From syllogism to common sense: a tour through the logical landscape

Categorical syllogisms – Part 2

Mehul Bhatt Oliver Kutz Thomas Schneider

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Categorical syllogisms

What happened so far?

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What happened so far?

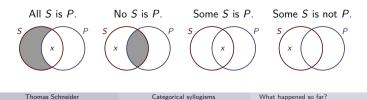
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Categorical propositions (CPs)

... state relations between classes:

Example	General form	Name
All policitians are liars.	All S is P.	A Universal affirmation
No policitians are liars.	No S is P.	E Universal negation
Some policitians are liars.	Some S is P.	I Particular affirmation
Some policitians are not liars.	Some $S$ is not $P$ .	${f 0}$ Particular negation

### ... can be interpreted via Venn diagrammes:



### What happened so far?

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What happened so far?

Categorical propositions (CPs)

... have a quantity, quality and distribution:

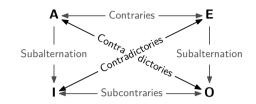
Proposition		Quantity	Quality	Distributes
All S is P.	Α	Universal	Affirmative	S
No S is P.	Е	Universal	Negative	<i>S</i> , <i>P</i>
Some S is P.	I.	Particular	Affirmative	
Some S is not P.	0	Particular	Negative	Р

Distribution: "Does the proposition make a statement about all members of S or P?"



### Immediate inferences

... via square of opposition:



### Further inferences:

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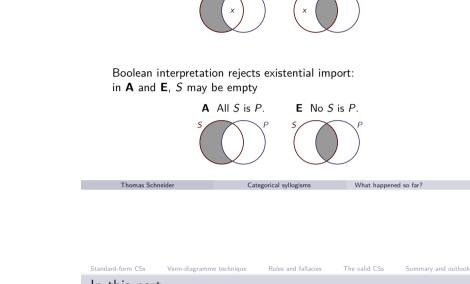
Standard-form CSs Venn-diagramme technique

- Conversion ( $S \mapsto P, P \mapsto S$ ; not always successful)
- Obversion (Change quality,  $P \mapsto \text{non-}P$ )
- Contraposition ( $S \mapsto \text{non-}P, P \mapsto \text{non-}S$ ; not always succ.)

Rules and fallacies

Categorical syllogisms

Categorical syllogisms



Aristotelian versus Boolean interpretation

Aristotelian interpretation assumes existential import:

E No S is P.

A All S is P.

What happened so far?

*S* is nonempty

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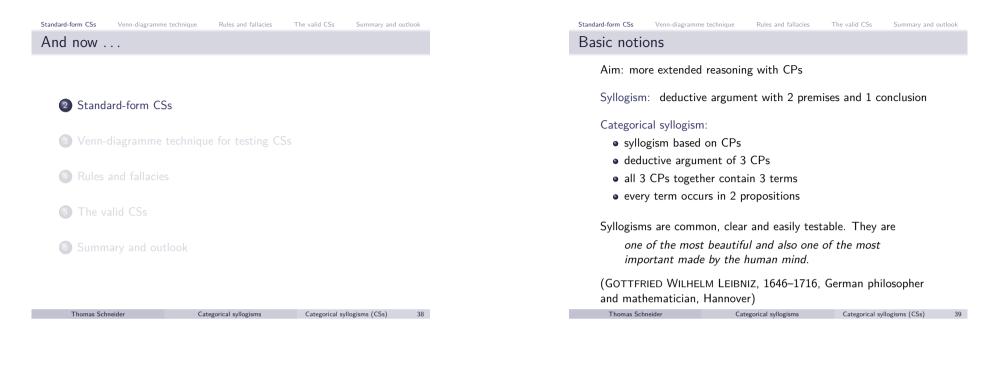
36

What happened so far?

The valid CSs Summary and outlook

Categorical syllogisms (CSs)

Categorical syllogisms Categorical syllogisms (CSs)



# Standard-form CSs Venn-diagramme technique Rules and fallacies The valid CSs Summary and outlook Standard-form CSs

- Premises and conclusion are standard CPs (A, E, I, O)
- OPs are arranged in standard order:

$$\frac{ \dots S_1 \text{ is } \dots P_1 }{ \dots S_2 \text{ is } \dots P_2 }$$

P: major term, S: minor term

Remember: 3 terms altogether, each in 2 propositions!  $\rightsquigarrow S_1, S_2, P_1, P_2$  consist of P, S and a third term: the middle term

Major premise contains P, MMinor premise contains S, M

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### Major term, minor term, middle term

All great scientists are college graduates. Some professional athletes are college graduates. Therefore some professional athletes are great scientists.

All artists are egotists. Some artists are paupers. Therefore some paupers are egotists.

40

Categorical syllogisms (CSs)

#### Standard-form CSs Summary and outlook Standard-form CSs Venn-diagramme technique Rules and fallacies The valid CSs Venn-diagramme technique Rules and fallacies The valid CSs Summary and outlook Figure of a CS Mood of a CS Figure of a CS: combination of order of S, M, P in the premises: Mood of a CS is the pattern of types of its three CPs, No P is M P-MSome S is not M has figure in the order major premise - minor premise - conclusions S–M ∴ All S is P · S-P A All artists are egotists. Some artists are paupers. 1 Mood All I Therefore some paupers are egotists. $\sim$ 4 figures: $\rightarrow 4^3 = 64 \mod s$ M–P (1)(2) *P*–*M* (3) M-P (4) P–M $\frac{S-M}{\therefore S-P}$ $\frac{M-S}{\therefore S-P}$ S–M M–S *∴ S*–P ∴ *S*–*P*

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And now	
2 Standard-form CSs	
3 Venn-diagramme technique for testing CSs	
4 Rules and fallacies	
5 The valid CSs	
6 Summary and outlook	
	<ul> <li>And now</li> <li>Standard-form CSs</li> <li>Venn-diagramme technique for testing CSs</li> <li>Rules and fallacies</li> </ul>

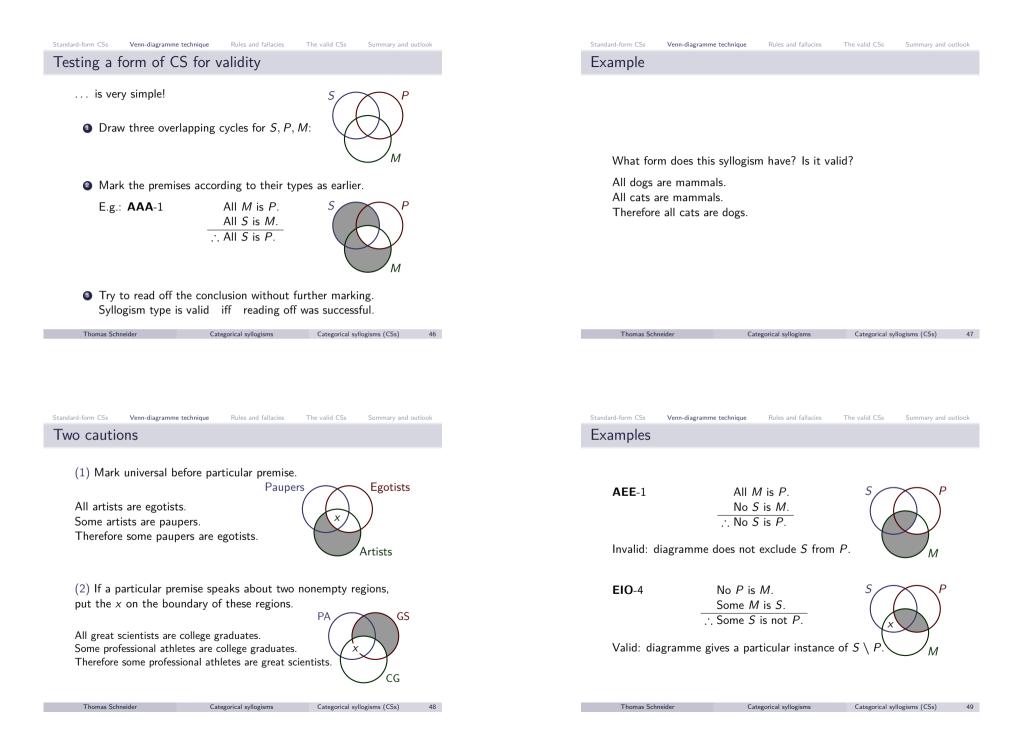
Categorical syllogisms (CSs)

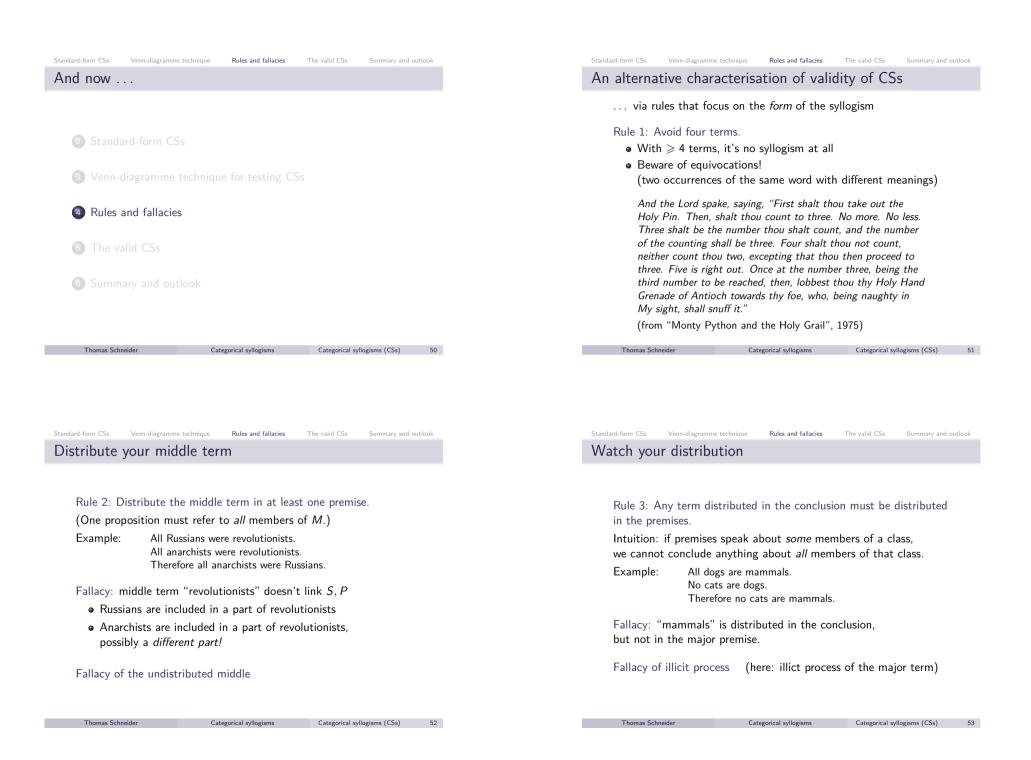
44

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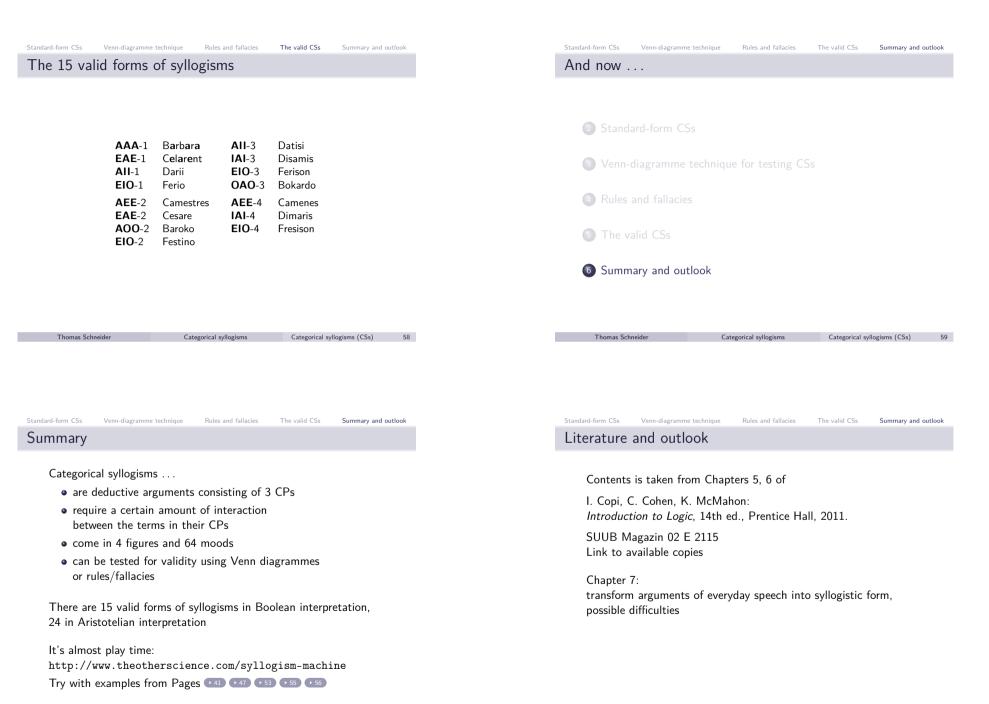
Standard-form CSs Venn-diagramme technique Rules and fallacies Standard-form CSs The valid CSs Summary and outlook Venn-diagramme technique Rules and fallacies Summary and outlook Two negative premises are bad Don't turn neg into pos Rule 5: If  $\ge 1$  premise is negative, the conclusion must be neg. Rule 4: Avoid two negative premises. • 2 negative premises • Affirmative conclusion  $\hat{=}$  one of *S*, *P* is (wholly or partly)  $\sim 2 \times$  class exclusion between S, M and between P, M contained in the other. • No power to enforce any relation between S, P• Can only be inferred if premises assert existence of M which contains one of S, P and is contained in the other • Try all nine possibilities in a Venn diagramme! • Class inclusion only via affirmative propositions Example: No artists are accountants. Example: No poets are accountants. Some poets are not accountants. Some artists are poets. Therefore some poets are not artists. Therefore some artists are accountants. Fallacy of exclusive premises Fallacy of drawing an affirmative conclusion from a neg. premise Categorical syllogisms Categorical syllogisms (CSs) Categorical syllogisms (CSs) Thomas Schneider 54 Thomas Schneider Categorical syllogisms 55 Standard-form CSs Venn-diagramme technique Rules and fallacies The valid CSs Standard-form CSs The valid CSs Summary and outlook Venn-diagramme technique Rules and fallacies Summary and outlook Don't be so Aristotelian And now . . . 2 Standard-form CSs Rule 6: From two universal premises, no particular conclusion may 3 Venn-diagramme technique for testing CSs be drawn. Example: All household pets are domestic animals. No unicorns are domestic animals. A Rules and fallacies Therefore some unicorns are not household pets. 5 The valid CSs Existential fallacy (not a fallacy in the Aristotelian interpretation) 6 Summary and outlook

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56

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Categorical syllogisms (CSs) 60

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61

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Standard-form CSs Venn-diagramme technique Rules and fallacies The valid CSs Summary and outlook

Literature and outlook

Contents is taken from Chapters 5, 6 of

I. Copi, C. Cohen, K. McMahon: Introduction to Logic, 14th ed., Prentice Hall, 2011.

SUUB Magazin 02 E 2115 Link to available copies

Chapter 7: transform arguments of everyday speech into syllogistic form, possible difficulties

## Thank you.

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61