

Systeme hoher Sicherheit und Qualität Universität Bremen, WS 2017/2018

Lecture 07:



# Testing

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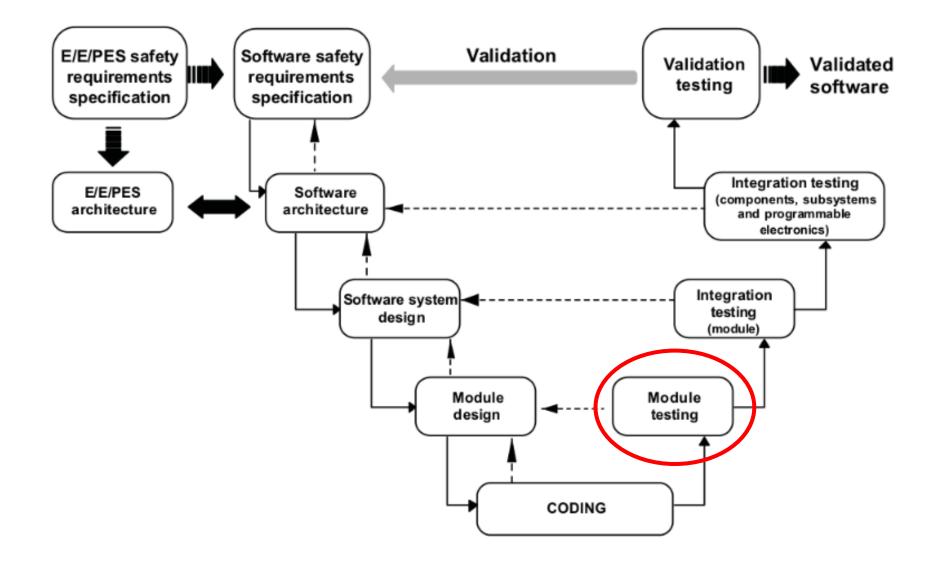
### Where are we?

- 01: Concepts of Quality
- 02: Legal Requirements: Norms and Standards
- 03: The Software Development Process
- 04: Hazard Analysis
- 05: High-Level Design with SysML
- 06: Formal Modelling with OCL
- 07: Testing
- 08: Static Program Analysis
- 09-10: Software Verification
- 11-12: Model Checking
- 13: Conclusions





# **Testing in the Development Cycle**





# What is Testing?

Testing is the process of executing a program or system with the intent of finding errors.

G.J. Myers, 1979

- ► In our sense, testing is selected, controlled program execution
- ► The **aim** of testing is to detect bugs, such as
  - derivation of occurring characteristics of quality properties compared to the specified ones
  - inconsistency between specification and implementation
  - structural features of a program that cause a faulty behavior of a program

Program testing can be used to show the presence of bugs, but never to show their absence.

E.W. Dijkstra, 1972





### **The Testing Process**

► Test cases, test plan, etc.

- System-under-test (s.u.t.) (cf. TOE in CC)
- ► Warning -- test literature is quite expansive

Testing is any activity aimed at evaluating an attribute or capability of a program or system and determining that it meets its required results.

Hetzel, 1983





### **Test Levels**

### Component and unit tests

test at the interface level of single components (modules, classes)

### Integration test

testing interfaces of components fit together

#### System test

functional and non-functional test of the complete system from the user's perspective

### Acceptance test

testing if system implements contract details



### **Test Methods**

- Static vs. dynamic
  - With static tests, the code is analyzed without being run. We cover these methods as static program analysis later
  - With dynamic tests, we run the code under controlled conditions, and check the results against a given specification
- Central question: where do the test cases come from?
  - Black-box: the inner structure of the s.u.t. is opaque, test cases are derived from specification only.
  - Grey-box: some inner structure of the s.u.t. is known, e.g. module architecture.
  - White-box: the inner structure of the s.u.t. is known, and tests cases are derived from the source code.



### **Black-Box Tests**

- Limit analysis:
  - If the specification limits input parameters, then values close to these limits should be chosen
  - Idea is that programs behave continuously, and errors occur at these limits
- Equivalence classes:
  - If the input parameter values can be decomposed into classes which are treated equivalently, test cases have to cover all classes
- Smoke test:
  - "Run it, and check it does not go up in smoke."



# **Example: Black-Box Testing**

#### Equivalence classes or limits?

#### **Example: A Company Bonus System**

The loyalty bonus shall be computed depending on the time of employment. For employees of more than three years, it shall be 50% of the monthly salary, for employees of more than five years, 75%, and for employees of more than eight years, it shall be 100%.

### Equivalence classes or limits?

#### **Example: Air Bag**

The air bag shall be released if the vertical acceleration  $a_v$  equals or exceeds 15  $m/_{s^2}$ . The vertical acceleration will never be less than zero, or more than 40  $m/_{s^2}$ .



### **Black-Box Tests**

### Quite typical for GUI tests, or functional testing

- Testing invalid input: depends on programming language the stronger the typing, the less testing for invalid input is required
  - Example: consider lists in C, Java, Haskell
  - Example: consider object-relational mappings<sup>1</sup> (ORM) in Python, Java

1) Translating e.g. SQL-entries to objects



## **Property- based Testing**

- In property-based testing (or random testing), we generate random input values, and check the results against a given executable specification.
- Attention needs to be paid to the **distribution** values.
- Works better with high-level languages, where the datatypes represent more information on an abstract level and where the language is powerful enough to write comprehensive executable specifications (i.e. Boolean expressions).
  - Implementations for e.g. Haskell, Scala, Java
- Example: consider list reversal in C, Java, Haskell
  - Executable spec: reversal is idempotent and distributes over concatenation.
  - Question: how to generate random lists?



### **White-Box Tests**

In white-box tests, we derive test cases based on the structure of the program (structural testing)

To abstract from the source code (which is a purely syntactic artefact), we consider the control flow graph of the program.

#### **Def: Control Flow Graph (CFG)**

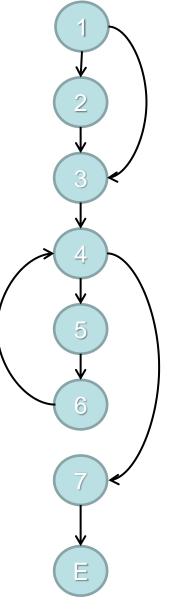
- nodes as elementary statements (e.g. assignments, return, break, . . . ), as well as control expressions (e.g. in conditionals and loops), and
- vertices from n to m if the control flow can reach a node m coming from a node n.

Hence, paths in the CFG correspond to runs of the program.



# **Example: Control-Flow Graph**

**if** (x < 0) /\*1\*/ { x:= - x /\*2\*/ } z = 1; /\*3\*/ **while** (x > 0) /\*4\*/ { z = z \* y; /\*5\*/ x = x - 1 /\*6\*/**return** 7 /\*7\*/



An execution path is a path though the cfg.

### Examples:

- [1,3,4,7, E]
- [1,2,3,4,7, E]
- [1,2,3,4,5,6,4,7, E]
- [1,3,4,5,6,4,5,6,4,7, E]

• • • •



### Coverage

#### Statement coverage:

Each **node** in the CFG is visited at least once.

#### Branch coverage:

Each **vertex** in the CFG is traversed at least once.

### Decision coverage:

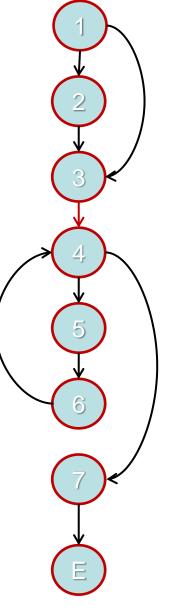
Like branch coverage, but specifies how often **conditions** (branching points) must be evaluated.

Path coverage: Each path in the CFG is executed at least once.



# **Example: Statement Coverage**

if (x < 0) /\*1\*/ {
 x:= - x /\*2\*/
}
z = 1; /\*3\*/
while (x > 0) /\*4\*/ {
 z = z \* y; /\*5\*/
 x = x - 1 /\*6\*/
}
return z /\*7\*/



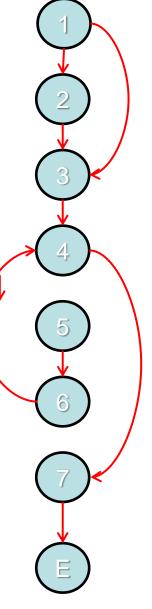
- Which (minimal) path covers all statements?
  - p = [1,2,3,4,5,6,4,7,E]
- Which state generates p?

x = -1 y any z any



# **Example: Branch Coverage**

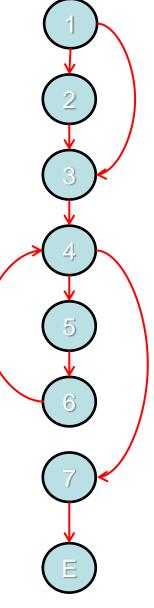
**if** (x < 0) /\*1\*/ { x:= - x /\*2\*/ } z = 1; /\*3\*/ **while** (x > 0) /\*4\*/ { z = z \* y; /\*5\*/ x = x - 1 /\*6\*/return z /\*7\*/



- ▶ Which (minimal) path covers all vertices?  $p_1 = [1,2,3,4,5,6,4,7,E]$  $p_2 = [1,3,4,7,E]$
- Which states generate  $p_1, p_2$ ?
  - $\begin{array}{ccc} p_1 & p_2 \\ x & -1 & 0 \\ y & any & any \\ z & any & any \end{array}$
- Note p<sub>3</sub> (x= 1) does not add coverage.

# **Example: Path Coverage**

**if** (x < 0) /\*1\*/ { x:= - x /\*2\*/ } z = 1; /\*3\*/ **while** (x > 0) /\*4\*/ { z = z \* y; /\*5\*/ x = x - 1 /\*6\*/return z /\*7\*/



How many paths are there?

Let 
$$q_1 = [1,2,3]$$
  
 $q_2 = [1,3]$   
 $p = [4,5,6]$   
 $r = [4,7,E]$ 

then all paths are  $P = (q_1|q_2) p^* r$ 

Number of possible paths:  $|P| = 2 \cdot MaxInt - 1$ 



### Statement, Branch and Path Coverage

#### Statement Coverage:

- Necessary but not sufficient, not suitable as only test approach.
- Detects dead code (code which is never executed).
- About 18% of all defects are identified.

#### Branch coverage:

- Least possible single approach.
- Detects dead code, but also frequently executed program parts.
- About 34% of all defects are identified.

#### Path Coverage:

- Most powerful structural approach;
- Highest defect identification rate (100%);
- But no practical relevance.



# **Decision Coverage**

- Decision coverage is more then branch coverage, but less then full path coverage.
- Decision coverage requires that for all decisions in the program, each possible outcome is considered once.
- **Problem**: cannot sufficiently distinguish Boolean expressions.
  - For A || B, the following are sufficient:

А	В	Result
false	false	false
true	false	true

But this does not distinguish A || B from A; B is effectively not tested.



# **Decomposing Boolean Expressions**

The binary Boolean operators include conjunction x \Lapha y, disjunction x \Lapha y, or anything expressible by these (e.g. exclusive disjunction, implication)

#### **Elementary Boolean Terms**

An elementary Boolean term does not contain binary Boolean operators, and cannot be further decomposed.

- An elementary term is a variable, a Boolean-valued function, a relation (equality =, orders <, ≤, >, ≥, etc.), or a negation of these.
- This is a fairly syntactic view, e.g.  $x \le y$  is elementary, but  $x < y \lor x = y$  is not, even though they are equivalent.
- ► In formal logic, these are called **literals**.



# **Simple Condition Coverage**

- For each condition in the program, each elementary Boolean term evaluates to *True* and *False* at least once
- Note that this does not say much about the possible value of the condition
- Examples and possible solutions:

if (temperature > 90 && pressure > 120) { }						
True True False	<i>C2</i> True False True False	True False False				



# **Modified Condition Coverage**

- It is not always possible to generate all possible combinations of elementary terms, e.g. 3 <= x && x < 5.</p>
- In modified (or minimal) condition coverage, all possible combinations of those elementary terms the value of which determines the value of the whole condition need to be considered.
- ► Example:

3 <= x 8	&& x < 5	5
False False True True	True False	False

Another example: (x > 1 && ! p) || p



# **Modified Condition/Decision Coverage**

- Modified Condition/Decision Coverage (MC/DC) is required by DO-178B for Level A software.
- It is a combination of the previous coverage criteria defined as follows:
  - Every point of entry and exit in the program has been invoked at least once;
  - Every decision in the program has taken all possible outcomes at least once;
  - Every condition in a decision in the program has taken all possible outcomes at least once;
  - Every condition in a decision has been shown to independently affect that decision's outcome.



# **How to achieve MC/DC**

- Not: Here is the source code, what is the minimal set of test cases?
- Rather: From requirements we get test cases, do they achieve MC/DC?
- Example:
  - Test cases:

Test case	1	2	3	4	5
Input A	F	F	Т	F	Т
Input B	F	Т	F	Т	F
Input C	Т	F	F	Т	Т
Input D	F	Т	F	F	F
Result Z	F	Т	F	Т	Т

Source Code: Z := (A || B) && (C || D)

# **Question**: do test cases achieve MC/DC?

Source: Hayhurst *et al*, A Practical Tutorial on MC/DC. NASA/TM2001-210876





### **Summary**

- (Dynamic) Testing is the controlled execution of code, and comparing the result against an expected outcome
- Testing is (traditionally) the main way for verification.
- Depending on how the test cases are derived, we distinguish white-box and black-box tests
- In black-box tests, we can consider limits and equivalence classes for input values to obtain test cases
- In white-box tests, we have different notions of coverage: statement coverage, path coverage, condition coverage, etc.
- Next week: Static testing aka. static program analysis

