

# Towards Merging *Plat* $\Omega$ and PGIP

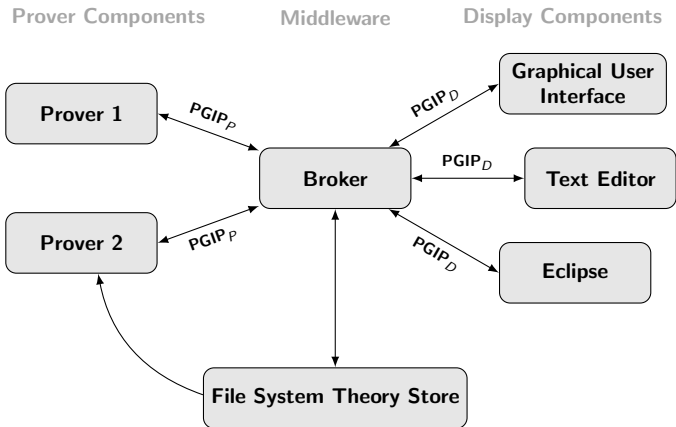
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User Interfaces for Theorem Provers  
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# PGKIT Architecture



- ▶ ACL2, Isabelle, HOL, Lambda-Clam, Lego, Plastic, Phox, ...
- ▶ ASCII Files (Input-only)
- ▶ Specific parsers
- ▶ Command-Line oriented
- ▶ Single focus
- ▶ Display of proof state

```
emacs@lume <-->
File Edit Options Buffers Tools ProofGeneral Help

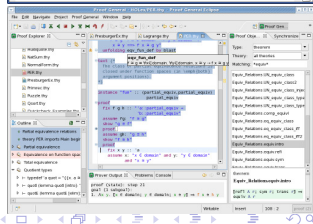
by (induct x, simp+)

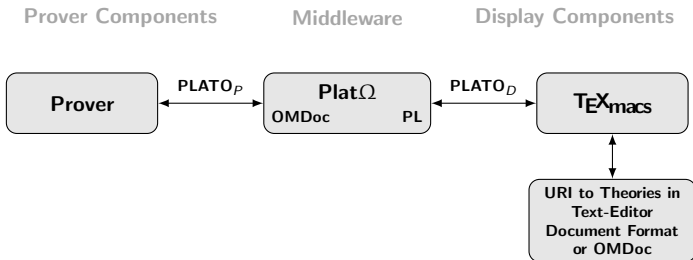
lemma add_S: "S (x+ y) = x+ (S y)"
by (induct x, simp+)

text{* Now we can prove commutativity. *}

theorem add commute: "x+ y = y+ x"
proof (induct x rule: N.induct)
  case Z thus ?case by (simp add: add_Z r)
  case S thus ?case by (simp add: add_S)
qed
end

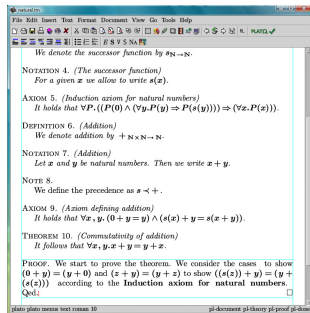
-1:** NN.thy* Bot L133 (ProofGeneral)
proof (state) step 1
□
goal (2 subgoals):
  1. Z + y = y + Z
  2. !!N. N + y = y + N ==> S N + y = y + S N
-1:** *response* 95% L162 (PGResp)-----
```







- ▶ Writing  $\text{T}_{\text{EX}}_{\text{MACS}}$  documents assisted by  $\Omega\text{MEGA}$
- ▶  $\Omega\text{MEGA}$ : OMDoc Input/Output
- ▶  $\text{T}_{\text{EX}}_{\text{MACS}}$ : Specific, flexible proof document style (PL)
- ▶ Multiple foci
- ▶ Bidirectional: proof steps done by the prover are propagated into the  $\text{T}_{\text{EX}}_{\text{MACS}}$  document
- ▶ XUPDATE/XMLDIFF based
- ▶ On the fly conversions between OMDoc and PL
- ▶ Context-sensitive menus for assistance





	<i>Plat</i> Ω Display	PG Kit Display	<i>PGIP</i> 2 Display
Document format	<b>X</b> ML	Plain text	<b>X</b> ML
Document syntax	<b>T</b> E <sub>X</sub> <sub>MACS</sub>	ASCII	<b>G</b> eneric
Change protocol	<b>X</b> Update	<i>PGIP</i> <sub>D</sub>	<b>X</b> Update
Operations	<b>C</b> ontext- <b>d</b> ependent <b>m</b> enus	Global menus, <b>t</b> yed <b>o</b> perations	<b>C</b> ontext-dependent <b>m</b> enus, <b>t</b> yed <b>o</b> perations



	<i>Plat</i> $\Omega$ Prover	PG Kit Prover	<i>PGIP</i> 2 Prover
Document format	<b>XML</b>	Plain text	<b>XML</b>
Document syntax	OMDOC	Native prover syntax	<b>Generic</b>
Change protocol	<b>XUpdate</b>	PGIP <sub>P</sub>	<b>XUpdate</b>
Prover support	$\Omega$ MEGA	<b>Generic (Coq, Isabelle, etc)</b>	<b>Generic (Coq, Isabelle, <math>\Omega</math>MEGA, etc)</b>
Operations	Context-dependent menus	Global menus, typed operations	Context-dependent menus, typed operations

# Overview of Extensions for PGIP 2



- ① Support for Semi Structured Documents
  - Multiple Foci
  - XUpdate/Semantic XMLDiff
  - Protocols
- ② Context-Sensitive Service Menus
- ③ Multiple Editing Displays in Parallel
- ④ Multiple Document Formats

Working hypothesis: Do not require any change for current displays/provers when using the new PGIP 2



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```
theory NN
imports Main
begin
```

```
text {* The datatype of natural numbers\footnote{Not
the real ones!}. *}
datatype N = Z | S N
```

```
text {* Induction is a derived concept: @{thm N.induct}
*}
```

```
text {* We define addition via recursive
equations, and declare its usual syntax. *}

```

```
fun "add" :: "N \ $\rightarrow$  N \ $\rightarrow$  N"
where
  "add Z x = x"
| "add (S x) y = S (add x y)"
```

```
notation
```

```
add (infixr "+" 65)
```

```
text {* We first need two lemmas. *}

```

```
lemma add_Z_r: "x + Z = x"
by (induct x, simp+)
```

```
lemma add_S: "S (x + y) = x + (S y)"
by (induct x, simp+)
```

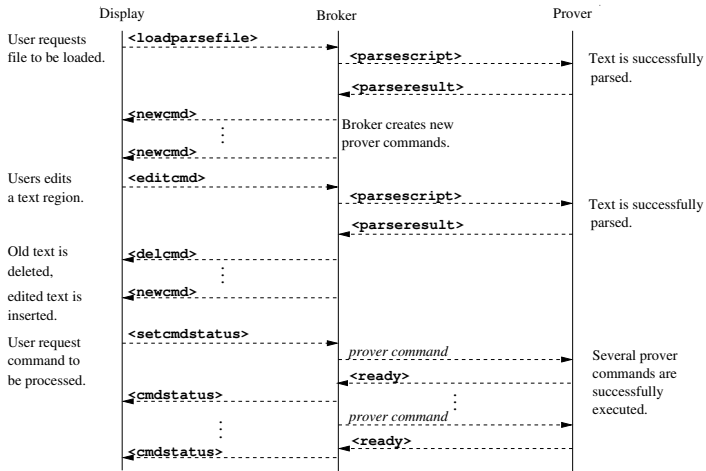
```
text {* Now we can prove commutativity. *}

```

```
theorem add_commute: "x + y = y + (x::N)"
proof (induct x rule: N.induct)
  case Z thus ?case by (simp add: add_Z_r)
  case S thus ?case by (simp add: add_S)
qed
```

```
end
```

# Unstructured Documents





```
<pgip tag = "Isabelle/Isar" id = "hume/cxl/27572/1208530140.785"
  destid =
  "broker:hume/2658/27571/2008318-144859-Z" class = "pg" refid =
  "broker:hume/2658/27571/2008318-144859-Z" refseq = "18" seq =
  "24"><parseresult>
```

```
<opentheory thyname = "NN" parentnames = "Main">theory NN
imports Main
begin</opentheory><openblock objtype = "theory body" />
```

```
<theoryitem objtype = "theory declaration">text {* The datatype of
natural numbers\footnote{Not the real ones!}. *}</theoryitem
>
```

```
<theoryitem objtype = "theory declaration">datatype N = Z | S N</
theoryitem>
```

```
<theoryitem objtype = "theory declaration">text{* Induction is a
derived concept: @{thm N.induct} *}</theoryitem>
```

```
<theoryitem objtype = "theory declaration">text{* We define addition
via recursive equations,
and declare its syntax as the usual infix operator. *}</theoryitem>
```

```
<theoryitem objtype = "theory declaration">fun &quot;add&quot;; :: &
quot;N \&lt;Rightarrow&gt;; N \&lt;Rightarrow&gt;; N&quot;;
```

where

```
&quot;add Z x = x&quot;;
| &quot;add (S x) y = S (add x y)&quot;;</theoryitem>
```

```
<pgip> ———— <opentheory/>
               <openblock/>
               <theoryitem/>
               <opengoal/>
               <openblock/>
               <proofstep/>
               <closeblock/>
               <closegoal/>
               <closeblock/>
               <closetheory/>
```

# Semi Structured Documents



```
<pgip tag = "Isabelle/Isar" id = "hume/cxl/27572/1208530140.785"
  destid =
  "broker:hume/2658/27571/2008318-144859-Z" class = "pg" refid =
  "broker:hume/2658/27571/2008318-144859-Z" refseq = "18" seq =
  "24">
```

```
<parseresult>
```

```
<document>
```

```
<theory thymname="NN" parentnames="Main">theory NN
```

```
imports Main
```

```
begin
```

```
<block objtype="theory body">
```

```
<theoryitem>text {* The datatype of natural numbers\footnote{Not
  the real ones!}. *}</theoryitem>
```

```
<theoryitem type="adt">datatype N = Z | S N</theoryitem>
```

```
<theoryitem>text {* Induction is a derived concept: @{thm N.induct}
  *}</theoryitem>
```

```
<theoryitem>text {* We define addition via recursive equations,
  and declare its syntax as the usual infix operator. *}</theoryitem>
```

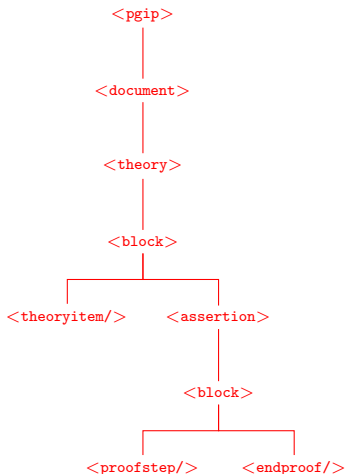
```
<theoryitem objtype="fundef">fun &quot;add&quot;; :: &quot;N \&lt;
  Rightarrow&gt;; N \&lt;Rightarrow&gt;; N&quot;;
```

```
where
```

```
&quot;add Z x = x&quot;;
```

```
| &quot;add (S x) y = S (add x y)&quot;;</theoryitem>
```

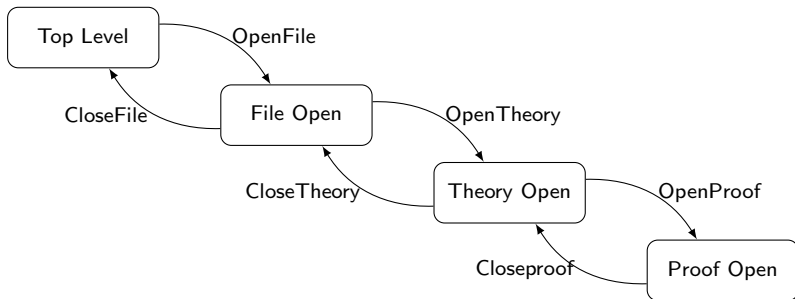
```
<theoryitem objtype="notation">notation
```

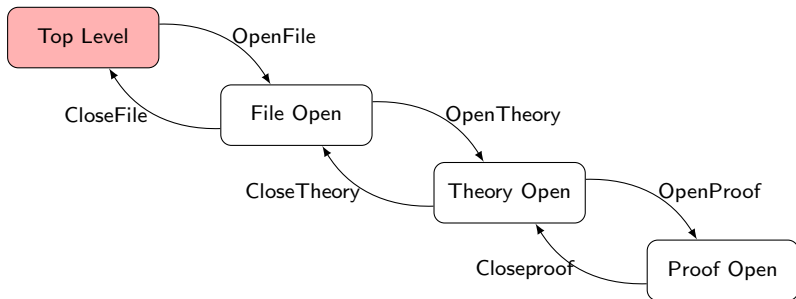


# Supporting Semi Structured Documents

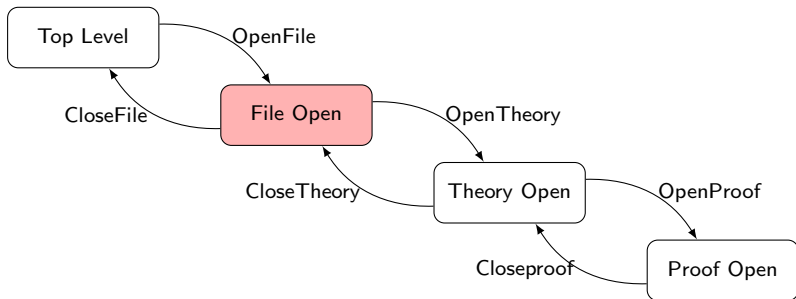


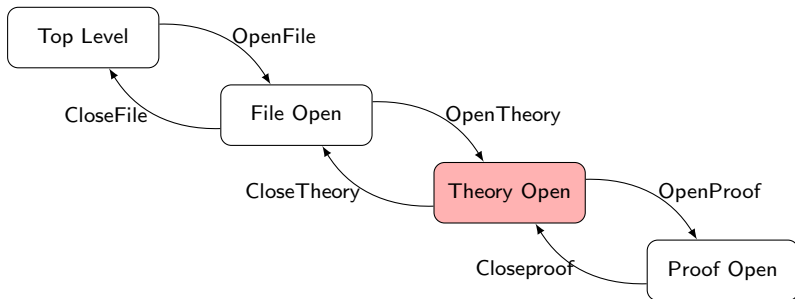
- ▶ New internal PGIP markup (PGML), tree compatible
  - ▶ Use `xml:id` to flexibilise document structure  
Example: theorems and proofs need not occur together physically
  - ▶ Rigid structure computed by the broker for the prover
- ▶ Provide on-the-fly converters between old and new markup  
⇒ provers need not be adapted
- ▶ Configuration

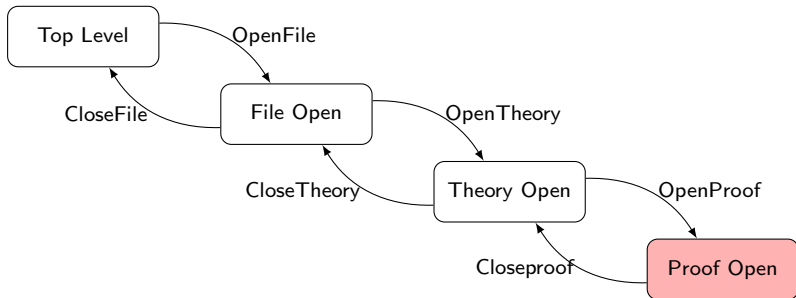




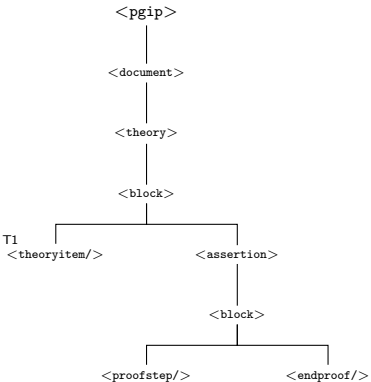
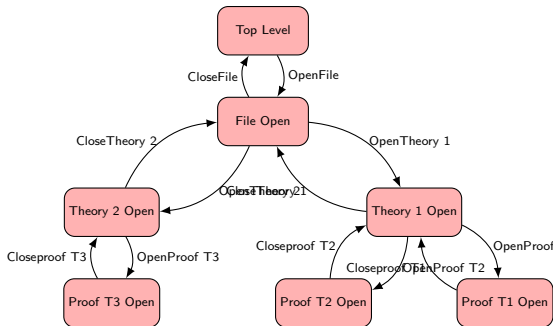








# Multiple Foci



# Supporting Semi Structured Documents



- ▶ New internal PGIP markup, tree compatible
- ▶ Provide on-the-fly converters between old and new markup  
⇒ provers need not be adapted
- ▶ Configuration

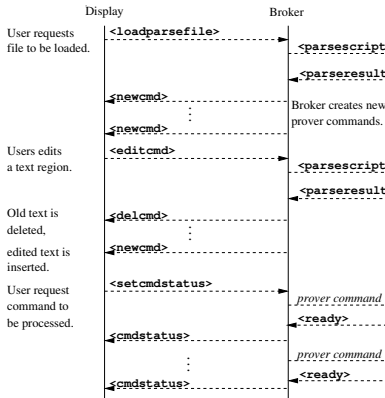


## Old PGIP<sub>D</sub> protocol (asymmetric):

- ▶ Display → Broker: <createcmd>, <editcmd>
- ▶ Broker → Display: <newcmd>, <delcmd>, <replacecmd>

## New PGIP<sub>D</sub> protocol:

- ▶ Rephrase in terms of Xupdate-modifications  
<insert-after>, <insert-before>, <remove>





- ▶ XUPDATES cannot be generated by all displays or provers
- ▶ Allow components to send only new document version and compute differences inside the broker
- ▶ Use semantic XMLDIFF tool inside the broker
  - ▶ Normal tree diff
  - ▶ Configurable to take some “semantics” into account
  - ▶ Configurable level of granularity for modifications
- ▶ Configuration if component can handle XUPDATES  
Broker generates appropriate representation for each component

# Protocol between Prover and Broker

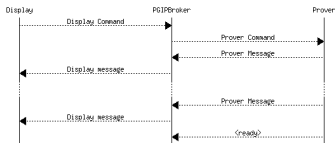


- ▶ `<parsescript>` and `<parseresult>`
- ▶ Prover commands in native prover command syntax
- ▶ prover answers `<normalresponse>`, `<errorresponse>`, `<ready>`

Unchanged, but contextualized (multiple foci)

Extension:

- ▶ `<normalresponse>` can contain XUPDATES for document which are relayed to the display





# Protocols between Display with Broker



In addition to PGIP<sub>D</sub> provide

- ▶ XML-RPC interface and
- ▶ HTTP in plain REST architecture

## HTTP Request

`/initsession`  
`/session1/initdocument?CONTENT`  
`/session1/document/1`  
`/session1/document/HEAD`

## HTTP answer

path to new session (`/session1`)  
HTML rendered document after parsing  
version 1 of the document  
the current version of the document

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- ▶ Allow requests of **service menu** for arbitrary elements in the display
- ▶ Requests relayed by the broker to the prover
- ▶ Prover returns menu description (PGML menu format)
  - ▶ Menus contain descriptions and actions
  - ▶ Actions can be
    - ▶ tactic calls (traditional)
    - ▶ requests for axiom/lemma applications ( $Plat\Omega/TeX_{MACS}$ )
- ▶ Computing the complete menus is expensive, most of the menu is discarded
- ▶ Support lazy menu computation
  - ▶ Menu entries trigger computations which results are modifications of the menu

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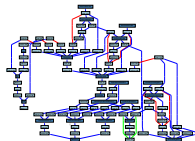
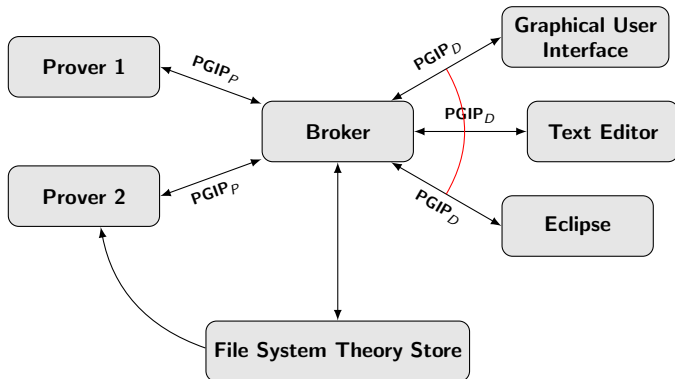
# Multiple Editing Displays



Prover Components

Middleware

Display Components



```

    (The following are the Axioms of the Theory of Numbers)
    Axiom 1. (Induction axiom for natural numbers)
    It holds that  $\forall P. (P(1) \wedge (\forall x. P(x) \Rightarrow P(x+1))) \Rightarrow (\forall x. P(x))$ 
    Axiom 2. (Addition)
    Let  $a$  and  $b$  be natural numbers. Then we write  $a + b$ .
    Axiom 3. (Associativity of addition)
    It holds that  $\forall a. \forall b. \forall c. (a + (b + c)) = (a + b) + c$ .
    Axiom 4. (Commutativity of addition)
    It holds that  $\forall a. \forall b. a + b = b + a$ .
    Axiom 5. (Zero is the neutral element for addition)
    It holds that  $\forall a. a + 0 = a$  and  $0 + a = a$ .
    Axiom 6. (Cancellation law for addition)
    It holds that  $\forall a. \forall b. \forall c. a + b = a + c \Rightarrow b = c$ .
    Axiom 7. (Addition)
    Let  $a$  and  $b$  be natural numbers. Then we write  $a + b$ .
    Axiom 8. (Associativity of addition)
    It holds that  $\forall a. \forall b. \forall c. (a + (b + c)) = (a + b) + c$ .
    Axiom 9. (Commutativity of addition)
    It holds that  $\forall a. \forall b. a + b = b + a$ .
    Axiom 10. (Zero is the neutral element for addition)
    It holds that  $\forall a. a + 0 = a$  and  $0 + a = a$ .
    Axiom 11. (Cancellation law for addition)
    It holds that  $\forall a. \forall b. \forall c. a + b = a + c \Rightarrow b = c$ .
    PROOF: We start to prove the theorem. We consider the case: to show
     $\forall a. \forall b. \forall c. (a + b = a + c \Rightarrow b = c)$  we show  $(\forall x. (a + x = a + c) \Rightarrow x = c)$ 
    according to the Induction axiom for natural numbers.
    [Q.E.D.]
  
```

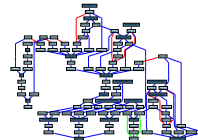
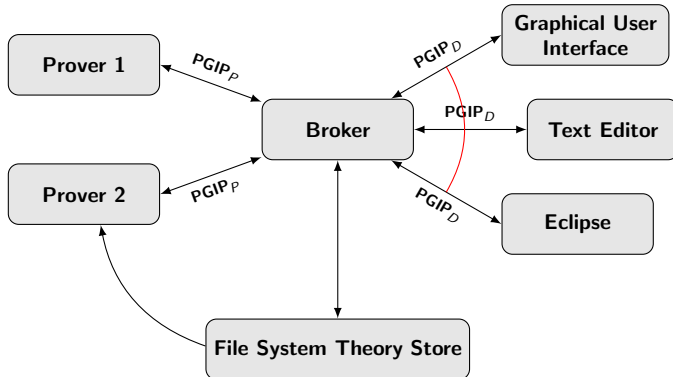
# Multiple Editing Displays



Prover Components

Middleware

Display Components



```

1. We show that  $\forall x \in \mathbb{N} \exists y \in \mathbb{N} (x + y = 0)$ .
2. We show the necessary lemmas by  $\text{no-}\omega$ .
3.
4. (The successor function)
   For a given  $x$  we define its  $\text{succ}(x)$ .
5. (Induction axiom for natural numbers)
   It holds that  $\forall P. (P(0) \wedge (\forall x. P(x) \Rightarrow P(\text{succ}(x)))) \Rightarrow (\forall x. P(x))$ .
6. (Addition)
   Let  $a$  and  $b$  be natural numbers. Then we write  $a + b$ .
7. (Addition)
   We define the predecessor as  $a \leftarrow$ .
8.
9. (Arith. defines addition)
   It holds that  $\forall x. \forall y. \forall z. (x + (y + z)) = (x + y) + z$ .
10. (Commutativity of addition)
    It follows that  $\forall x. \forall y. x + y = y + x$ .
11.
12. Proof: We start to prove the theorem. We consider the case: to show
     $\forall x \in \mathbb{N} \exists y \in \mathbb{N} (x + y = 0)$  and let  $x \in \mathbb{N}$  be given. We show  $\exists y \in \mathbb{N} (x + y = 0)$ 
    according to the induction axiom for natural numbers.
    QED.

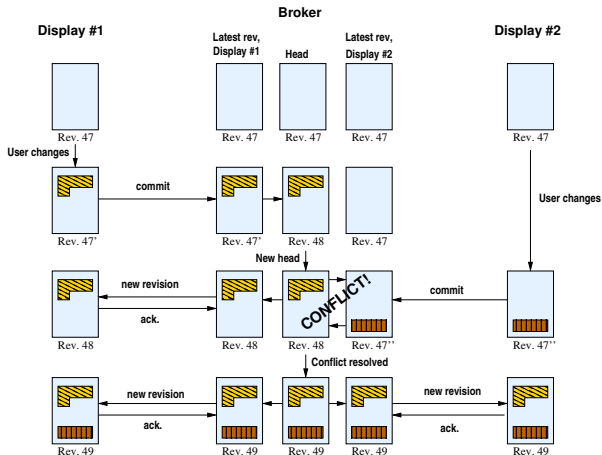
```

Requires Synchronisation by the Broker

# Multiple Displays



- ▶ Simple kind of version control inside the broker
- ▶ Broker stores for each display the latest version communicated
- ▶ Uses semantic XMLMerge (diff3)
- ▶ Conflicts are marked in special markup extending XUpdate markup.



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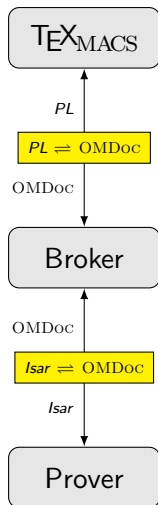
# Multiple Document Formats



- ▶ Have: Display  $D$  communicates in format  $A$
- ▶ Have: Prover  $P$  communicates in format  $B$
- ▶ Wanted: Use display  $D$  with prover  $P$

For instance:

- ▶ *Plat* $\Omega$  connects  $\text{TEX}_{\text{MACS}}$  with format  $PL$  to  $\Omega\text{MEGA}$  with format  $\text{OMDoc}$
- ▶ Now want to use  $\text{TEX}_{\text{MACS}}$  with Isabelle (*Isar*)



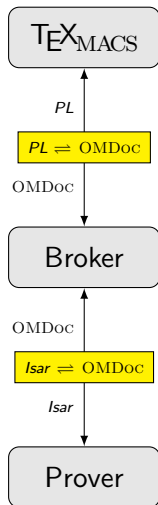
# Multiple Document Formats



- ▶ Have: Display  $D$  communicates in format  $A$
- ▶ Have: Prover  $P$  communicates in format  $B$
- ▶ Wanted: Use display  $D$  with prover  $P$

For instance:

- ▶  $Plat\Omega$  connects  $TEX_{MACS}$  with format  $PL$  to  $\Omega$ MEGA with format  $OMDOC$
  - ▶ Now want to use  $TEX_{MACS}$  with Isabelle (Isar)
- Provide autonomous converters from  $PL$  to  $OMDOC$  and  $OMDOC$  and Isar
- ▶ Bidirectional
  - ▶ Conversion of Xupdates
  - ▶ Maintain mappings to relay service requests





- ▶ Semi-structured input documents  
*MathsTiles* (structured input to multiple domain reasoners, unidirectional)
- ▶ Multiple foci  
 $\Omega$ MEGA (status management added), Isabelle (multi-foci under the way)
- ▶ Multiple displays  
MATITA (proof script, goal display), L $\Omega$ UI, GEOPROOF/ COQ
- ▶ Support modifications to the document from the prover:  
MATITA (tinycals)  
Could be realised by the generic functionality proposed here?



- ▶ Implementation (any feedback/remarks welcome before we start. . . )
- ▶ Implement *Plat* $\Omega$  functionality on PGIP 2 basis
- ▶ Connect other editing displays (Word 2007, OpenOffice, Netbeans)
- ▶ Multiple foci, changes from prover could serve interaction styles in other provers (Agda, Mizar, PVS)