

Plan for today

Description Logics: a Nice Family of Logics

— Modularity —

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And now ...

- 1 What is modularity good for?
- 2 Modules for reuse
- 3 Summary and Outlook

What can I do with my ontology?

Ontology users and engineers want to use ontologies to

- represent and archive knowledge **(M)**
in a structured way
- compute inferences from archived knowledge **(M)**
e.g., classification, query answering
- explain inferences **(M)**
justifications = pinpointing, abduction
- reuse (parts of) other ontologies to build their ontology **(M)**
import
- expose the logical structure of the represented knowledge **(M)**
comprehension



(M) = modularity helps



What can I do with my ontology?

Building and using an ontology often requires

- fast reasoning **(M)**
expressivity \leftrightarrow complexity; optimisations, incremental reasoning
- collaborative development **(M)**
- version control **(M)**
- *efficient* reuse **(M)**
- an understanding of the ontology's content and structure **(M)**
comprehension

(M) = modularity helps



And now ...

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A priori vs. a posteriori modularisation

A priori (not covered today)

- At first, a modular structure is decided on.
- Then, the ontology is developed and used according to that structure.

A posteriori

- The ontology is regarded as a monolithic entity.
- At some point, a module is extracted or the ontology is decomposed into several modules.



Comparing two ontologies

Assume that ...

- you want to buy a medical ontology from me
- I offer two medical ontologies \mathcal{O}_1 and \mathcal{O}_2

Q: which one do you choose?

Possible A: the one that contains more knowledge.

Q: how do you measure the amount of knowledge in \mathcal{O}_i ?

Possible A: ~~Number of axioms?~~

- Well, compare $\{A \sqsubseteq B, B \sqsubseteq A\}$ vs. $\{A \equiv B\}$
- or $\{A \sqsubseteq B, B \sqsubseteq A \sqcup \neg A, A \sqcap \neg A \sqsubseteq B\}$ vs. $\{A \equiv B\}$

Possible A: Number of entailments? Number of models?



Ontologies and their entailments

Think of axioms as **generating entailments** – e.g.:

$$\left. \begin{array}{l} A \sqsubseteq \exists r.B \\ \exists r.T \sqsubseteq C \sqcap D \end{array} \right\} \models A \sqsubseteq D$$

Q: how many entailments can a TBox have?

A:

$$A \sqsubseteq D \quad A \sqsubseteq D \sqcup A \quad A \sqsubseteq D \sqcup (A \sqcap D), \quad \dots$$

∞



Ontologies and their models

Think of axioms as **restricting possible models**

Axioms “filter out” unwanted models – e.g.:

- $\text{Hand} \sqsubseteq \exists \text{hasPart.Finger}$
 \rightsquigarrow models cannot have instances of Hand with no hasPart-edge to an instance of Finger
- $\text{Hand} \sqsubseteq = 5 \text{hasPart.Finger}$
 \rightsquigarrow models cannot have instances of Hand with $\neq 5$ hasPart-edges to instances of Finger

Q: how many models can a TBox have?

A: 0

∞



Next attempt at “more” entailments/models

We cannot compare *numbers* of entailments or models

But we can use set inclusion:

“ \mathcal{O} knows at most as much as \mathcal{O}' ” if

- every entailment of \mathcal{O} is one of \mathcal{O}' :
 $\{\eta \mid \mathcal{O} \models \eta\} \subseteq \{\eta \mid \mathcal{O}' \models \eta\}$ or
- every model of \mathcal{O}' is one of \mathcal{O} :
 $\{\mathcal{I} \mid \mathcal{I} \models \mathcal{O}'\} \subseteq \{\mathcal{I} \mid \mathcal{I} \models \mathcal{O}\}$

Problem:

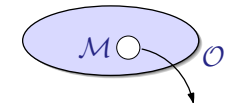
How do we test these conditions?



Knowledge w.r.t. a signature

Let's reformulate the initial dialogue.

Assume that ...



- you want to buy a **subset of** a medical ontology \mathcal{O} from me that covers the subdomain of, say, diseases
- I offer two subsets \mathcal{M}_1 and \mathcal{M}_2

Q: which one do you choose?

Possible A: the one that “knows more” about diseases!

Q: which is the **best subset** I can offer?

Possible A: a **module for diseases**

- $\mathcal{M} \sqsubseteq \mathcal{O}$ that knows as much as \mathcal{O} about diseases:
 \mathcal{M} **indistinguishable** from \mathcal{O} w.r.t. all terms relevant for diseases
- \mathcal{M} as small as possible



Inseparability w.r.t. a signature

Definition

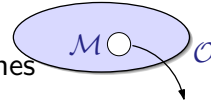
- **Signature** Σ = a set of concept/role names
- The signature of axiom (ontology) X
= all concept/role names in X
- \mathcal{O}_1 and \mathcal{O}_2 are **Σ -inseparable w.r.t. a logic \mathcal{L}** ,
written $\mathcal{O}_1 \equiv_{\Sigma}^{\mathcal{L}} \mathcal{O}_2$, if: [Konev et al. 2009]
for all $\eta \in \mathcal{L}$ with $\text{sig}(\eta) \subseteq \Sigma$,

$$\mathcal{O}_1 \models \eta \quad \text{iff} \quad \mathcal{O}_2 \models \eta$$

- \mathcal{O} is a **Σ -conservative extension (Σ -dCE)** of \mathcal{M} w.r.t. \mathcal{L}
if $\mathcal{M} \subseteq \mathcal{O}$ and $\mathcal{M} \equiv_{\Sigma}^{\mathcal{L}} \mathcal{O}$ [Ghilardi et al. 2006]

Alternative names:

- \mathcal{M} **covers** \mathcal{O} for Σ w.r.t. \mathcal{L}
- \mathcal{M} is a **module of** \mathcal{O} for Σ w.r.t. \mathcal{L}



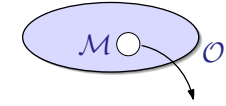
Choosing the signature Σ

Definition (repeated from previous slide)

\mathcal{O} is a Σ -module of \mathcal{M} w.r.t. \mathcal{L}
if $\mathcal{M} \subseteq \mathcal{O}$ and $\mathcal{M} \equiv_{\Sigma}^{\mathcal{L}} \mathcal{O}$

The signature Σ ...

- can be seen as a “topic”
- that the module is required to cover
- is difficult to formulate:
 - **Q:** how many interesting entailments in $\Sigma = \{\text{Disease}\}$
can \mathcal{O} possibly have?



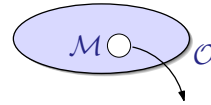
Choosing the logic \mathcal{L}

Definition (repeated from previous slide)

\mathcal{O} is a Σ -module of \mathcal{M} w.r.t. \mathcal{L}
if $\mathcal{M} \subseteq \mathcal{O}$ and $\mathcal{M} \equiv_{\Sigma}^{\mathcal{L}} \mathcal{O}$

Choice of \mathcal{L} depends on your usage of the module:

- for ontology design: subsumptions betw. (complex?) concepts
- for ontology usage: your favourite query language



Modules for reuse

If we want to reuse module \mathcal{M} ,
we need a stronger guarantee:

$$\mathcal{M} \cup \mathcal{O}' \equiv_{\Sigma}^{\mathcal{L}} \mathcal{O} \cup \mathcal{O}' \quad \text{for all } \mathcal{O}'$$

i.e., we can safely import \mathcal{M} into any \mathcal{O}'

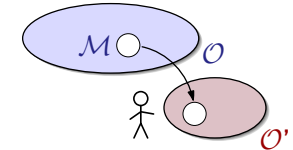
Ensured by two additional requirements:

Lemma [Konev et al. 2009]

If $\mathcal{M} \subseteq \mathcal{O}$ and $\mathcal{M} \equiv_{\Sigma}^{\mathcal{L}} \mathcal{O}$, then $\mathcal{M} \cup \mathcal{O}' \equiv_{\Sigma}^{\mathcal{L}} \mathcal{O} \cup \mathcal{O}'$, for

- 1 every \mathcal{O}' with $\text{sig}(\mathcal{O}) \cap \text{sig}(\mathcal{O}') \subseteq \Sigma$,
- 2 expressive enough \mathcal{L} , e.g. *SROIQ* (OWL).

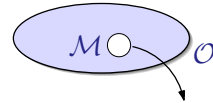
(1) means that \mathcal{O}' may reuse only terms from Σ



How is a minimal Σ -module extracted?

Simple module extraction algorithm:

- $\mathcal{M} \leftarrow \mathcal{O}$
- While $\mathcal{M} \setminus \{\alpha\} \equiv_{\Sigma}^{\mathcal{L}} \mathcal{O}$, for some $\alpha \in \mathcal{M}$,
do $\mathcal{M} \leftarrow \mathcal{M} \setminus \{\alpha\}$
- Output \mathcal{M}



Observation:

Different orders of choosing α
can lead to different minimal modules

Example

Let $\Sigma = \{\text{Knee}, \text{HingeJoint}\}$. Suppose *Galen* contains:

$$\text{Knee} \equiv \text{Joint} \sqcap \exists \text{hasPart.Patella} \sqcap \exists \text{hasFunct.Hinge} \quad (1)$$

$$\text{Patella} \sqsubseteq \text{Bone} \sqcap \text{Sesamoid} \quad (2)$$

$$\text{Ginglymus} \equiv \text{Joint} \sqcap \exists \text{hasFunct.Hinge} \quad (3)$$

$$\text{Joint} \sqcap \exists \text{hasPart.}(\text{Bone} \sqcap \text{Sesamoid}) \sqsubseteq \text{Ginglymus} \quad (4)$$

$$\text{Ginglymus} \equiv \text{HingeJoint} \quad (5)$$

$$\text{Meniscus} \equiv \text{FibroCartilage} \sqcap \exists \text{locatedIn.Knee} \quad (6)$$

\sqsubseteq -Minimal module for Σ ? $\{(1), (2), (4), (5)\}$ and $\{(1), (3), (5)\}$

Note that a module for Σ does not necessarily contain

- all axioms that use terms from Σ
- only axioms that only use terms from Σ



Bad news for expressive ontology languages?

Big, sad theorem [Ghilardi et al. 2006]

Let $\mathcal{O}_1, \mathcal{O}_2$ be ontologies in \mathcal{L} and Σ a signature.

Determining whether $\mathcal{O}_1 \equiv_{\Sigma}^{\mathcal{L}} \mathcal{O}_2$ is

EXPTIME-complete for $\mathcal{L} = \mathcal{EL}$
2EXPTIME-complete for $\mathcal{ALC} \leq \mathcal{L} \leq \mathcal{ALCQI}$, and
undecidable for $\mathcal{L} \geq \mathcal{ALCQO}$, including OWL

(even if $\mathcal{O}_1, \mathcal{O}_2$ are in \mathcal{ALC}).

Consequences for modules of expressive DLs

Extracting modules is highly complex for expressive DLs.

What to do?

- 1 Give up? No: modules clearly too important
- 2 Reduce expressivity of logic? Yes! (Not covered here.)
- 3 Approximate for expressive logics? Yes – but from the *right* direction!

Next: 2 approximations, i.e., sufficient conditions for inseparability

- 1 based on semantic locality
- 2 based on syntactic locality

[Cuenca Grau et al. 2009]



Model-theoretic inseparability

Remember: $\mathcal{O}_1 \equiv_{\Sigma}^{\mathcal{L}} \mathcal{O}_2$ if:
for all $\eta \in \mathcal{L}$ with $\text{sig}(\eta) \subseteq \Sigma$,

$$\mathcal{O}_1 \models \eta \quad \text{iff} \quad \mathcal{O}_2 \models \eta$$

Good news:

\Uparrow

$$\{\mathcal{I}|_{\Sigma} \mid \mathcal{I} \models \mathcal{O}_1\} = \{\mathcal{I}|_{\Sigma} \mid \mathcal{I} \models \mathcal{O}_2\}$$

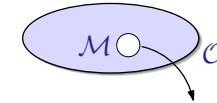
- i.e., \mathcal{O}_1 and \mathcal{O}_2 have the same models modulo Σ ($\mathcal{I}|_{\Sigma}$ is the restriction of \mathcal{I} to Σ)
- shorthand: $\mathcal{O}_1 \equiv_{\Sigma}^{\text{mod}} \mathcal{O}_2$ (model-inseparable)
- this notion does not depend on \mathcal{L}

Bad news: $\mathcal{O}_1 \equiv_{\Sigma}^{\text{mod}} \mathcal{O}_2$ is undecidable already for \mathcal{ALC} !



Semantic locality

We can approximate model-inseparability, exploiting that \mathcal{M} is a subset of \mathcal{O}



$$\mathcal{M} \equiv_{\Sigma}^{\text{mod}} \mathcal{O}$$

\Updownarrow

every $\mathcal{I} \models \mathcal{M}$ can be extended to $\mathcal{J} \models \mathcal{O}$ with $\mathcal{I}|_{\Sigma} = \mathcal{J}|_{\Sigma}$

\Uparrow

every $\mathcal{I} \models \mathcal{M}$ can be extended to $\mathcal{J} \models \mathcal{O}$ with $\mathcal{I}|_{\Sigma} = \mathcal{J}|_{\Sigma}$
and $\forall X \notin \Sigma : X^{\mathcal{J}} = \emptyset$

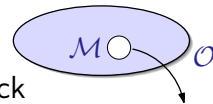
\Updownarrow

every $\alpha \in \mathcal{O} \setminus \mathcal{M}$ is **semantically local w.r.t.** $\Sigma \cup \text{sig}(\mathcal{M})$:
 α , with all terms not in $\Sigma \cup \text{sig}(\mathcal{M})$ replaced by \perp , is a tautology



From semantic to syntactic locality

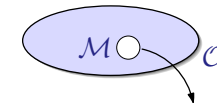
- Semantic locality involves tautology check
 \rightsquigarrow can be tested using a reasoner
 \rightsquigarrow has the same complexity as standard reasoning
- A syntactic approximation that can be tested in poly-time:
syntactic locality
(describes “obviously” sem. local axioms via a grammar)
- Both notions lead to modules that are
 - $(\Sigma \cup \text{sig}(\mathcal{M}))$ -inseparable from \mathcal{O}
 - not necessarily minimal



Module extraction with locality

Module extraction algorithm:

- $\mathcal{M} \leftarrow \emptyset$
- While α **not local** w.r.t. $\Sigma \cup \text{sig}(\mathcal{M})$, for some $\alpha \in \mathcal{O} \setminus \mathcal{M}$,
do $\mathcal{M} \leftarrow \mathcal{M} \cup \{\alpha\}$
- Output \mathcal{M}



Variations:

- this notion: (semantic/syntactic) \perp -module
- dual notion: (semantic/syntactic) \top -module
- smaller modules by nesting \top - and \perp -module extraction:
 $\top\perp^*$ -modules



Summary locality-based modules

Locality-based modules ...

- are “good approximations” of minimal modules because they guarantee $\mathcal{M} \equiv_{\Sigma}^{\mathcal{L}} \mathcal{O}$
- are not necessarily minimal (but in practice often small enough)
- can be extracted in polynomial time (syntactic locality)
- are even **self-contained**:

$$\mathcal{M} \equiv_{\Sigma \cup \text{sig}(\mathcal{M})}^{\mathcal{L}} \mathcal{O}$$

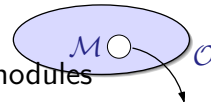
and **depleting**:

$$\mathcal{O} \setminus \mathcal{M} \equiv_{\Sigma \cup \text{sig}(\mathcal{M})}^{\mathcal{L}} \emptyset$$

and thus **unique**

- contain all justifications for any α with $\text{sig}(\alpha) \subseteq \Sigma$

↪ **Cheap is cheerful! :)**



And now ...

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Summary on modularity

- Inseparability/coverage is a guarantee relevant (not only) for reuse
- Approximation of minimal covering modules via locality
- Modules based on syntactic locality can be extracted efficiently in logics up to *SR_OI_Q* (OWL 2)
- Tool support for extracting modules:
<http://owl.cs.manchester.ac.uk/modularity>
<http://owlapl.sourceforge.net/>
- This line of research is rather new for DLs and ontology languages, and many questions are (half)open.



See also ...

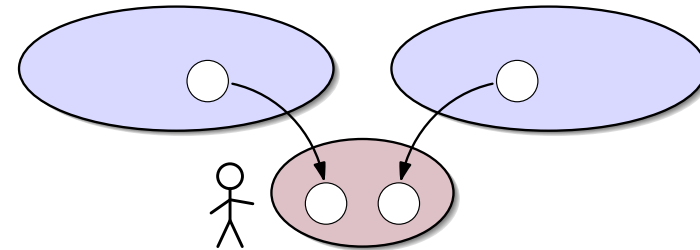
- ... slides from ESSLLI 2013 course “Modularity in Ontologies”:
http://www.informatik.uni-bremen.de/~ts/teaching/2013_modularity/
- ... the references at the end of this presentation

We’re almost done! :)



Appendix and References

“Borrow” knowledge from external ontologies



- Provides access to well-established knowledge
- Doesn't require expertise in external disciplines

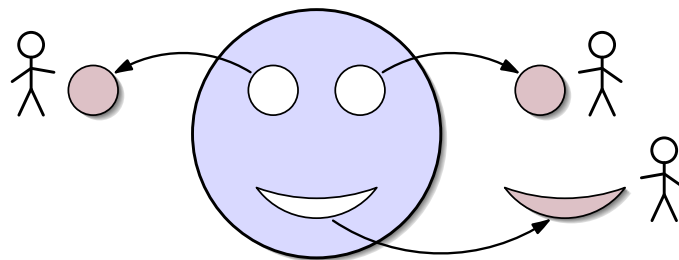
This scenario is well-understood and implemented.



A collaboration scenario

Understanding and/or structuring an ontology

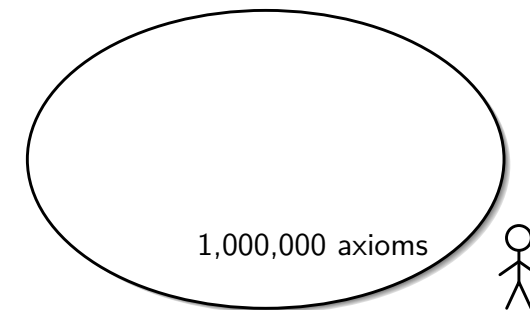
Collaborative ontology development



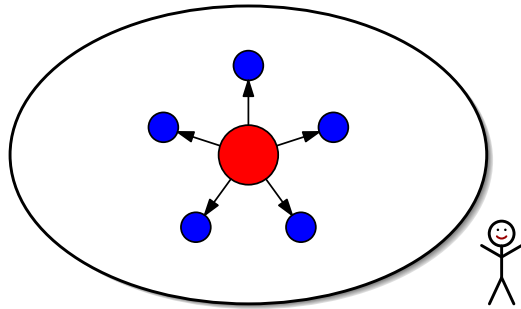
- Developers work (edit, classify) locally
- Extra care at re-combination
- Prescriptive/analytic behaviour

This approach is mostly understood, but not implemented yet.

Compute the modular structure of an ontology





Compute the modular structure of an ontology



This is work in progress.

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 Extracting Modules from Ontologies: a Logic-Based Approach.
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