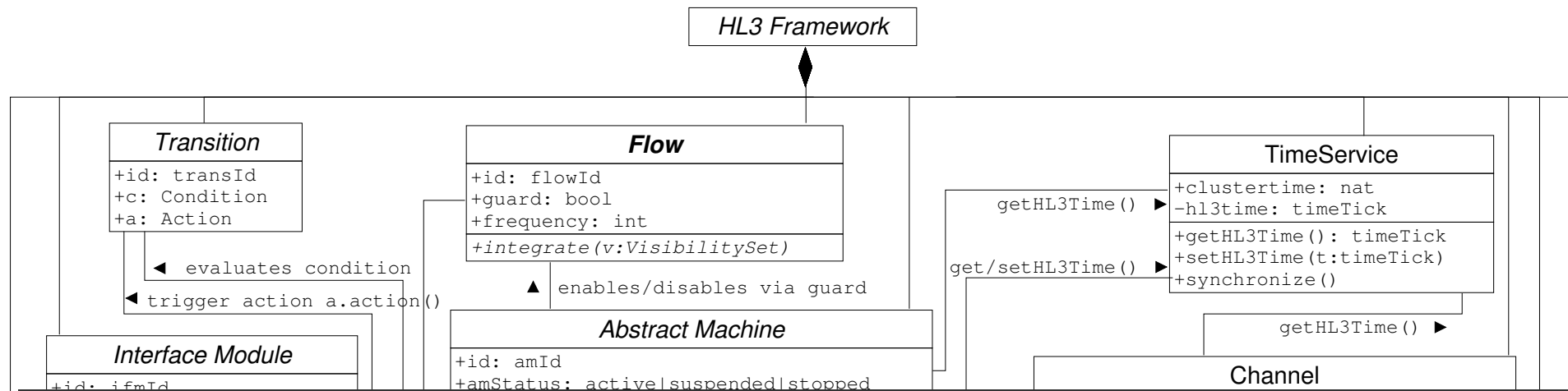
AbstractMachine example: BrakePointController



AbstractMachine example: BrakePointController



AbstractMachine example: BrakePointController



Step 2 – Generate $HL^3::Flow$

⇒ Flow class: once

⇒ `integrate(...)`: once

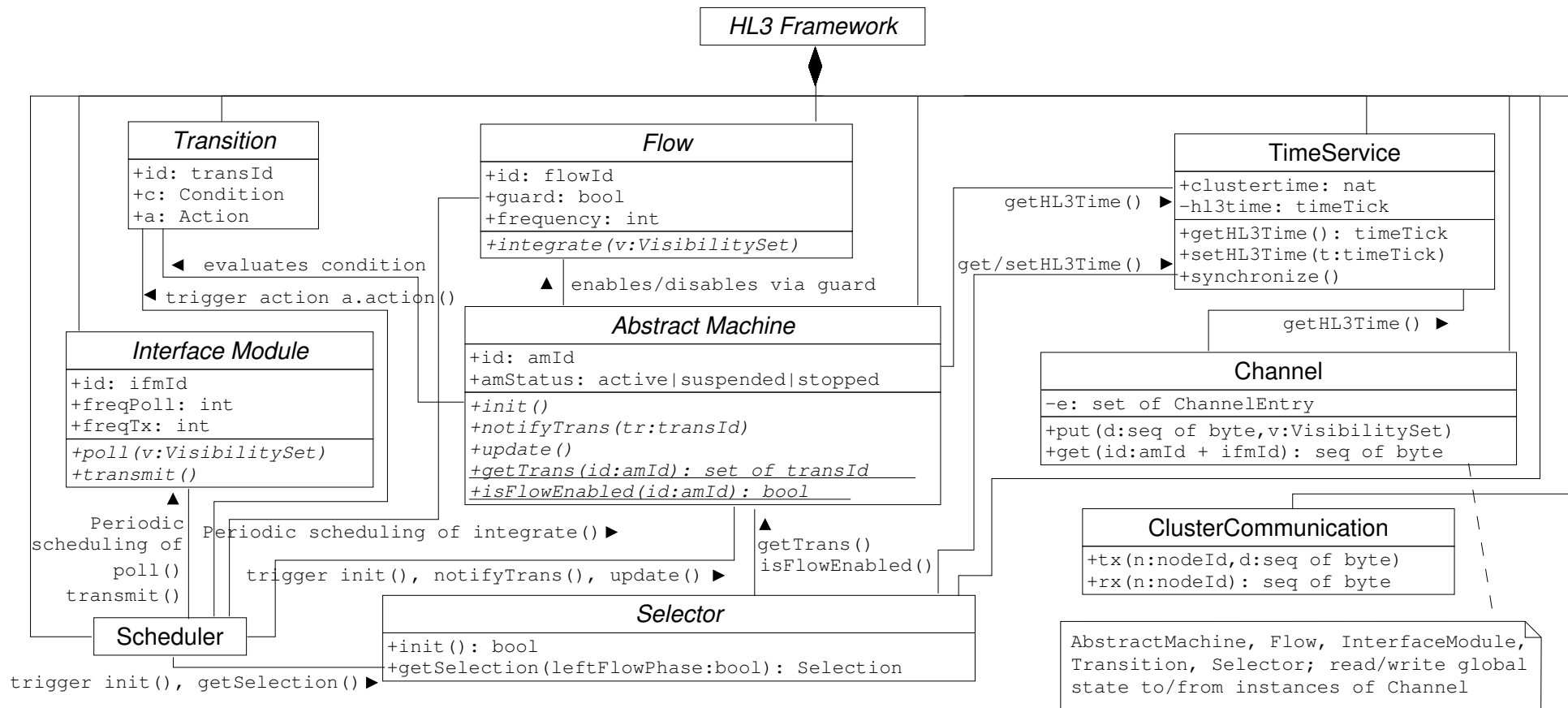
→ Flow instances for HybridUML algebraic and flow constraints: for each HybridUML model

⇒ integration operations for each instance: for each HybridUML model

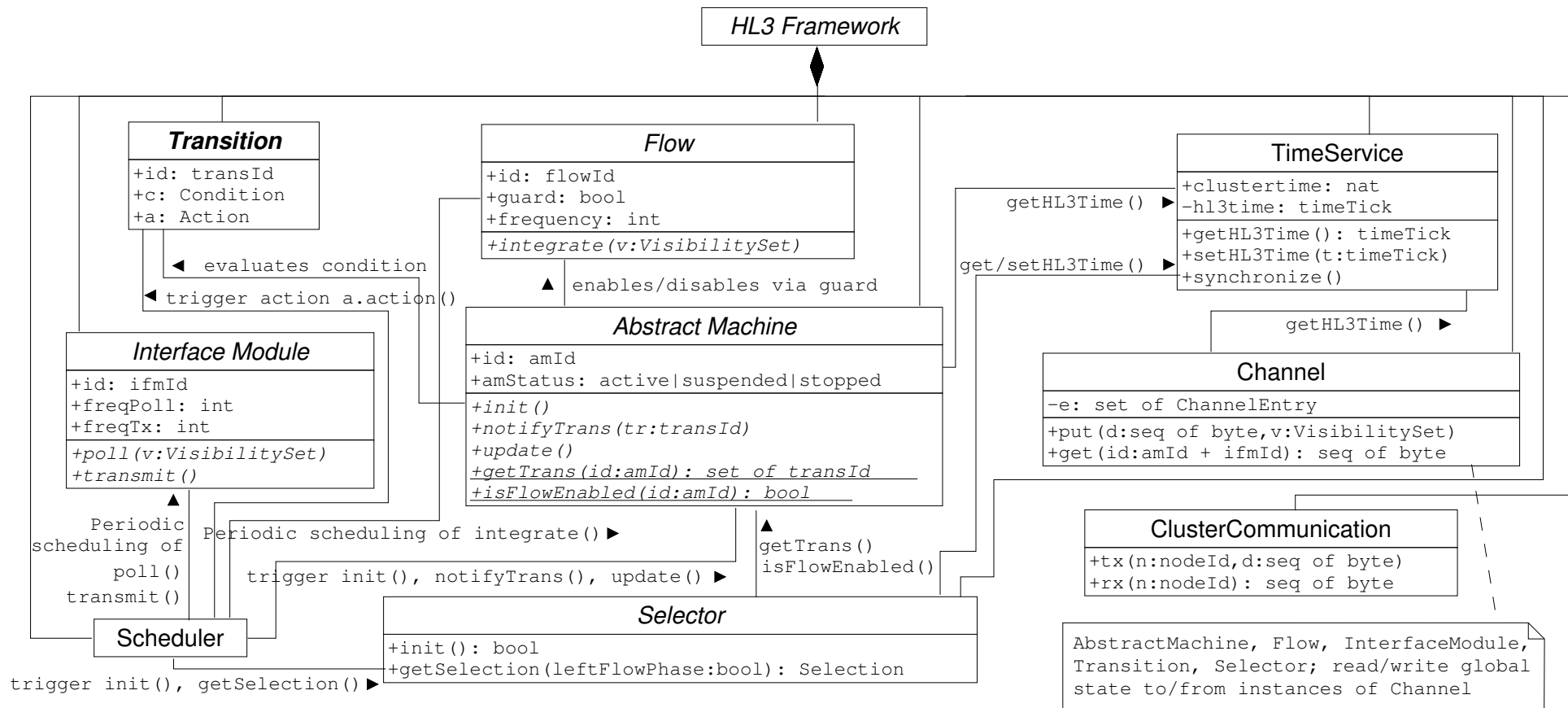
```
class Flow {
public:
    static void flowBrakePoint1 (const VisibilitySet &);
    static void flowBrakePoint2 (const VisibilitySet &);
    /* ... */
private:
    /** The flow's condition that guards if the flow is active or not. */
    bool m_guard;
    /** The associated abstract machine. */
    amId_t m_amId;
    /** The function that internally executes the integration step. */
    void (*const m_pItgrFct)(const VisibilitySet &);
public:
    /** Executes an integration step. */
    void integrate (const VisibilitySet &v) {if (m_guard) (*m_pItgrFct)(v);}
};
```



```
void Flow::flowBrakePoint1 (const VisibilitySet &visSet) {
    /* read values needed for calculation */
    RouteAtlas &ra = *(RouteAtlas*)Channel::ra.get(m_amId);
    float &v = *(float*)Channel::v.get(m_amId);
    GlobalConstants &gc = *(GlobalConstants*)Channel::gc.get(m_amId);
    /* prepare result */
    byteSeq_t byteSeq(sizeof(float));
    float &brakePoint1 = (float&)byteSeq;
    /* do calculate */
    brakePoint1
        = ra.vtp[1].x - (ra.vtp[1].v * ra.vtp[1].v - v * v) / 2 * gc.a_min;
    /* write result */
    Channel::brakePoint1.put(byteSeq, visSet);
}
```



Step 3 – Generate $HL^3::Transition...$



HybridUML Selector – getSelection(...)

HybridUML: interleaving of discrete and continuous steps

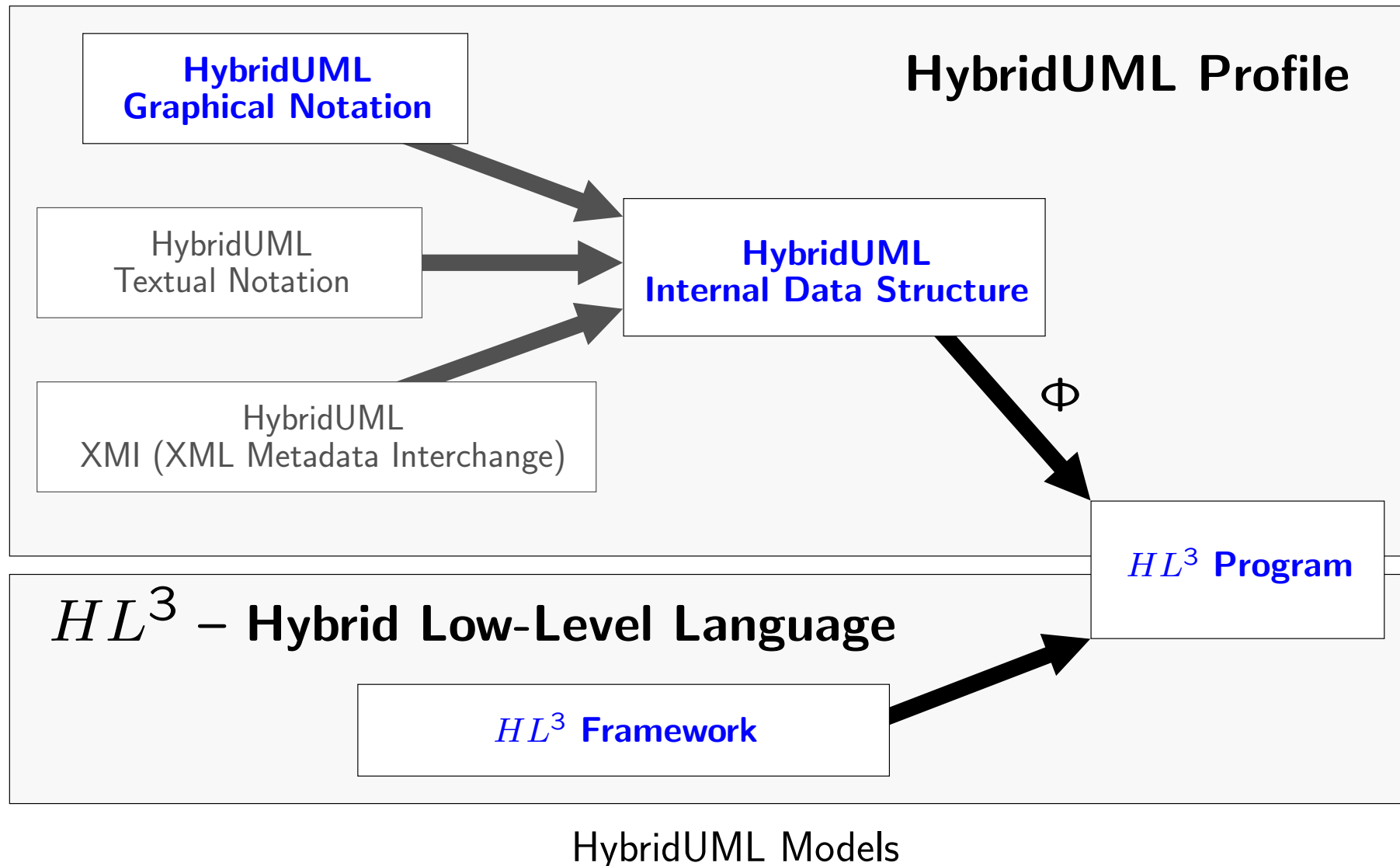
Discrete step ● A single basic agent fires one transition.

Continuous step ● All agents synchronously let time pass.

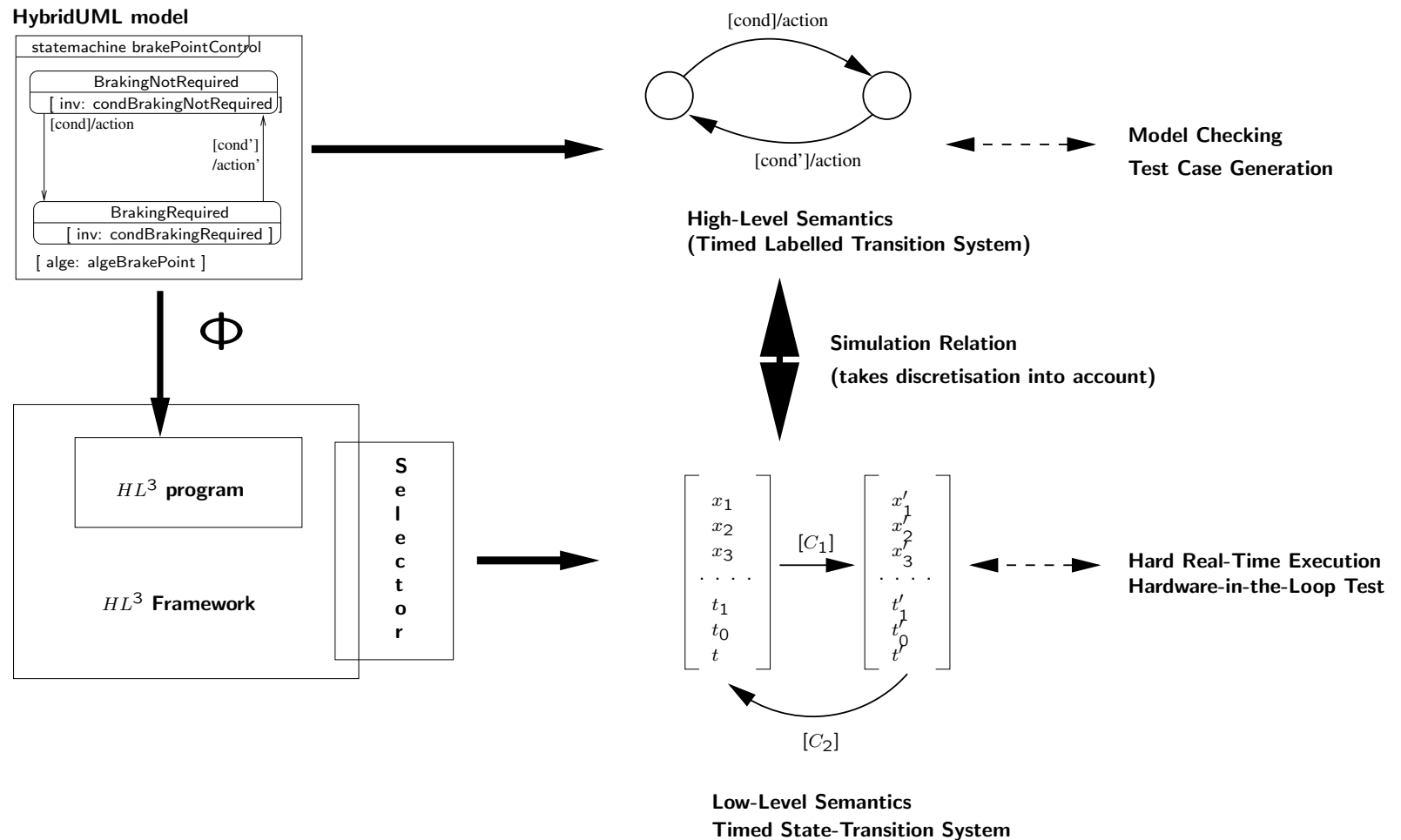
- Active algebraic and flow conditions are applied.
- All invariants of current mode configurations must be satisfied.

1. Active invariants are checked. $\Rightarrow e(c)$: Continuous step c admissible?
2. Set $T_{enabled}$ of enabled transitions is calculated.
3. $|T_{enabled}| > 0 \Rightarrow$ One enabled transition $t \in T_{enabled}$ is chosen non-deterministically.
4. $e(c) \wedge \neg(|T_{enabled}| > 0)$ — c is chosen.
 $\neg e(c) \wedge |T_{enabled}| > 0$ — t is chosen.
 $e(c) \wedge (|T_{enabled}| > 0)$ — Non-deterministic choice of t or c .
 $\neg e(c) \wedge \neg(|T_{enabled}| > 0)$ — Deadlock.
5. The chosen step is taken, then proceeded with 1.

... High-Level Semantics of HybridUML



... High-Level Semantics of HybridUML



HybridUML Model – High-Level Model – *HL³* Program

HybridUML Semantics

Semantics of agents are induced by (flat) Timed Labelled Transition System (LTS).

- Hierarchical structure of modes is encoded in *location* set Loc .
- A state σ maps (local and global) variable symbols to (appropriately typed) values
- Γ is a global structure denoting the signal space.
- Execution with respect to some global clock value $t \in \mathbb{R}_+$.

\implies An agent configuration is a tuple (loc, σ, Γ, t) .

Discrete Transitions

A discrete transition step labelled $c[b]/f(\sigma); d$ between two nodes loc and loc' in agent i is thus handled as transition

$$(loc, \sigma, \Gamma, t) \xrightarrow{c} (loc', \sigma', \Gamma', t)$$

if $\Gamma \models (c, i)$ and $\sigma \models b$,

with $\sigma' = f(\sigma)$, $\Gamma' \models \neg(c, i)$ and $\Gamma \models (d, j)$ for all agents j .

Flow Transitions

A flow transition f acts on all time-continuous variables simultaneously.

We have a transition

$$(loc, \sigma, \Gamma, t) \longrightarrow (loc, \sigma', \Gamma', t')$$

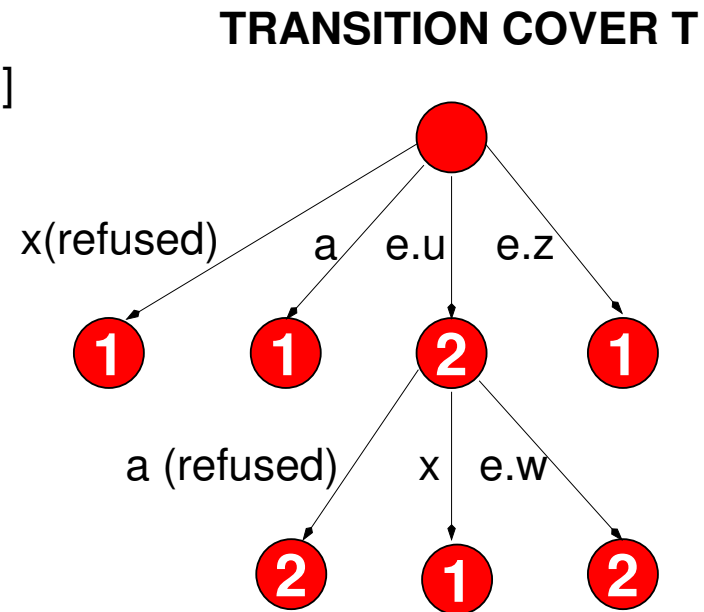
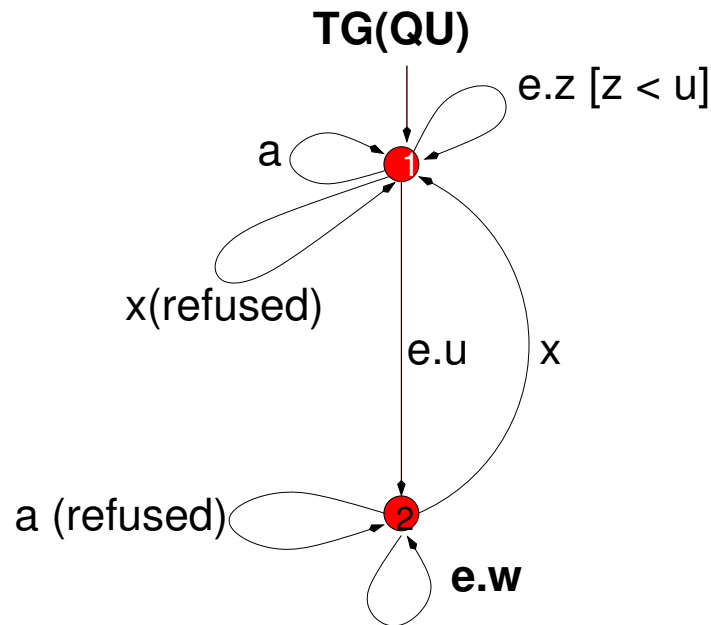
if the flow f is defined on the interval $[0, t' - t]$ and enabled on the interval $[t, t']$,
with $f(0) = \sigma$, $f(t' - t) = \sigma'$, and $\Gamma' \models \neg(sig, i)$ for all signals sig and all agents j .

Automated Testing against (Hybrid) Real-Time Specifications

- Automated Testing against Timed CSP specifications
 - **W-Method** style theorem: Correct coverage of testing tree and characterisation set implies **correctness** of system under test in the sense of **Timed Failures Refinement**
 - Efficient test data selection heuristics for systems with constant timer durations
- Test data selection for time-continuous observables:
 - Select piecewise smooth curves through tangent vector fields on differentiable manifolds
 - Equivalence between specification and implementation may be characterised as isometry between manifolds – metric tensor maps coordinates of physical state space to coordinates of implementation state space

Automated Testing against (Hybrid) Real-Time Specifications

Conjecture: We cannot find a weaker relation than isometry for implementation correctness



CHARACTERISATION SET $W = \{ \langle a \rangle \}$ **TESTS DEFINED BY** T^W

TEST TRACES $T1 = \langle x, a \rangle$ $T2 = \langle a, a \rangle$ $T3 = \langle e.u, a, a \rangle$

$T4 = \langle e.u, x, a \rangle$ $T5 = \langle e.u, e.w, a \rangle$ $T6 = \langle e.z, a \rangle$

complete set of tests if SUT has the same number of states as Q

Domain-specific description of railway control systems

- Motivation:
 - Wide-spectrum formalism are suitable for most application domains, but require considerable IT expertise \Rightarrow too complicated to be used as a means of communication between domain experts and IT specialists
 - Reason: language elements of wide-spectrum formalisms do not map directly onto concrete objects of the application domain
- Objectives of domain-specific formalisms:
 - Facilitate communication between domain experts and IT specialists by using terms and objects of the application domain in a direct way.
 - Define formal meaning of domain-specific descriptions by mapping into formal model or into wide-spectrum language with well-defined semantics

- Question: Is UML suitable for domain-specific descriptions?

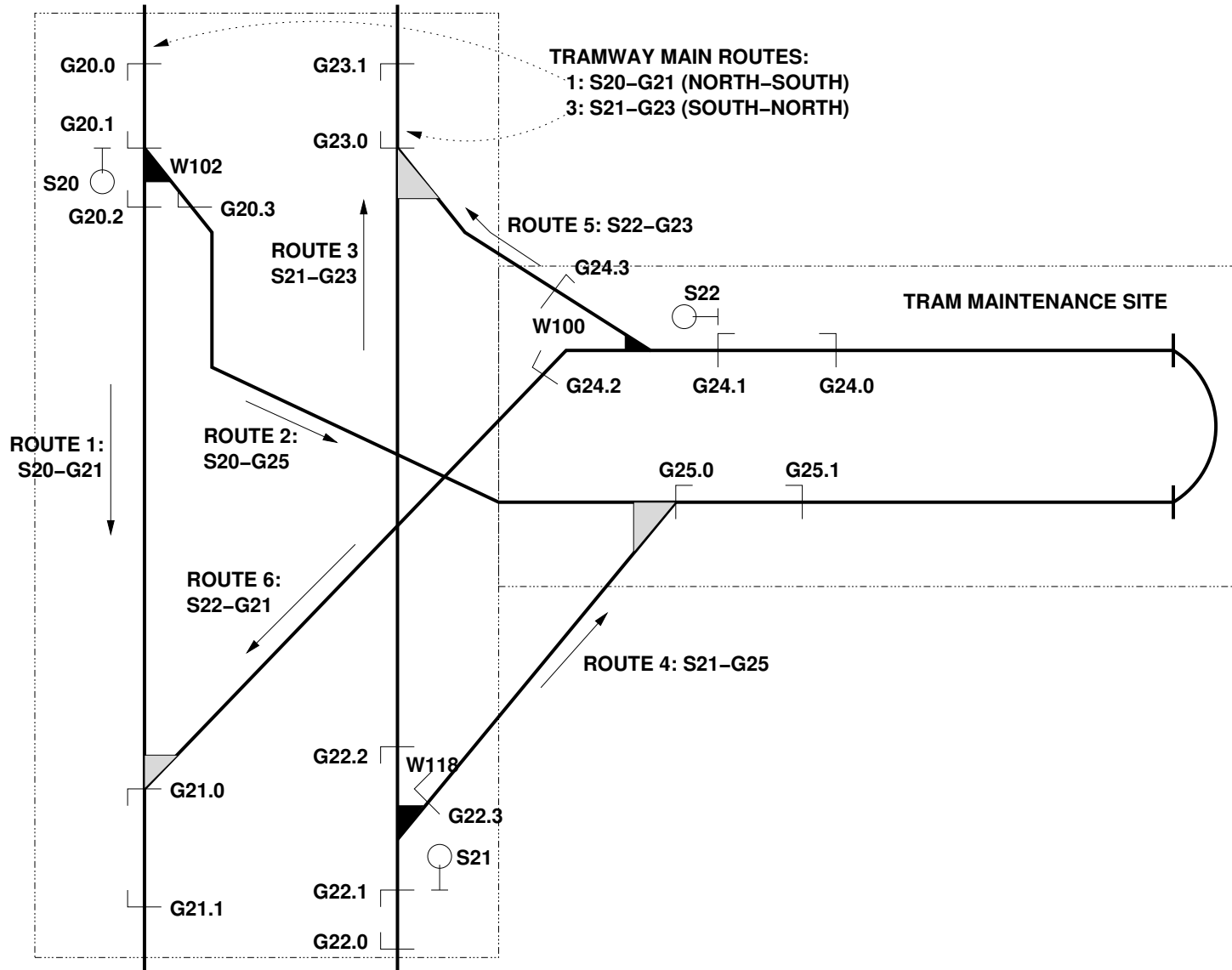
- Answer: Yes – but we need UML2.0 with full profiling support:
 - Explain terms and objects of the application domain by means of the UML2 profile mechanism

 - Semi-formal semantics is given by the UML2.0-style profile description

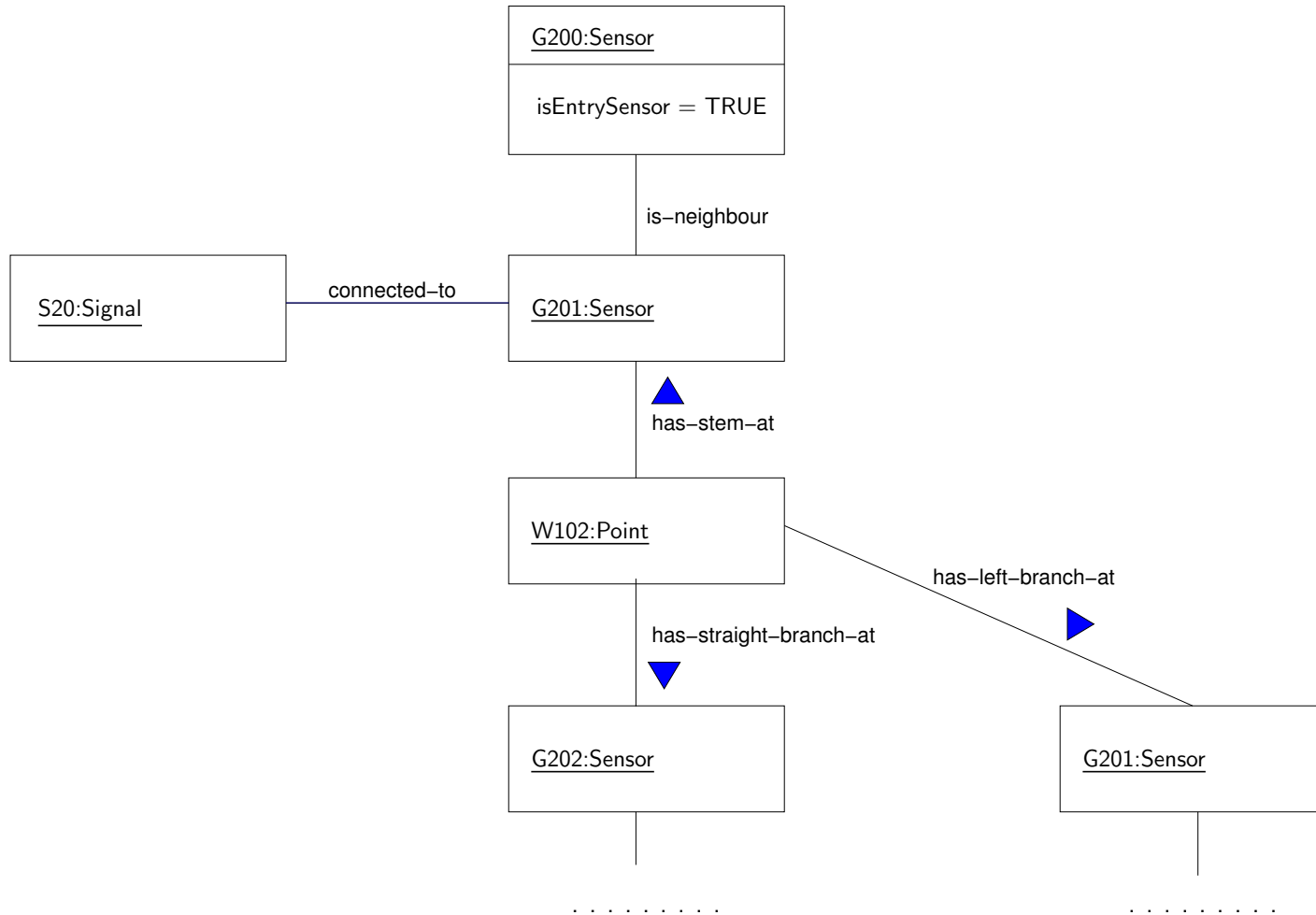
 - Formal semantics is available, as long as constructs used in profile have formal meaning
 - for example, HybridUML constructs

 - Use domain-specific icons to depict the language elements of the new profile

- Examples from the railway domain:
 - Abstract railway networks are diagrams with nodes **Signal**, **Point**, **Sensor**, **Track Segment** and associations such as **connected-to**
 - These nodes are derived from HybridUML stereotype **Agent** – that is, from **Class** and **StateMachine**
 - Generic transition rules are encoded by StateMachines associated with each type of agent
 - A project-specific railway network is a concrete object diagram instantiated from the Agent diagram
 - Concrete object behaviour is specified by inserting concrete object identifications into StateMachines

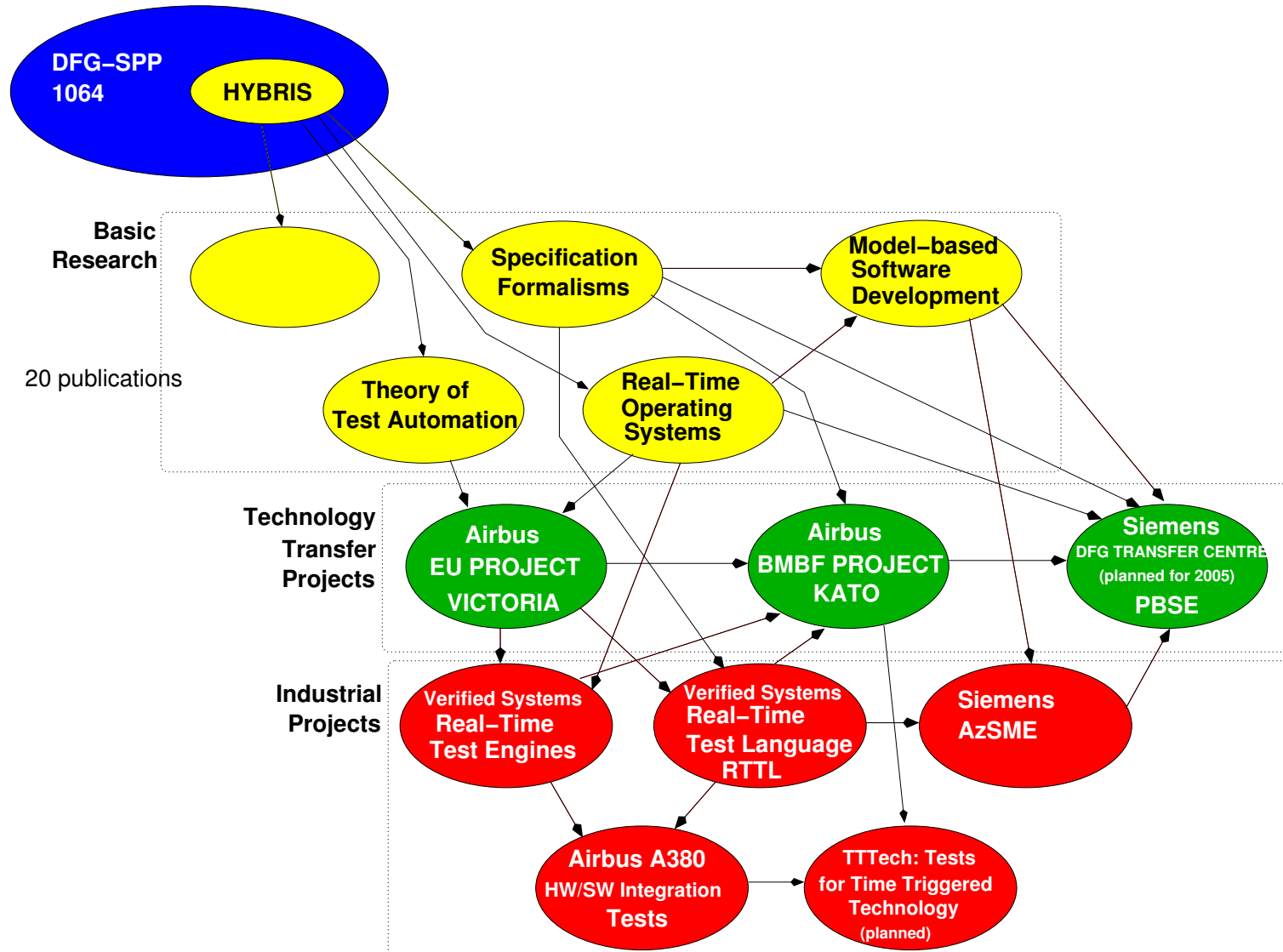


Tramway network



Tramway network – UML2.0 representation

Conclusion – Impact of the HYBRIS Project



Contributions by ...

Peter Amthor – Kirsten Berkenkötter – Stefan Bisanz – Bettina Buth – Markus Dahlweid – Rolf Drechsler – Christof Efkemann – Ingo Fiß – Daniel Große – Ulrich Hannemann – Anne E. Haxthausen – Detlef Kendelbacher – Oliver Meyer – Jan Peleska – Holger Schlingloff – Uwe Schulze – Aliko Tsiolakis

Literature

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The end.

$$\begin{aligned} \mathbf{condBrakingRequired} &\equiv & (1) \\ \exists i \in \{1..VTP_COUNT\} \bullet \\ & \quad brakePoint[i].x \leq x \wedge ra.vtp[i].v < v \wedge ra.vtp[i].x > x \wedge \\ & \quad (vtpActive[i] \vee (3) \text{ condTooLate}) \end{aligned}$$

$$\begin{aligned} \mathbf{condBrakingNotRequired} &\equiv & (2) \\ \forall i \in \{1..VTP_COUNT\} \bullet \\ & \quad \neg(brakePoint[i].x \leq x \wedge ra.vtp[i].v < v \wedge ra.vtp[i].x > x \wedge \\ & \quad (vtpActive[i] \vee (3) \text{ condTooLate})) \end{aligned}$$

$$\begin{aligned} \mathbf{condTooLate} &\equiv & (3) \\ & \mathit{ra.vtp}[i].\mathit{type} = \mathit{VTP_TYPE.CROSSING} \wedge \\ & ((x_{\mathit{closedTooLong},1}[\mathit{ra.vtp}[i].\mathit{cr.id}] \leq \mathit{ra.vtp}[i].\mathit{cr.x}_{\mathit{end}} + \mathit{const.l} \\ & \quad \wedge t_{\mathit{closedTooLong}}[\mathit{ra.vtp}[i].\mathit{cr.id}] \leq t_{\mathit{brake}}) \\ & \vee (x_{\mathit{closedTooLong},2}[\mathit{ra.vtp}[i].\mathit{cr.id}] \leq \mathit{ra.vtp}[i].\mathit{cr.x}_{\mathit{end}} + \mathit{const.l} \\ & \quad \wedge t_{\mathit{closedTooLong}}[\mathit{ra.vtp}[i].\mathit{cr.id}] > t_{\mathit{brake}})) \end{aligned}$$

algeBrakePoint \equiv

$$\forall i \in \{1..VTP_COUNT\} \bullet \mathit{brakePoint}[i] = \mathit{ra.vtp}[i].x - \frac{\mathit{ra.vtp}[i].v^2 - v^2}{2 \cdot \mathit{const.a}_{min}}$$

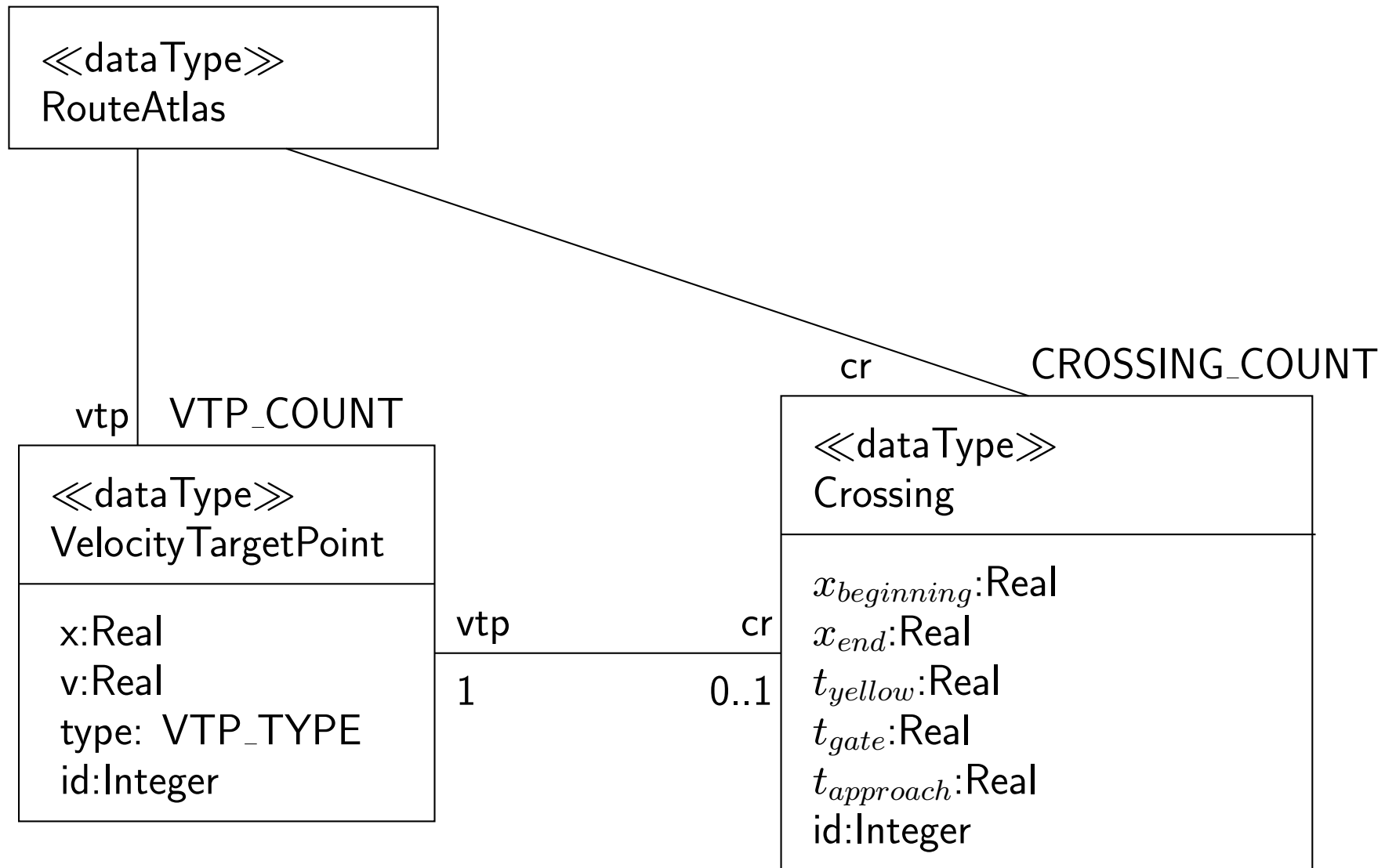
(4)

$$\mathbf{algeStoppingDistance} \equiv (5)$$
$$s_{brake} = \frac{-v^2}{2 \cdot const.a_{min}}$$

$$\mathbf{algeStoppingDuration} \equiv (6)$$
$$t_{brake} = \frac{-v}{const.a_{min}}$$

$$\begin{aligned} \mathbf{algeGuaranteedPosition1} &\equiv & (7) \\ \forall c \in \{1..CROSSING_COUNT\} \bullet \\ x_{closedTooLong,1}[c] &= x + \frac{const.a_{min}}{2} \cdot t_{closedTooLong}[c]^2 + v \cdot t_{closedTooLong}[c] \end{aligned}$$

$$\begin{aligned} \mathbf{algeGuaranteedPosition2} &\equiv & (8) \\ \forall c \in \{1..CROSSING_COUNT\} \bullet \\ x_{closedTooLong,2}[c] &= x + s_{brake} + (t_{closedTooLong}[c] - t_{brake}) \cdot const.v_{pass} \end{aligned}$$



Datatypes

$$\begin{aligned} \mathbf{readSetTransBrakingRequired} &\equiv & (9) \\ \{v \mid \exists i \in \{1..VTP_COUNT\} \bullet \\ & v \equiv \mathit{chan}(\mathit{vtpActive}[i]) \vee v \equiv \mathit{chan}(\mathit{brakePoint}[i]) \vee \\ & v \equiv \mathit{chan}(\mathit{ra.vtp}[i].v) \vee v \equiv \mathit{chan}(\mathit{ra.vtp}[i].x) \\ & \} \cup \{\mathit{chan}(x), \mathit{chan}(v)\} \end{aligned}$$