

Transfer functions to propagate information along the execution path (i.e. from input to output, or vice versa)

- ▶ Information is encoded as a lattice $L = (M, \sqsubseteq)$.
- Transfer functions mapping information
 - $f_l: M \to M$ with l being a label
 - ▶ Knowledge transfer is monotone $\forall x, y. x \sqsubseteq y \Rightarrow f_l(x) \sqsubseteq f_l(y)$
 - Restricted to a specific type of knowledge Pin (Reachable Definitions, Available Expressions,...)
- What about a more general approach Transfer function f Maintaining arbitrary knowledge ? Knowledge representation ? Pout

Software Verification

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- Software Verification proves properties of programs. That is, given the basic problem of program *P* satisyfing a property *p* we want to show that for all possible inputs and runs of P, the property p holds.
- ► Software verification is far more powerful than static analysis. For the same reasons, it cannot be fully automatic and thus requires user interaction. Hence, it is complex to use
- Software verification does not have false negatives, only failed proof attempts. If we can prove a property, it holds.
- Software verification is used in highly critical systems.

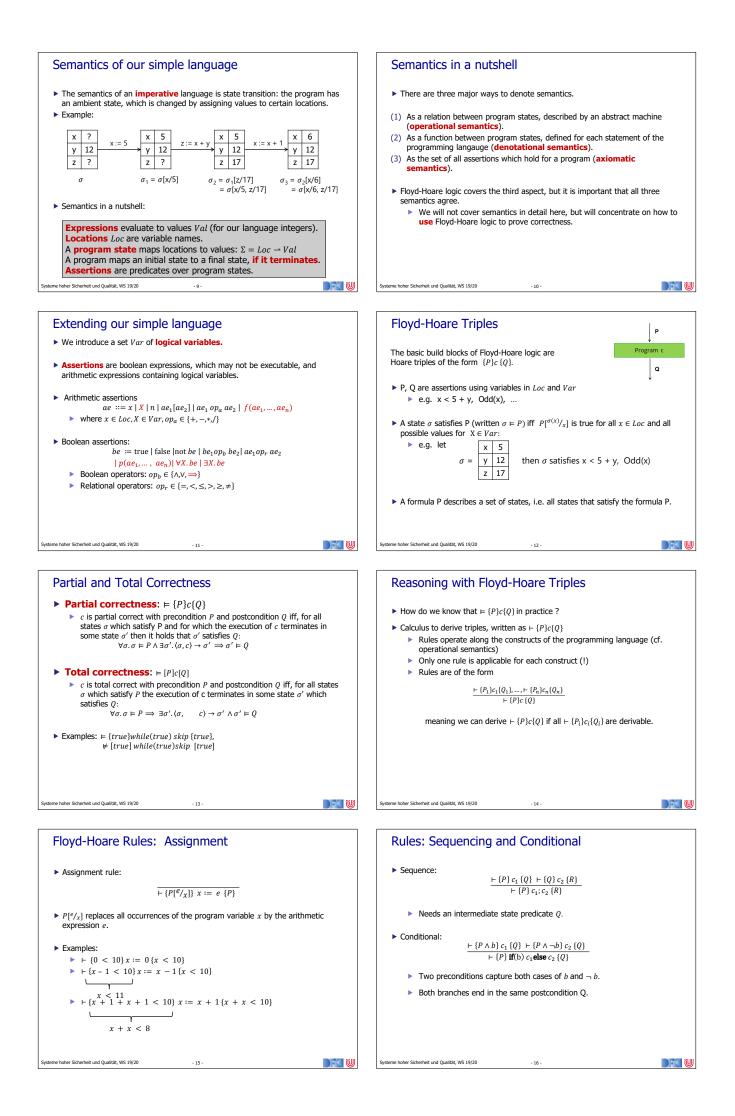
Recall our simple programming language Arithmetic expressions: $a ::= x \mid n \mid a_1[a_2] \mid a_1 \, op_a \, a_2$ Arithmetic operators: $op_a \in \{+, -, *, /\}$ Boolean expressions: $b := \text{true} \mid \text{false} \mid \text{not } b \mid b_1 o p_b \mid b_2 \mid a_1 o p_r \mid a_2$ ▶ Boolean operators: $op_b \in \{and, or\}$ ▶ Relational operators: $op_r \in \{=, <, \leq, >, \geq, \neq\}$ Statements: S ::= x := a | skip | S1; S2 | if (b) S1 else S2 | while (b) SLabels from basic blocks omitted, only used in static analysis to derive cfg. Note this abstract syntax, operator precedence and grouping statements is not covered.

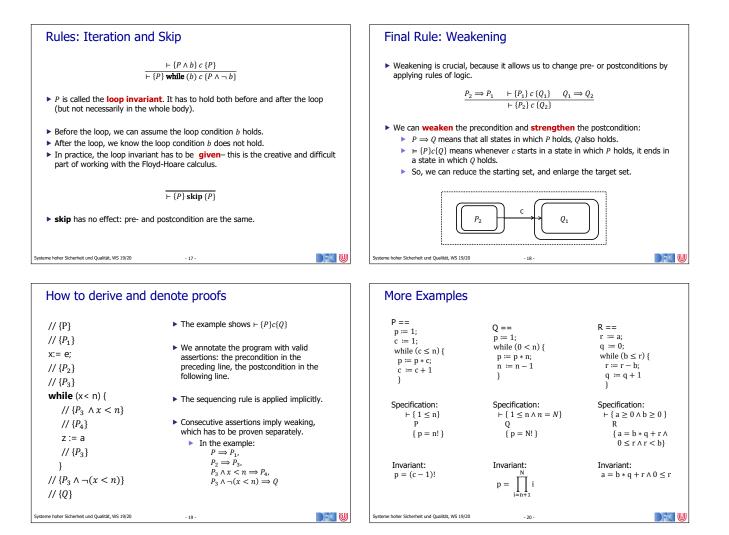
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How to find an Invariant

- Going backwards: try to split/weaken postcondition Q into negated loopcondition and "something else" which becomes the invariant.
- Many while-loops are in fact for-loops, i.e. they count uniformly:

i := 0;while $(i < n) \{$...;i := i + 1 $\}$

In this case:

- ▶ If post-condition is P(n), invariant is $P(i) \land i \leq n$.
- If post-condition is ∀j. 0 ≤ j < n. P(j) (uses indexing, typically with arrays), invariant is ∀j. j ≤ 0 < i. i ≤ n ∧ P(j).</p>

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Summary

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- Floyd-Hoare-Logic allows us to prove properties of programs.
- ► The proofs cover all possible inputs, all possible runs.
- There is partial and total correctness:
 - Total correctness = partial correctness + termination.
- There is one rule for each construct of the programming language.
- Proofs can in part be constructed automatically, but iteration needs an invariant (which cannot be derived mechanically).
- Next lecture: correctness and completeness of the rules.

